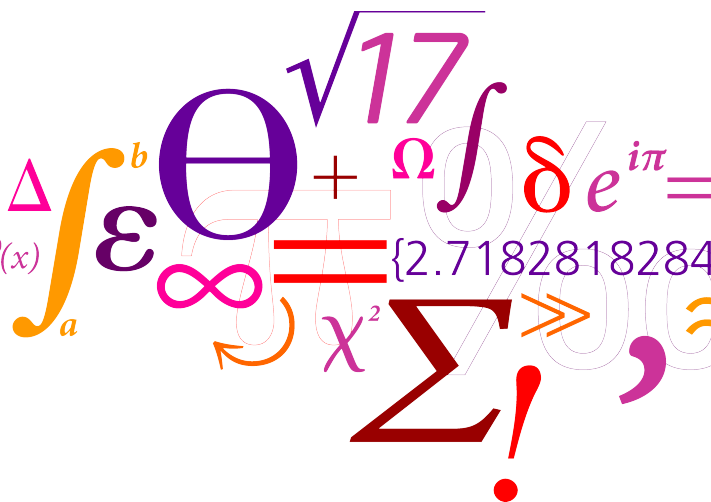


Task Mapping and Partition Allocation for Mixed-Criticality Real-Time Systems

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$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$


Outline

- Motivation
- System and application models
- Problem formulation and example
- Optimization strategy
- Experimental results
- Conclusions

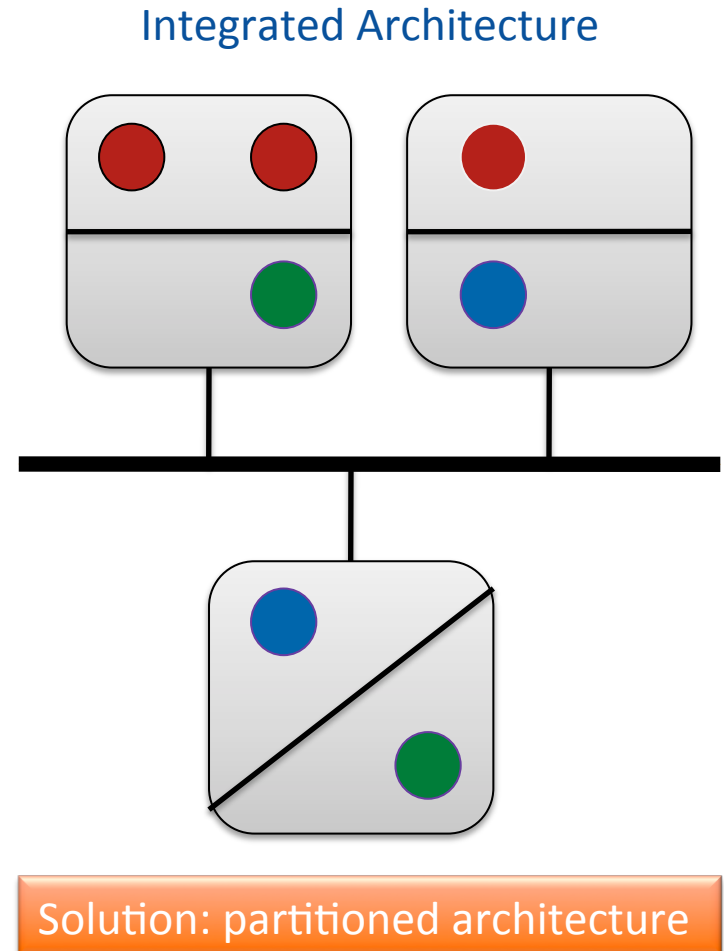
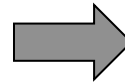
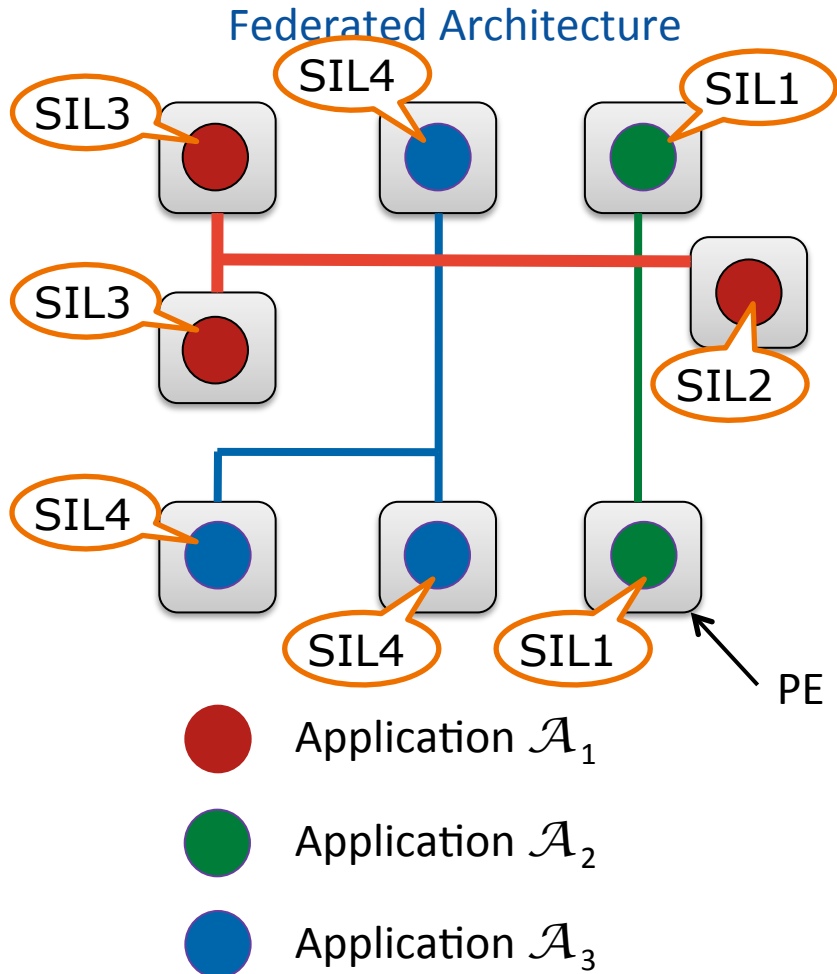
Motivation

- **Safety** is the property of a system that will not endanger human life or the environment
- A safety-related system needs to be **certified**
- A Safety Integrity Level (SIL) is assigned to each safety related function, depending on the required level of risk reduction
- There are 4 SILs:
 - SIL4 (most critical)
 - SIL1 (least critical)
 - SIL0 (non-critical) – not covered by standards
- SILs dictate the development process and certification procedures

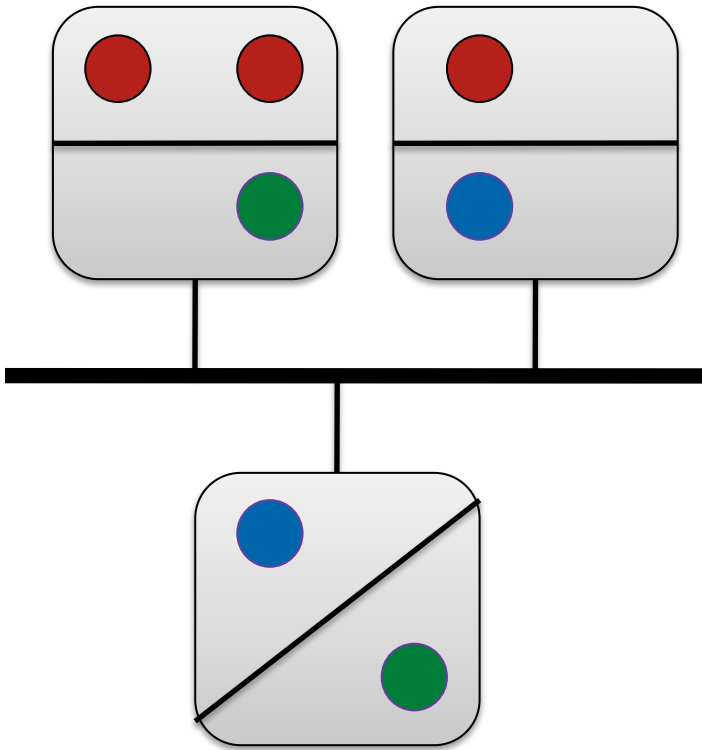
Motivation

- Real time applications implemented using distributed systems

- Mixed-criticality applications share the same architecture

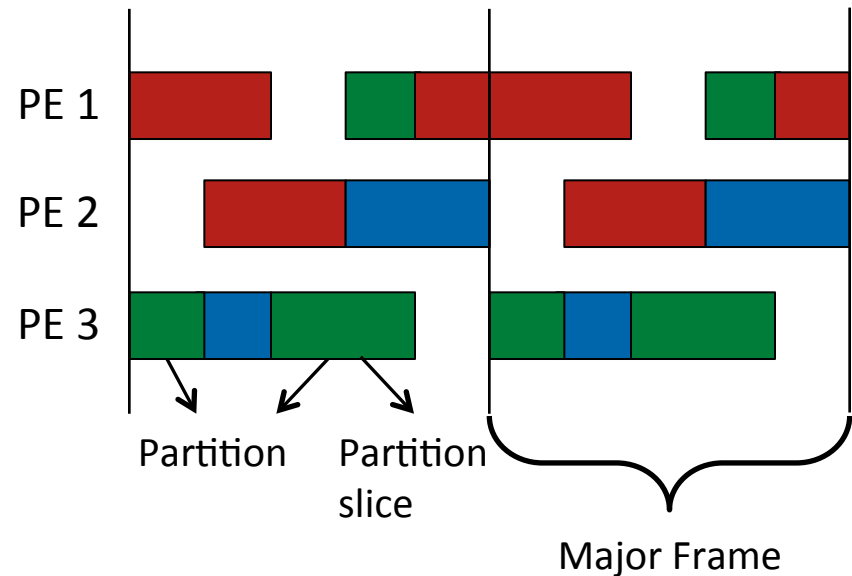
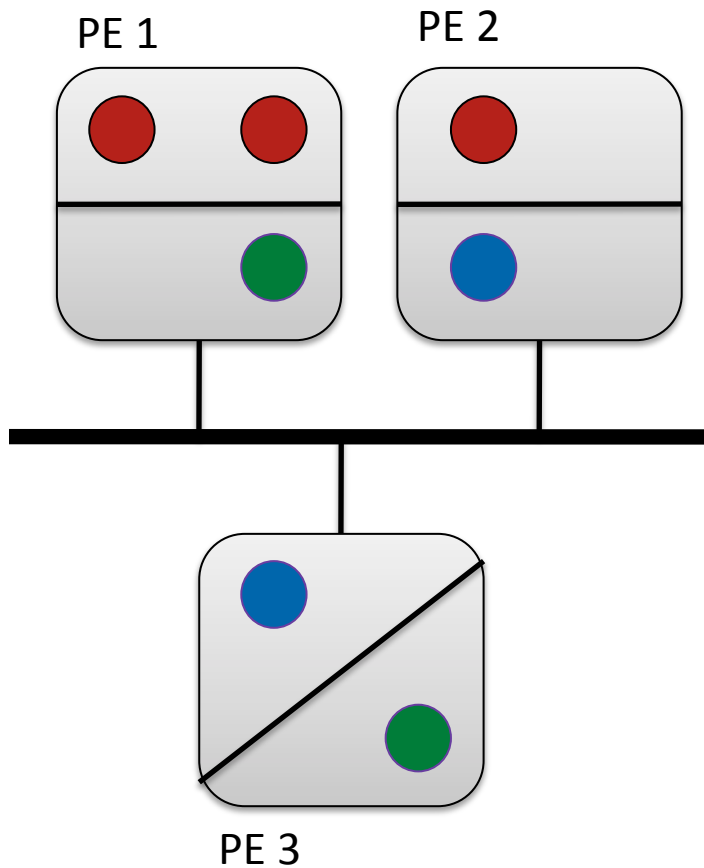


System Model



- Partition = virtual dedicated machine
- Partitioned architecture
 - Spatial partitioning
 - protects one application's memory and access to resources from another application
 - Temporal partitioning
 - partitions the CPU time among applications

System Model

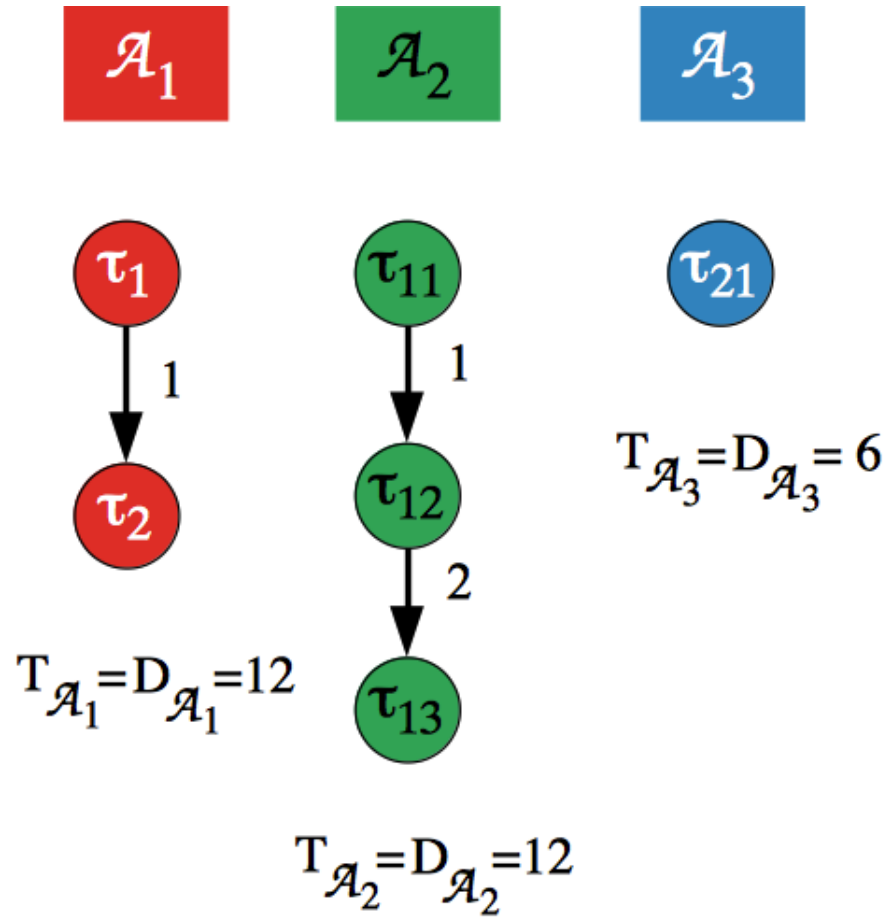


- Temporal partitioning
 - Static partitioning
 - Real-time scheduling
 - Real-time scheduling period MF
 - Each partition can have its own scheduling policy
 - A partition has a certain SIL

Problem: optimize task mapping and allocation of partitions

Application Model

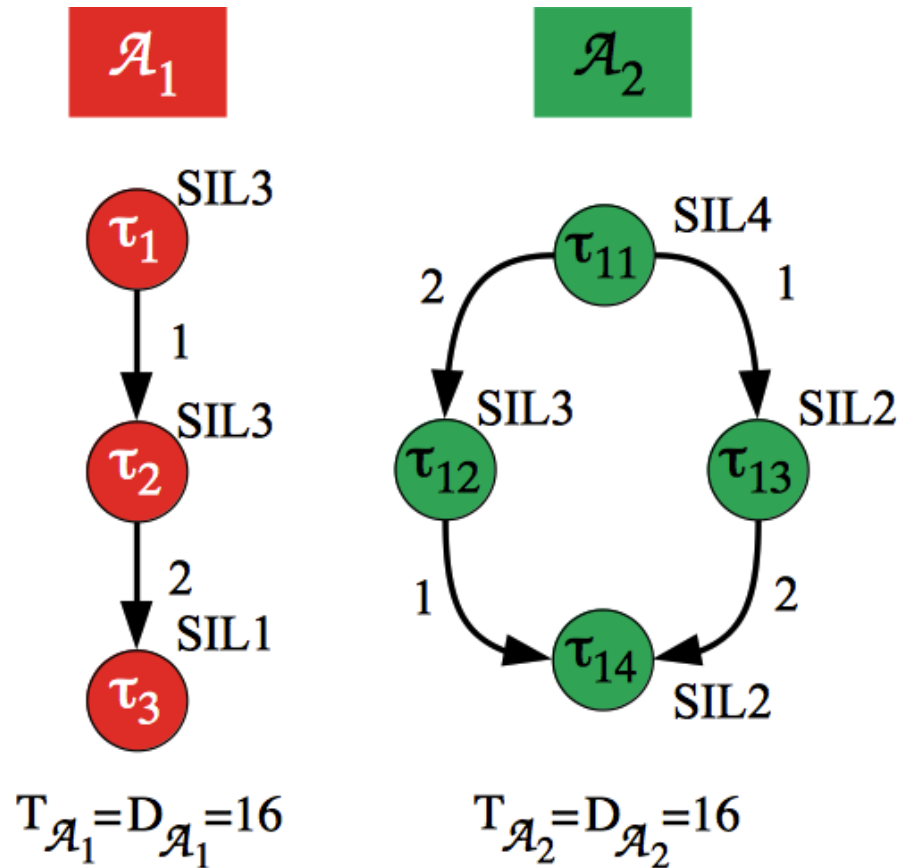
- Static Cyclic Scheduling



Problem formulation

- Given
 - A set of applications
 - The criticality level (or SIL) for each task
 - A set of N processing elements (PEs)
 - The size of the Major Frame and of the Application Cycle
- Determine
 - The mapping of tasks to PEs
 - The sequence and length of partition slices on each processor
 - The assignment of tasks to partitions
 - The schedule for all the tasks in the system
- Such that
 - All applications meet their deadline

Motivational Example

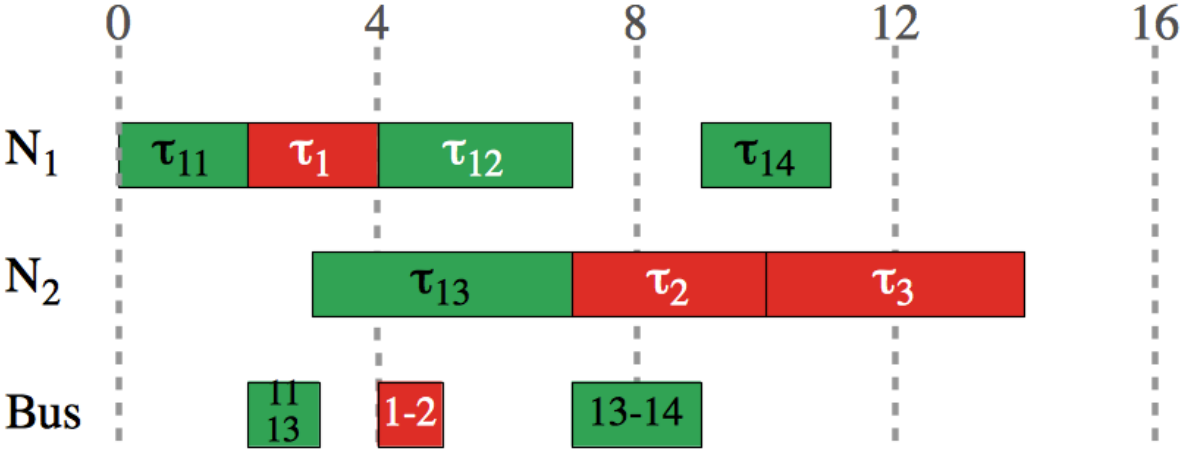


Mixed-criticality applications

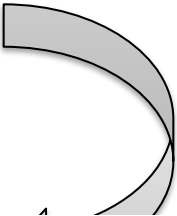
	N_1	N_2	
\mathcal{A}_1	τ_1	2	4
	τ_2	x	3
	τ_3	3	4
\mathcal{A}_2	τ_{11}	2	3
	τ_{12}	3	5
	τ_{13}	x	4
	τ_{14}	2	3

WCET and mapping restrictions

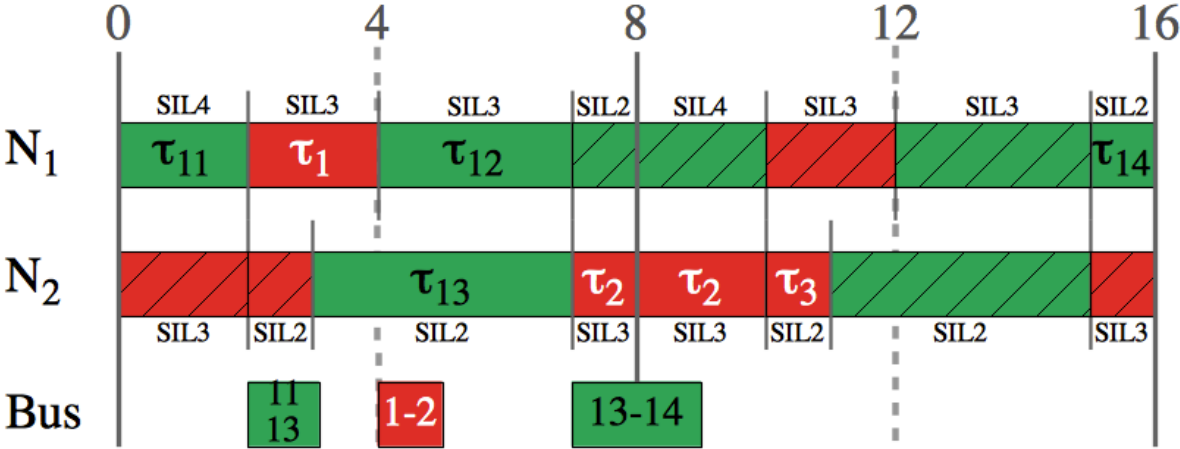
Motivational Example



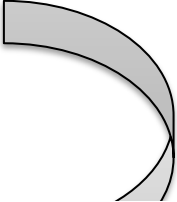
Optimal mapping,
without considering
partitions.



Motivational Example



Partitioning, using the previously obtained mapping. τ_3 and τ_{14} miss their deadline.



Optimization Strategy

- Mapping and Time-Partitioning Optimization (MTPO) strategy:
 - Tabu Search meta-heuristic
 - The mapping of tasks to processors
 - The sequence and length of partition slices on each PE
 - The assignment of tasks to partitions
 - List scheduling
 - The schedule for the applications
- Tabu Search
 - Minimizes the cost function
 - Explores the solution space using design transformations

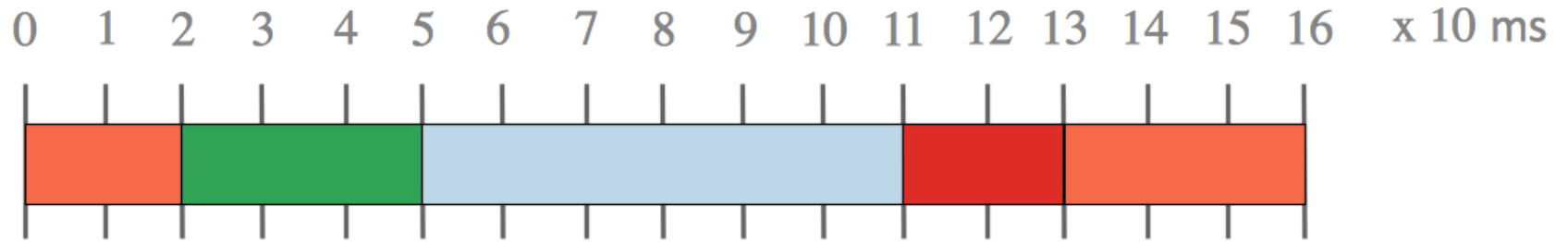
Optimization Strategy

- Degree of schedulability
 - Captures the difference between the worst-case response time and the deadline

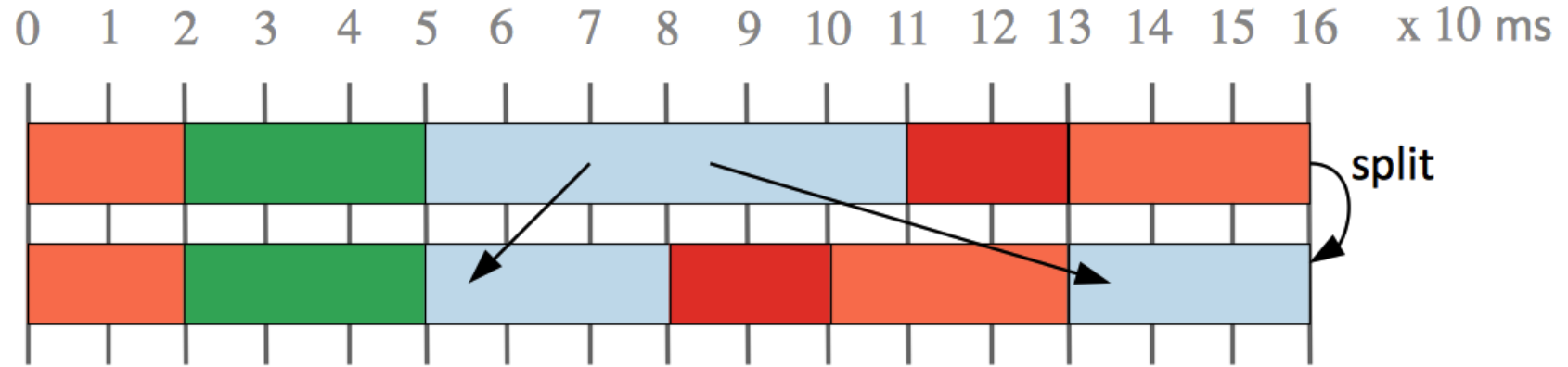
- Cost Function

$$Cost(\Psi) = \begin{cases} c_1 = \sum_{\mathcal{A}_i \in \Gamma} \max(0, R_i - D_i) & \text{if } c_1 > 0 \\ c_2 = \sum_{\mathcal{A}_i \in \Gamma} (R_i - D_i) & \text{if } c_1 = 0 \end{cases}$$

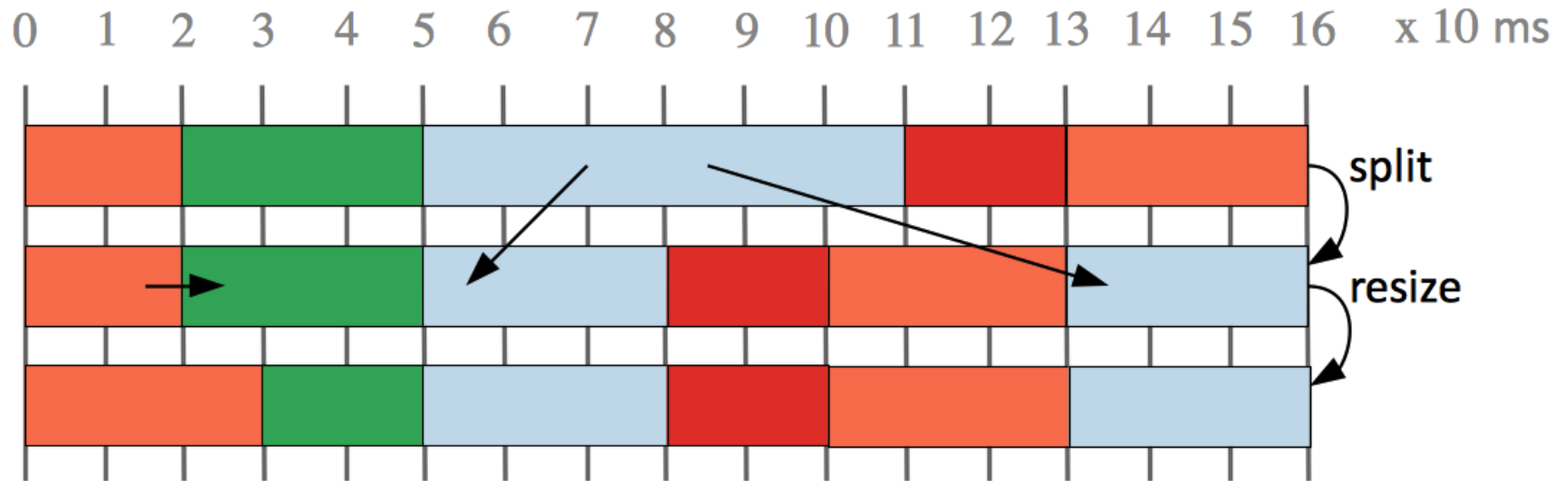
Optimization Strategy: Design Transformations



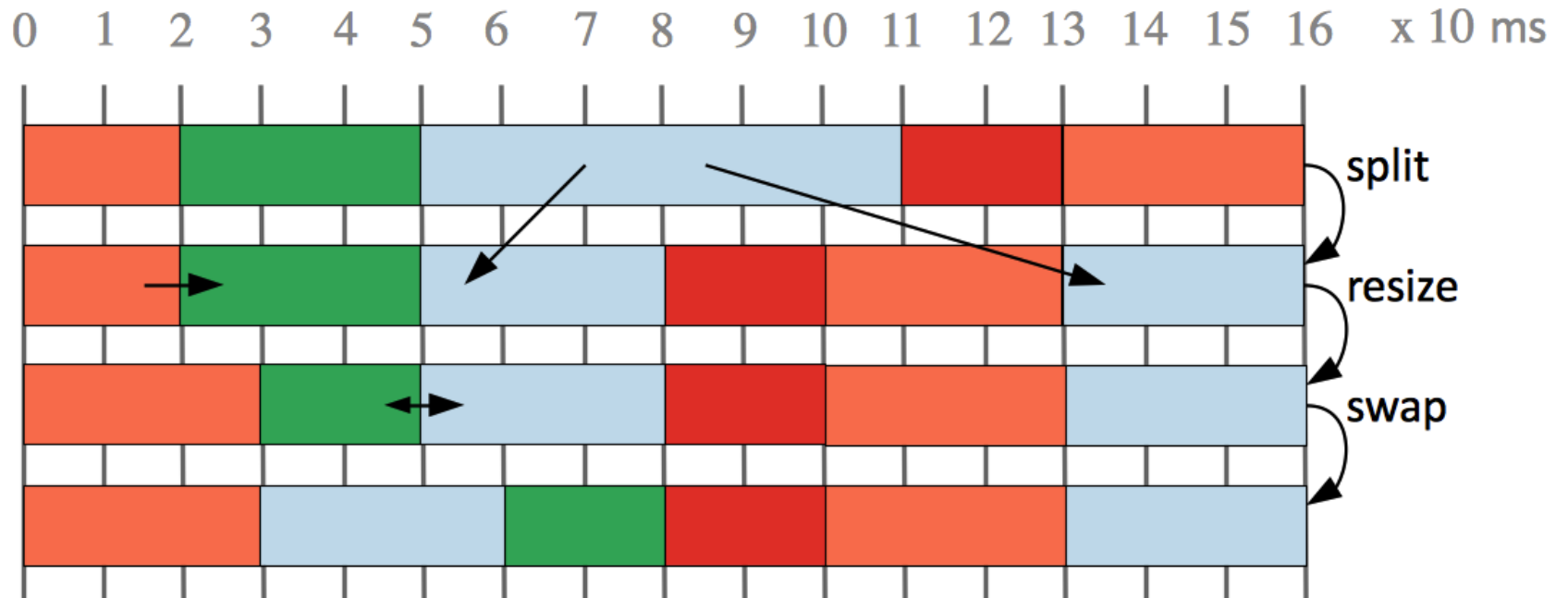
Optimization Strategy: Design Transformations



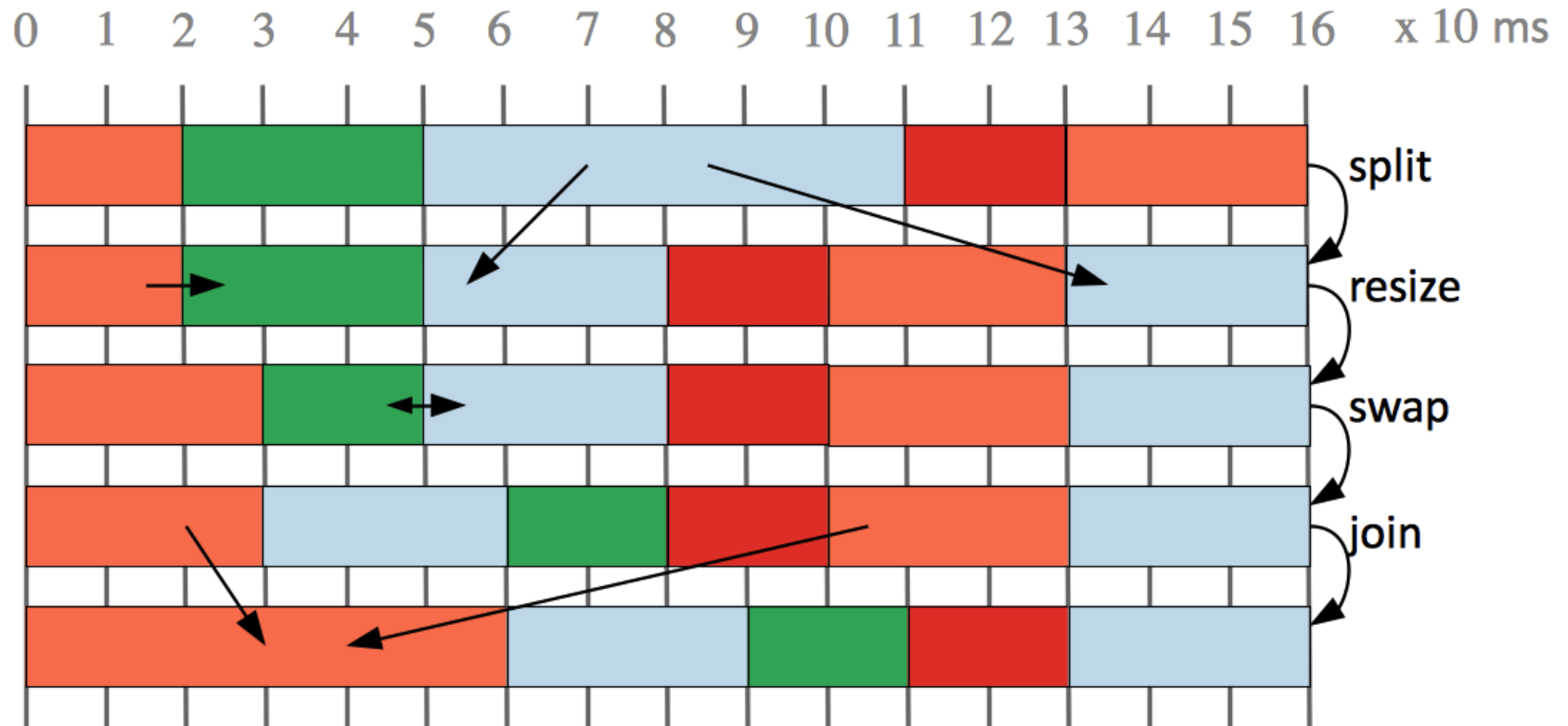
Optimization Strategy: Design Transformations



Optimization Strategy: Design Transformations



Optimization Strategy: Design Transformations



- Task re-assignment

Experimental Results

- Benchmarks
 - 5 synthetic
 - 3 real life test cases from E3S
- MTPO compared to:
 - MO+TPO
 - Optimization where first we do a mapping optimization, without considering partitioning (MO), and then we perform a partitioning optimization, considering the mapping obtained previously as fixed (TPO)

Experimental Results

Test Case	Apps	Tasks	PE	MO+TPO	MTPO	% increase
1	3	15	2	0	3	261.54
2	3	20	3	2	3	223.81
3	4	34	4	2	3	78.13
4	4	40	5	2	4	153.66
5	5	53	6	4	5	3116.67
consumer	2	12	3	2	2	19.88
networking	4	13	3	4	4	55.52
telecom	9	30	3	3	9	100.01

Conclusions

- Mixed-criticality systems, with applications of different criticalities running on the same processors, are implemented using a partitioned architecture.
- Optimizing the time partitions and the task allocation to partitions leads to schedulable solutions with improved resource utilization.
- We proposed a Tabu Search based optimization algorithm.

Thank you!

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