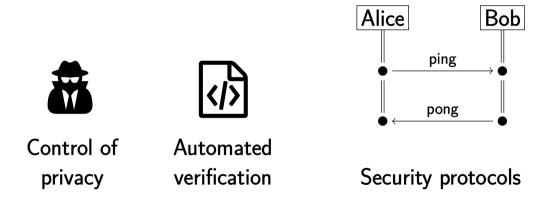
How to Verify Privacy Automatically

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1. We should formally verify privacy in many applications



Electronic voting



Contact tracing



Mobile payments, transport, e-passports...



2. We can define privacy goals in a declarative and intuitive way with logic

(lpha,eta)-privacy



3. Automated verification of (α, β) -privacy is practical

Decision procedure and prototype tool [1]



Challenge 25 by the bartender: private information disclosed



The Bourne Identity, 2002



Challenge 25 by the bartender: private information disclosed



The Bourne Identity, 2002



Protocol specification

 $\begin{array}{l} \begin{array}{l} \begin{array}{l} Tag \\ \star \ T \in Tags. \end{array} \\ \mathcal{K} := r(T). \\ r(T) := h(\mathcal{K}). \\ \operatorname{snd}(g(\mathcal{K})).0 \end{array}$

```
Readerrcv(x).try T = getT(x) ins := state(T).try s' = extract(x, s) instate(T) := h(s').snd(ok).0
```

- Processes with atomic transactions
- Intruder controlling the network
- Crypto API

(lpha,eta)-privacy

- Formula α = payload, over alphabet $\Sigma_0 \subset \Sigma$
- Formula β = technical information, over alphabet Σ
- Violation of privacy = β excludes some models of α

Example: unlinkability for two sessions $\alpha \equiv T_1, T_2 \in \text{Tags}$ Question: $T_1 \stackrel{?}{=} T_2$

Example: voting



- $\alpha \equiv \textit{v}_1, \textit{v}_2, \textit{v}_3, \textit{v}_4 \in \{0, 1\} \land \textit{v}_1 + \textit{v}_2 + \textit{v}_3 + \textit{v}_4 = 2$
- β includes α and encrypted ballots etc.

Example: voting



- $\alpha \equiv \textit{v}_1, \textit{v}_2, \textit{v}_3, \textit{v}_4 \in \{0, 1\} \land \textit{v}_1 + \textit{v}_2 + \textit{v}_3 + \textit{v}_4 = 2$
- β includes α and encrypted ballots etc.
- If $\beta \Rightarrow \mathbf{v_1} = \mathbf{v_4} \land \mathbf{v_2} = \mathbf{v_3}$: privacy violation

Protocol excerpt

```
. . .
* x in Agent.
* y in {yes, no}. # Flip a coin
receive M.
try N := dcrvpt(inv(pk(s)), M) in
if y = yes then
  new R. send crypt(pk(x),pair(ves,N),R)
else
  new R. send crypt(pk(x),no,R)
```

```
. . .
```

Multi message-analysis problem

Several possibilities

$$(y = yes, [\dots, I \mapsto \{yes, N\}_{pk(x)}])$$

 $(y = no, [\dots, I \mapsto \{no\}_{pk(x)}])$

The concrete execution corresponds to one of them

One multi message-analysis problem = one pair (α, β)

Automated verification

Challenges:

- Undecidable problem
- Infinite state space
- Proofs!

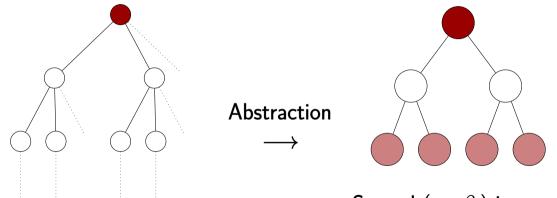
Methods:

- Restriction to a (large) class of protocols + bound
- Constraints solving with abstractions

- We verify privacy as a *reachability property* in a transition system
- We use the *lazy intruder* (finite branching when the intruder is sending messages)
- In each state, we represent several executions
- We normalize states so that, in each state, all possibilities are "equivalent"

Symbolic representation

 (α, β) in every state



Several (α_i, β_i) in every symbolic state

- Paper on decision procedure with correctness and termination proofs
- Prototype tool implemented in Haskell
- Models and case study for several existing protocols
- Paper on typing result for guaranteeing well-typed attacks

- Compositionality result: how to combine protocols securely?
- Development of the tool (user-friendliness)
- Support for a larger class of protocols



- We should formally verify privacy in many applications
 We can define privacy goals in a declarative and intuitive way with logic, using (α, β)-privacy
- **6** Automated verification of (α, β) -privacy is practical

References

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