

## 02424 Week 12

Since you are having the Assignment No. 3 today's exercise is rather limited. You should simply derive the likelihood function needed for solving Assignment No. 3, ie. (given Theorem 5.10) you must show that

$$\begin{aligned} \ell(\boldsymbol{\mu}, \boldsymbol{\Sigma}, \boldsymbol{\Sigma}_0; \bar{x}_{1+}, \dots, \bar{x}_{k+}) = & \hspace{20em} (1) \\ & -\frac{N-k}{2} \log(\det(\boldsymbol{\Sigma})) - \frac{1}{2} \text{tr}((SSE)\boldsymbol{\Sigma}^{-1}) - \sum_{i=1}^k \left[ \frac{1}{2} \log \left( \det \left( \frac{\boldsymbol{\Sigma}}{n_i} + \boldsymbol{\Sigma}_0 \right) \right) \right. \\ & \left. + \frac{1}{2} (\bar{x}_{i+} - \boldsymbol{\mu})^T \left( \frac{\boldsymbol{\Sigma}}{n_i} + \boldsymbol{\Sigma}_0 \right)^{-1} (\bar{x}_{i+} - \boldsymbol{\mu}) \right] \end{aligned}$$