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Abstract

This paper consists of two parts: A philosophy part and a terse summary of my April 2019 ACM Trans. on Software Engineering and Methodology paper on *Domain Analysis & Description*.

In the philosophy part, Sect. 3, we outline Kai Sørlander's philosophy on what must necessarily be in any description of any world.

In the domain analysis & description part, Sects. 4–9, we present a new preamble for software engineering, one that precedes requirements engineering. We outline two calculi: one for the analysis of the endurants of human artefact "dominated" domains, and one for their description. By a transcendental deduction endurant domain descriptions are translated into perdurant domain descriptions: manifest parts becoming behaviours.

We show how the ontology of the second part is basically founded on the necessities of description outlined in the first part — thereby contributing to a philosophy basis for computing.

1 Introduction

Before **software** can be **design**ed the programmer must **grasp** its requirements. Before **requirements** are **prescribed** the engineer must **grasp** an **adequate extent** of the **domain** in which that software is to serve. **But do software engineers today have a sufficient grasp of their target domains**?

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By an adequate (domain) we do not mean "an entire, full, complete" domain, but a sizable part of it — usually "somewhat more" than entailed by [subsequent] requirements. By a grasp (of a domain) we mean an understanding that enables us to **reason** about the domain. Our 'reasonable grasp' is, we suggest, manifested in some text; that is, in some language.

In order to *reason* we we expect that language to be **formal**; that is, to have a formal **syntax**, a formal, mathematical **semantics** and a **proof system**. We no not expect the **domain**, the **requirements** and the **software design** [incl. coding] languages to be the same, one **specification** language.

Ideally software development, therefore, to us, entails three major phases: **domain engineering** in which we analyze and describe the domain, \mathscr{D} , in which the software is to serve; **requirements engineering** in which we "derive" the requirements, \mathscr{R} , that the software is to fulfill; and **software design** in which we finally arrive, via one or more steps of software design, \mathscr{S} .

Domain descriptions express properties of the chosen domain. Requirements prescriptions express desired properties of the desired software, not how it is implemented. Software designs express how requirements are to be satisfied by executable code.

Software, \mathscr{S} , is expected to fulfill customer *expectations*, hence must be based on *domain understanding*, \mathscr{D} , and to be *correct* with respect to requirements, \mathscr{R} . We can express this formally: $\mathscr{R} \models \mathscr{D}$ (\mathscr{R} models \mathscr{D}), respectively $\mathscr{D}, \mathscr{S} \models \mathscr{R}$ (\mathscr{S} , in the context of \mathscr{D} , models \mathscr{R}). This obviously means that we

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expect developers to consider domain, requirements and software specifications (incl. code) as mathematical objects and that tests, model checks and theorem proofs ideally be carried out accordingly.

The above portrays a **hypothetical situation**. Today's software engineering essentially has no domain engineering phase. This current situation is unlike any other engineering. The classical disciplines of chemical, civil, electrical and mechanical engineering all build on the sciences of physics. Major software systems are today developed without a proper understanding of their underlying domain. It seems that software engineering today starts, "at best", with requirements engineering.

The present paper, as well as its precedent papers [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 14], lead us to claim that domain science & engineering offers a compelling *new foundation for software development*. Physics is the basis for all branches classical of engineering. So, we claim, [that] domain science, is a basis for all software. We shall, however, cover only a fragment of this basis.

2 Domain Science & Engineering

DEF.1: By a **domain** we shall understand a **rationally describable** segment of a **human assisted** reality. That is, of the world, its physical parts: natural ["God-given"] and artefactual ["man-made"], and living species: plants and animals including, notably, humans DEF.2: By rationally describable we mean describable using, for example, the principles, techniques and analysis & description prompts of this paper and detailed in [12] DEF.3: By human assisted reality we mean a universe of discourse with at least one artefactual phenomenon and as monitored & controlled by at least one human • We present an essence of two calculi: a *calculus* of **domain analysis prompts** and a *calculus* of **domain description prompts**. We shall only present the prompts, not their algebra, that is, not the laws of combined uses of prompts. DEF.4: By a prompt we shall here mean an act of encouraging the domain analyser cum describer, that is, a human, to do something, here: to analyse and/or describe **DEF.5**: By **domain analysis** we mean an inquiry, by domain analysers, i.e., humans, into the make-up of a domain, with the analysis resulting in affirmative answers, to questions like "is, what I am observing, such-and-such" – true or false **DEF.6**: By a **domain description** we mean a textual document, both informal, the narrative, and formal, the specification **The narrative** is a natural language text which in terse statements introduces the names of the domain, and, possibly, also the definitions, of sorts (types) of syntactic and semantic entities, actions, events and behaviours, and axioms; not anthropomorphically, but by emphasizing their properties. The formal specification is a collection of sort, or type definitions, function and behaviour definitions, together with axioms and proof obligations constraining the definitions. So the problem is to analyse and describe a domain, that is, to describe physical parts, whether natural or man-made, and, in [rare] cases also living species: plants and animals, notably humans. The next many sections shows how we tackle, and hence expect others to tackle that problem. The approach takes its departure in **philosophy**. Most decisively in the philosophy of Kai Sørlander.

3 Some Issues of Philosophy

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The question is: "What must inavoidably be in any description ?" We take it as the necessary characteristics of any domain is equivalent with the conceptual, logical conditions for any possible description of that domain. Sørlander, after careful studies [24, 25, 27, 31] of all possibly relevant philosophers' work, puts forward the thesis of the possibility of truth and then basing transcendental deductions on indisputable logical relations to arrive at the conceptual, logical conditions for any possible description of that domain. The starting point, now, in a series of deductions, is that of logic and that we can assert a property, \mathcal{P} , and its negation $\neg \mathcal{P}$; and that these two assertions cannot both be true, that is, that $\mathcal{P} \land \neg \mathcal{P}$ cannot be true. So the possibility of truth is a universally valid condition. When we claim that, we also claim the contradiction principle. The implicit meaning theory is this: "in assertions there are mutual dependencies between the meaning of designations and consistency relation between assertions". When we claim that a philosophy basis is that of the possibility of truth, then we assume that this basis include the contradiction principle

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and the implicit meaning theory. We shall also refer to the implicit meaning theory as the inescapable meaning assignment. As an example of what "goes into" the inescapable meaning assignment, we bring, 22 albeit from the world of computer science, that of the description of the stack data type (its endurants and operations). 23

_ An Inescapable Meaning Assignment Example, Narrative The meaning of designations: 1 Stacks, s:S, have elements, e:E; 2 the empty_S operation takes no arguments and yields a result stack; 3 the is_empty_S operation takes an argument stack and yields a Boolean value result. 4 the stack operation takes two arguments: an element and a stack and yields a result stack. 5 the unstack operation takes an non-empty argument stack and yields a stack result. 6 the top operation takes an non-empty argument stack and yields an element result. The consistency relations: 7 an empty_S stack is_empty, and a stack with at least one element is not; 8 unstacking an argument stack, stack(e,s), results in the stack s; and 9 inquiring as to the top of a non-empty argument stack, stack(e,s), yields e. 24 The Inescapable Meaning Assignment Example, Formalisation

The meaning of designations: type 1. E, S value 2. empty_S: Unit \rightarrow S 3. is_empty_S: $S \rightarrow Bool$ $\text{4. stack: } \mathsf{E} \, \times \, \mathsf{S} \to \mathsf{S}$ 5. unstack: $S \xrightarrow{\sim} S$ 6. top: $S \xrightarrow{\sim} E$ The consistency relations: 7. $is_empty(empty_S()) = true$ 7. $is_empty(stack(e,s)) = false$ 8. unstack(stack(e,s)) = s

9. top(stack(e,s)) = e

3.1 **Logical Connectives**

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3.1.1 Negation: ¬

The logical connective, **negation** (\neg) , is defined as follows: if assertion \mathscr{P} holds then assertion $\neg \mathscr{P}$ does not hold - the contradiction principle understood as a definition of the concept of negation.

3.1.2 Conjunction and Disjunction: \land and \lor

Assertion $\mathscr{P} \wedge \mathscr{Q}$ holds, i.e., is true, if both \mathscr{P} and \mathscr{Q} holds. Assertion $\mathscr{P} \lor \mathscr{Q}$ holds, i.e., is true, if either \mathscr{P} or \mathscr{Q} or both \mathscr{P} and \mathscr{Q} holds.

3.1.3 Implication: \Rightarrow

Assertion $\mathscr{P} \Rightarrow \mathscr{Q}$ holds, i.e., is true, if the first assertion, \mathscr{P} , holds, *tt*, and the second assertion, \mathscr{Q} , is not false, $\neg ff.[(\mathscr{P},\mathscr{Q}),\mathscr{P}\Rightarrow\mathscr{Q}]$: [(tt,tt),tt], [(tt,ff),ff], [(ff,tt),ff], and [(ff,ff),tt].

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3.2 Transcendence

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DEF.7: By transcendental "we shall understand the philosophical notion: the a priori or intuitive basis of knowledge, independent of experience" **DEF.8:** By a transcendental deduction "we shall understand the philosophical notion: a transcendental 'conversion' of one kind of knowledge into a seemingly different kind of knowledge" **We** shall take what can be expressed in logical propositions and predicates as "one kind of knowledge". A keyword, in the above definition, is "seemingly". We refer to Sects. 3.3.6-3.3.8.

3.3 Towards a Philosophy Basis for Physics and Biology 30

In a somewhat long series of deductions we shall, based on Sørlander's Philosophy motivate the laws of Newton and more, not on the basis of empirical observations, but on the basis of transcendental deductions based on rational reasoning.

3.3.1 Possibility and Necessity

Based on logical implication we can transcendentally define the two *modal operators:* **possibility** and **necessity**. DEF.9: An assertion is **necessarily** true if its truth follows from follows from the definition of the designations by means of which it is expressed **DEF.10**: An assertion is **possibly** true if its negation is not necessary **DEF.10**:

3.3.2 **Empirical Assertions**

There can be assertions whose truth value does not only depend on the definition of the designations by means of which they are expressed. Those are assertions whose truth value does not follow only from the definition of designations but depend also on the assertions *referring* to something that exists independently of the designations by means of which they are expressed. We shall call such assertions *empirical*.

3.3.3 Existence

With Sørlander we shall now argue that there exist many entities in any world: [31, pp 145] "Entities, in a first step of reasoning, that can be referred to in empirical assertions do not necessarily exist. It is, however, an empirical fact that they do exist; hence there is a logical necessity that they do not exist. In a second step of reasoning, these entities must exist as a necessary condition for their actually being ascribed the predicates which they must necessarily befit in their capacity of of being entities referred to in empirical assertions."

3.3.4 Identity, Difference and Relations

[31, pp 146] "An entity, referred to by A, is identical to an entity, referred to by B, if A cannot be ascribed a predicate, in-commensurable with a predicate ascribed to B." That is, if A and B cannot be ascribed in-commensurable predicates. [31, pp 146] "Entities A and B are different if they can be ascribed in-commensurable predicates." [31, pp 147] "Identity and difference are thus transcendentally derived through these formal definitions and must therefore be presupposed in any description of any domain and must be expressible in any language." Identity and difference are relations. [31, pp 147] "As a consequence identity and difference imply relations. … Symmetry and asymmetry are also relations: A identical to B is the same as B identical to A. And A different from B is the same as B different from A. Finally transitivity follows from A identical to B and B identical to C implies A identical to C."

3.3.5 Sets, Quantifiers and Numbers

We can, as a consequence of two or more different entities satisfying a same predicate, say P, define the notion of the **set** of all those entities satisfying P. And, we can, as a consequence of two or more

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entities, $e_i, ..., e_j$, all being *distinct*, therefore implying in-commensurable predicates, $Q_i, ..., Q_j$, but still satisfying a common predicate, P, claim that they all belong to a same set. The predicate P can be said to **type** that set. And so forth: following this line of reasoning we can introduce notions of cardinality of sets, finite and infinite sets, existential (\exists) and universal (\forall) quantifiers, etc.; and we can in this way transcendentally deduce the concept of (positive) numbers, their addition and multiplication; and that such are an indispensable aspect of any domain. We leave it then to mathematics to further study number theory.

3.3.6 Space and Geometry

DEF.11: Space: [31, pp 154] "The two relations asymmetric and symmetric, by a transcendental deduction, can be given an interpretation: the relation (spatial) direction is asymmetric; and the relation (spatial) distance is symmetric. Direction and distance can be understood as spatial relations. From these relations are derived the relation in-between. Hence we must conclude that primary entities exist in space. Space is therefore an unavoidable characteristic of any possible world" [31, pp 155] "Entities, to which reference 43 can be made in simple, empirical assertions, must exist in space; they must be spatial, i.e., have a certain extension in all directions; they must therefore "fill up some space", have surface and form." From this, 44 by further reasoning one can develop notions of points, line, surface, etc., i.e., Euclidean as well as non-Euclidean geometry.

3.3.7 States

We introduce a notion of **state**. [31, pp 158–159] "*Entities may be ascribed predicates which it is not logically necessary that they are ascribed. How can that be possible ? Only if we accept that entities may be ascribed predicates which are in-commensurable with predicates that they are actually ascribed." That is possible, 46 we must conclude, if entities can exist in distinct states. We shall let this notion of state further undefined – till Sect. 6.3.4.*

3.3.8 Time and Causality

DEF.12: Time: [31, pp 159] "Two different states must necessarily be ascribed different incompatible predicates. But how can we ensure so ? Only if states stand in an asymmetric relation to one another. This state relation is also transitive. So that is an indispensable property of any world. By a transcendental deduction we say that primary entities exist in time. So every possible world must exist in time"

So space and time are not phenomena, i.e., are not entities. They are, by transcendental reasoning, aspects of any possible world, hence, of any description of any domain.

In a concentrated series [31, 160-163], of logical reasoning and transcendental deductions, Sørlander, introduce the concepts of the empirical circumstances under which entities exist, implying *non-logical implication* between one-and-the-same entity at distinct times, leading to the notions of **causal effect** and **causal implication** – all deduced transcendentally. Whereas Kant's *causal implication* is transcendentally deduced as necessary for the *possibility of self-awareness*. Sørlander's *causal implication* does not assume *possibility of self-awareness*. The **principle of causality** is a necessary condition for assertions being about the same entity at different times.

3.3.9 Kinematics

[31, pp 164] "Entities are in both space and time; therefore it must be assumed that they can change their spatial properties; that is, are subject to **movement**. An entity which changes location is said to **move**. An entity which does not change location is said to be **at rest**." In this way [31] transcendentally introduces the notions of velocity and acceleration, hence kinematics.

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3.3.10 Dynamics: Newton's Laws

[31, pp 166] "When combining the causality principle with dynamics we deduce that when an entity changes its state of movement then there must be a cause, and we call that cause a **force**." [31, pp 166] "The **change** of state of entity movement must be **proportional** to the applied force; an entity not subject to an external force will remain in its state of movement: This is **Newton's 1st Law**." [31, pp 166] "But to change an entity's state of movement by some force must imply that the entity exerts a certain **resistance** to that change; the entity must have a **mass**. Changes in an entity's state of movement besides being proportional to the external force, must be **inverse proportional** to its mass. This is **Newton's 2nd Law**." [31, pp 166-167] "The forces that act upon entities must have as source other entities: entities may **collide**; and when they collide **the forces** they exert on each other must be **the same but with opposite directions**. This is **Newton's 3rd Law**." [31, pp 167-168] "How can entities be the source of forces? How can they have a mass? Transcendentally it must follow from **gravitational pull**. Across all entities of mass, there is a mutual attraction, **universal gravitation**." [31, pp 168-169] "Gravitation must, since it has its origin in the individual entities, propagate with a definite velocity; and that velocity must have a limit, a constant of nature, the **universal speed limit**."

3.3.11 From Philosophy to Physics

Based on logical reasoning and transcendental deductions one can thus derive major aspects of that which be (assumed to be) in any description of any world, i.e., domain. In our domain description ontology we shall let the notions of **natural parts** and **continuous endurants** (non-solids) cover what we have covered so far: they are those entities which satisfy the laws of physics, hence are in space and time. In the next sections we shall make further use of Sørlander's Philosophy to logically and transcendentally justify the inevitability of **living species: plants** and **animals** including, notably, **humans**, in any description of any domain.

3.3.12 Purpose, Life and Evolution

[31, pp 174] "For language and meaning to be possible there must exist entities that are not constrained to just the laws of physics. This is possible if such entities are further subject to a "purpose-causality" directed at the future. These entities must strive to maintain their own existence." We shall call such entities living species. Living species must maintain and also further develop their form and do so by an exchange of materials with the surroundings, i.e., metabolism, with one kind of living species subject only to development, form and metabolism, while another kind additionally move purposefully, The first we call plants, the second animals. Animals, consistent with the principle of causality, must possess sensory organs, a motion apparatus, and instincts, feelings, promptings so that what has been sensed, may be responded to [through motion]. The purpose-directness of animals must be built into the animals. Biology shows that that is the case. The animal genomes appear to serve the purpose-directness of animals. [31, pp 178] "Biology shows that it is so; transcendental deduction that it must be so."

3.3.13 Awareness, Learning and Language

[31, pp 180]"

Animals, to learn from experience, must be able to feel inclination and disinclination, and must be able to remember that it has acted in some way leading to either the feeling of inclination or disinclination. As a consequence, an animal, if when acting in response to sense impression, 1, experiences the positive feeling of inclination (desire), then it will respond likewise when again receiving sense impression 1, until it is no longer so inclined. If, in contrast, the animal feels the negative feeling of disinclination (dislike), upon sense impression 1, then it will avoid responding in this manner when receiving sense impression 1." [31, pp 181] "Awareness is built up from the sense impressions and feelings on the basis of, i.e., from what the individual animal has learned. Different animals can be expected to have different levels of

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consciousness; and different levels of consciousness assume different biological bases for learning. This 67 is possible, biology tells us, because of there being a central nervous system with building blocks, the neurons, having an inner determination for learning and consciousness." [31, pp 181–182] "In the mutual 68 interaction between animals of a higher order of consciousness these animals learn to use signs developing increasingly complex sign systems, eventually "arriving" at languages." It is thus we single out humans. 69 [31, pp 183] "Any human language which can describe reality, must assume the full set of concepts that are prerequisites for any world description." 70

INTERLUDE

We have concluded the presentation of a major issue of this paper. that of a philosophy that may be a possible basis for domain science & engineering. We now "apply" this, Kai Sørlander's, Philosophy to the problem of domain analysis & description.

Phenomena and Entities 4

DEF.13: By an entity, is_entity, we shall understand a phenomenon, i.e., something that can be observed, *i.e.*, be seen or touched by humans, or that can be conceived as an abstraction of an entity; alternatively, a phenomenon is an entity, if it exists, it is "being", it is that which makes a "thing" what it is: essence, essential nature [20, Vol. I, pg. 665] An entity is what we can analyse and describe using the analysis 72 & description prompts outlined in this paper. Many of the entities that we are concerned with are those with which Kai Sørlanders Philosophy is likewise concerned. They are the ones that are unavoidable in any description of any possible world.

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Before main Sects. 5–9, we introduce two categories of entities: endurants and perdurants.

4.1 **Endurants**

DEF.14: By an endurant we shall understand an entity that can be observed, or conceived and described, as a "complete thing" at no matter which given snapshot of time; alternatively an entity is endurant if it is capable of enduring, that is persist, hold out [20, Vol. I, pg. 656]. Were we to "freeze" time we would still be able to observe the entire endurant Endurants, thus, are capable of enduring. Ex.1. Endurants: A train wagon, a rail track and a railway station We suggest that the concept of endurants can be seen as a transcendental deduction based on the inescapable fact that there is a multitude of entities, cf. Sect. 3.3.5, and that considering these as existing in just space, are the endurants. But note that endurants are [to be] observed.

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4.2 Perdurants

DEF.15: By a perdurant we shall understand an entity for which only a fragment exists if we look at or touch them at any given snapshot in time. Were we to freeze time we would only see or touch a fragment of the perdurant, alternatively an entity is perdurant if it endures continuously, over time, persists, lasting [20, Vol. II, pg. 1552] Perdurants are entities that only exists partially at any given point in time. Ex.2. Perdurant: 78 a train ride We suggest that the concept of perdurants can be seen as a transcendental deduction based 79 on the inescapable fact that there are a multitude of entities, cf. Sect. 3.3.5, and that considering these as existing in both space and time, are the perdurants. 80

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Sections 5–7 and Sect. 9 reviews the complex, conceptual "universes" of endurants, respectively perdurants. Section 8 unveils, by a transcendental deduction, the link between endurants and perdurants: that endurant parts transcend into behaviours. Figure 1 suggests a structuring of endurants, perdurants and their relations.

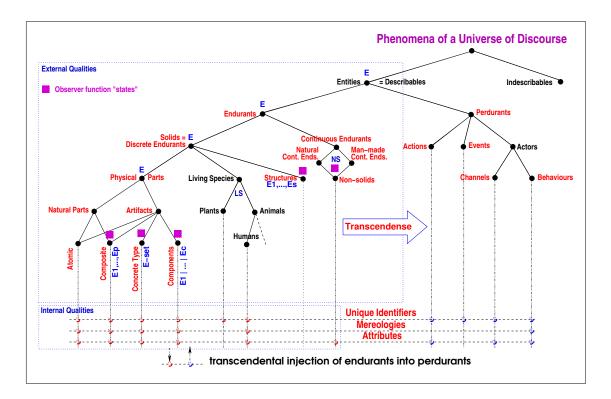


Figure 1: An Upper Ontology for Domain Entities. We shall not discuss black labeled entity classes. The magenta coloured square boxes, , designate "analysis states: where respective description prompts apply.

5 Endurants: Analysis of External Qualities

Observable qualities of endurants are those that can be touched. Endurants are either discrete or continuous, that is, solid, respectively non-solid. We choose, it may seem arbitrarily, to analyse endurants into either **discrete** (solid) or **continuous** (non-solid) endurants. That is, we claim that endurants can be so analysed either of one kind, or of the other, but not both ! We justify the distinctions based on physics.

5.1 Discrete and Continuous Endurants

DEF.16: By a **discrete endurant** (a solid) we shall understand an endurant which is **separate**, **individual** or **distinct** in form or concept [20, OED] **EX.3**. **Discrete Endurants**: a canal lock, a canal link between two adjacent locks, a barge **DEF.17**: By a **continuous endurant** (a non-solid) we shall understand an endurant which is **prolonged**, without **interruption**, in an **unbroken series** or **pattern** [20, OED] **W** think of a non-solid to be either a gas or a plasma or a liquid. **Ex.4**. **Continuous Endurant**: water **Note**, and please accept, the OED definitions. They are not precise in the sense of mathematics. We are not dealing with an exact 'world'. We are dealing with real worlds.

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5.2 Solids

Solids, i.e., discrete endurants, are either physical parts, or living species, or structures. We shall motivate the first two categories of solids on the background of Sølander's philosophy. Structures are motivated pragmatically.

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5.2.1 Physical Parts and Living Species

DEF.18: By a physical part we shall understand a discrete endurant existing in time and subject to laws of physics, including the causality principle and gravitational pull – which are not living species or animals ■
Ex.5. Physical parts: A pipeline system, a pipeline, pipeline units: pipes, valves, pumps, etc. ■
DEF.19: 89
By a living species we shall understand a discrete endurant, subject to laws of physics, and additionally
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subject to causality of purpose ■
Ex.6. Living Species: a garden, a flower bed, a rhodendenron ■
In this
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paper we shall not elaborate on the possibility of natural versus man-made living species.

5.2.2 Natural Parts and Artefacts

DEF.20: By a **natural part** we shall understand physical parts, i.e., that are in space and time, are subject to the laws of physics, and also subject to the principle of causality and gravitational pull, but are not man made and not living species **EX.7.** Natural Parts: a landscape, a lake, a forest, a mountain **93** DEF.21: By an **artefact** we shall understand physical parts that are man made with one or more intents **94** We shall explain the notion of *intent* later. **EX.8.** Artefacts: a road network, with automobiles, hubs (a **95** road intersections), links (between two adjacent hubs), routes (contiguous sequences of zero, one or more adjacent, alternating hubs and links). The intents are that automobiles drive along routes and that hubs and links serve as conduits for automobiles **1**

5.2.3 Atomic or Composite Parts

DEF.22: By an **atomic part** we shall understand a part which, in a given context, deemed to **not** contain of meaningful, separately observable proper sub-part. A sub-part is a part **a** Ex.9. **Atomic Artefacts:** hubs, 97 links, automobiles **b** We shall not consider natural parts as other than that, neither atomic, nor composite 98 in this paper. DEF.23: By a **composite part** we shall mean physical parts which, in a given context, are 99 deemed to indeed consist of meaningful, separately observable proper sub-parts **b** Ex.10. **Composite** 100 **Artefacts:** a road net, a pipeline system, a railway system **b** Ex.11. **Elements of a Composite** 101 **Artefact:** The domain of road transport is assumed to contain a road net which then contains a set of links, a set of hubs, a set of automobiles, a set of zero, one or more road maintenance departments, and a set of zero, one or more automobile clubs. I may contain other parts

5.2.4 Varieties of Artefacts

In addition to **atomic** and **composite** artefacts there are **concrete type** artefacts and **component** artefacts. The analysis into this variety of four kinds is based on pragmatic grounds. DEF.24: By a **concrete type artefact** we shall, simplifying, mean a set of endurants, all of the same sort **E**X.12. **Concrete 103 Type Artefacts:** *a set of hubs, a set of links, a set of automobiles* **DEF.25**: By a **component type 104 artefact** we shall understand a set of zero, one or more discrete endurants of the same kind which we, the domain analyser cum describer choose to not endow with mereology **E**X.13. **Components:** *letters* (of a mail box), *sand grains* (of a heap), *bricks* (of a stack)

5.2.5 Plants, Animals and Humans

Living species are either plants or animals. **DEF.26**: By a **plant**, **animal** and **human** we shall understand what Kari Sørlander's Philosophy transcendentally arrives at as such **u** We omit examples !

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5.2.6 Structures

DEF.27: By a **structure** we shall understand a discrete endurant which the domain engineer chooses to describe as consisting of one or more endurants, whether discrete or continuous, but to not endow with internal qualities: unique identifiers, mereology or attributes **•** Structures are "conceptual endurants". A structure "gathers" one or more endurants under "one umbrella", often simplifying a presentation of some elements of a domain description. Sometimes, in our domain modelling, we choose to model an endurant as a structure, sometimes as a physical part; it all depends on what we wish to focus on in our domain model. As such structures are "compounds" where we are interested only in the (external and internal) qualities of the elements of the compound, but not in the qualities of the structure itself.

5.3 Non-solids

We remind you of Sect. 5. En entity may thus be a non-solid. A composite part, p, natural or manmade, may have one or more non-solid entities, though with at least one solid entity — in which case has_non_solids(p).

5.4 The Analysis Prompts

We summarise the analysis prompts informally introduced in this section.

- is_entity,
- is_discrete,
- is_continuous,
- is_physical,
- is_living,is_structure,
- is natural.
- is artefact.
 - 15<u>-</u>41 001400,
- Endurants: Analysis of Internal Qualities

Internal qualities of endurants are those qualities that cannot be touched but can be either conceptualised or measured. We consider the following internal qualities: **unique identifiers**, **mereology**, and **attributes**. Physical parts have the full set of internal qualities. Structures are endurants for which the domain analyser cum describer had decided to not endow with internal qualities. We shall not, in this paper, be concerned

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6.1 Unique Identifiers

with the internal qualities of living species.

It is based on the philosophy idea of *identity*, cf. Sect. 3.3.4, that we associate with each solid a unique identifier. $\mathbb{E}x.14$. Road Net Links and Hubs: The road net of a transport system consists of links, i.e., street segments, and hubs, i.e., street intersections. Links of a road not have unique identifiers. (Links of all road nets are distinctly identified.) Hubs of any road net are distinctly identified.

6.2 Mereology

DEF.28: Mereology is the study of parts and the wholes they form **•** Mereology, as here put forward, is due to the Polish philosopher/logician/mathematician Stanisław Leśhniewski [21, 15]. There are basically two relations that can be relevant for part-hood (i) a topological one, and (ii) a conceptual one. (i) Physically two or more parts may be adjacent to one another or one within within another. (ii) Conceptually some parts, "relate" to a "therefrom physically distinct" part. **E**x.15. **Topological Mereology**: The mereology of links of a road net is a set of two distinct hub identifiers of that net, and of hubs of a road net is a set of zero, one or more link identifiers of that net. The mereology thus defines a concept of routes of a road net, and must be such that there is at least one route from any hub to any other hub of a road net **• E**x.16.

• is_atomic.

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• is_composite,

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- is_concrete,
- is_component,

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has_non_solids,

• has_components.

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Conceptual Mereology: The mereology of an automobile (of a road transport system) identifies the hubs and links that it may traverse and the zero, one or more automobile clubs it may be a member of. The mereology of a hub and a link, (of a road transport system) in addition to what has already been ascribed to hubs and links, identifies one road maintenance department

We may model the mereology of a part, p, as a triplet: an input set of unique identifiers of parts from which p "receives input" in a sense not further described here; a pair of input/output sets of unique identifiers of parts from which p "receives input" and "delivers output" in a sense not further described here; and an output set of unique identifiers of parts to which p "delivers output" in a sense not further described here.

6.3 **Attributes**

Unique identifications and mereologies form abstract concepts. Although topological mereologies may be observed they, and unique identification, are not manifest – although they can be the quantities that are referred to in empirical assertions. Attributes are measurable properties of endurants, properties that can be referred to in empirical assertions — they, so-to-speak, gives "flesh and blood", that is, substance to endurants. Endurants are typically recognised because of their spatial form and are otherwise characterised 120 by their intangible, but measurable attributes. We equate all endurants which, besides possible type of unique identifiers and possible type of mereologies, have the same types of attributes, with one sort. Removing a quality from an endurant makes no sense: the endurant of that type either becomes an endurant of another type or ceases to exist (i.e., becomes a non-entity) !

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6.3.1 Attribute Categories

Attributes [19] are either of static value, i.e., does change value, or of monitorable value, i.e., inert or reactive: monitorable values can change, or of controllable value, i.e., biddable or programmed: biddable values can be prescribed, but prescription may fail, programmable values can be set. Ex.17. Link 122 Attributes: Typical link attributes could be: location (e.g., as a Bézier curve) [static], length [static], road condition (icy, dry, ...) [monitored], state - as a set of pairs of adjacent hub identifiers [controllable], state spaces – as set of all such states [static], and automobile history: recordings of which automobiles have been on the link, at which position and time **EX.18.** Hub Attributes: Typical hub attributes could be: 123 location [static], state – as set of pairs of adjacent link identifiers [controllable], and automobile history: recordings of which automobiles have been on the hub, and at which time. States are abstractions of traffic signals EX.19. Automobile Attributes: Typical automobile attributes could be: position (on hub or 124 link), velocity, etc., road net history: recordings of the hubs and links on which the automobile has been, at which position and time

6.3.2 Artefact Intents

With artefacts we can associate **intents**. DEF.29:By an **intent** of an artefact we shall understand a simple label which informally indicates the purpose for which the artefact is intended An artefact may be ascribed more than one intent. Artefacts are usually ascribed at least one intent. Ex.20. Intents of Automobiles and Road Nets: To automobile we may ascribe the intent that they are located on the road net, i.e., on hubs and links; and to hubs and links we then ascribe the intent that they accommodate automobiles

6.3.3 Intentional Pull

Gravitational pull, cf. Sect. 3.3.10, follows from Newton's Third Law. Intentional pull "follows" from the fact that pairs or triples, etc., of artefacts of different sorts may be ascribed commensurate intents. Ex.21. 128 Intentional Pull between Automobiles and Road Net: If an automobile's road net history records

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that is has visited a road net unit at time t and position π , then that road net unit's automobile history records that very same fact! And vice versa. It cannot be otherwise!

6.3.4 States

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By a state we shall understand any collection of endurants for which any one endurant has at least one dynamic, i.e., non-static, attribute. By the state of a behaviour we shall understand its current *program point*, that is, its point of execution, and the collection of its monitorable and controllable variables, that is, of their current values.

7 Endurants: Description Prompts

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So far we have outlined a number of domain analysis prompts, cf. Sect. 5.4. We now summarise some description prompts. We refer to Fig. 1. The "analysis states" marked with magenta colored square boxes, • , correspond, left-to-right in the ontology graph to the following description prompts: observe_endurant_sorts, observe_concrete_part, observe_component_sort, observe_structure_components and observe_non_solids.

_ type: observe_endurant_sorts: E→Text _

Narrative:

s. narrative: s. narrative text on sorts $E_1,...,E_n$ o. narrative text on observers $obs_E_1,...,obs_E_n$ p. narrative text on proof obligation: \mathscr{P} Formalisation: s. type $E_1,...,E_n$ o. value $obs_E_1: E \rightarrow E_1,...,obs_E_n: E \rightarrow E_n$ p. proof obligation $\mathscr{P}: \forall i:\{1..n\}$ •is $_E_i(e) \equiv \land \{\sim E_j(e)|j:[1..n] \setminus \{i\}|j:[1..n]\}$

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A similar observer is defined for concrete type parts, cf. Sect. 5.2.4:

______ type: observe_concrete_part: E→Text _

Narratives: s. narrative text on sort P o. narrative text on observer obs_Ps Formalisation: s. type P, Ps = P-set o. value obs_Ps: E→P-set

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We refer to [12] for observers of components, structures and non-solids. The above covered the prompts for describing external qualities. Prompts for describing internal qualities are: **observe_unique_identifier**, **observe_mereology** and **observe_attributes**.

type observe_unique_identifier: $P \rightarrow Text$

Narratives:
i. text on unique identifier: UI
o. text on unique identifier observer: uid_E
Formalisation:
i. type UI
o. value uid_E: E → UI

```
_ type observe_mereology: P→Text ____
```

Narratives: m. text on mereology: M o. text on mereology observer: mereo_E Formalisation: m. type $M = \mathscr{E}(UI_a, ..., UI_c)$ o. value mereo_E: $E \rightarrow M$

_ type observe_attributes: P→Text _

Next we informally describe an ("interactive") analysis and description process. It postulates endurant values, V, as either (physical) part values, or component values, or non-solid values. The *process* evolves around: uod:UoD, an endurant, a universe of discourse, value. new, a variable holding a set of endurant values; gen a variable also holding a set of endurant values; and txt, a variable holding (a set) of narrative and formal texts, those generated generated, as illustrated, by observer functions. The analysis function **observe_endurant_values(v)** yields sets of endurant values.

```
_____ A Domain Analysis & Description Process, Part I/II ___
```

```
type
    V = Part_VAL | Komp_VAL | Non_Sol_VAL
variable
    new:V-set := {uod:UoD},
    gen:V-set := \{\},
    txt:Text := \{\}
value
    discover_sorts: Unit \rightarrow Unit
    discover_sorts() \equiv
         while new \neq {} do
             let v{:}V \mathrel{\scriptstyle\bullet} v \in \mathsf{new} in
              (new := new \setminus \{v\} \parallel gen := gen \cup \{v\});
             is_part(v) \rightarrow
                  (is_atomic(v) \rightarrow skip ,
                   is_composite(v) \rightarrow
                       (new := new ∪ observe_endurant_values(v) ∥
                        txt := txt \cup observe_endurant_sorts(v)),
                   has_concrete_type(v) \rightarrow
                       (new := new \cup \{\iota \text{ observe_endurant_values}(v)\} \parallel
                        txt := txt \cup observe\_concrete\_part(v))),
             has_components(v) \rightarrow
                   (new := new \cup \parallel
                   txt := txt \cup observe\_component\_sorts(v)),
             has_non_solids(v) \rightarrow
                   txt := txt \cup observe\_non\_solid\_sorts(v),
             is_structure(v) \rightarrow
                   ... EXERCISE FOR THE READER !
                                                         ...
     end end
```

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 ι s selects an element of the set s. If s is empty { ι s} is empty.

A Domain Analysis & Description Process, Part II/II

```
discover_uids: Unit \rightarrow Unit
discover_uids() \equiv
        for \forall v:(PVAL|KVAL) \bullet v \in gen
              do txt := txt \cup observe_unique_identifier(v) end
discover_mereologies: Unit \rightarrow Unit
discover_mereologies() \equiv
        for \forall \ v: \mathsf{PVAL} \ {\boldsymbol{\bullet}} \ v \in \mathsf{gen}
              do txt := txt \cup observe\_mereology(v) end
discover_attributes: Unit \rightarrow Unit
discover_attributes() \equiv
        for \forall v:(PVAL|MVAL) \bullet v \in gen
              do txt := txt \cup observe_attributes(v) end
analysis+description: Unit \rightarrow Unit
analysis+description() \equiv
        discover_sorts();
                                       discover_uids();
        discover_mereologies(); discover_attributes()
```

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8 From Parts to Behaviours

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It is often said "every noun can be verbed" and "every verb can be nouned". That may be so. In any case we shall perform the following one-way transcendental deduction: "to every [endurant] physical part" "we shall associated a perdurant behaviour". That deduction is "inspired" by the following observations: (i) there is the train, as an endurant entity, as as it stands, there, on the platform, statically observable, over time; (ii) there is the train, as a perdurant behaviour, as it "speeds" down the railway track, only a part of it visible at any given point and time; and (iii) there is the train, as a railway system attribute, as it "appears" in a time table; programmable.

By an **action** we shall understand a function which, among its arguments, take a state and delivers an updated state, and where that action has been knowingly, willfully applied. By an **event** we shall understand a state change for which we do not seek its origin, i.e., who or what caused that state change. By a **behaviour** we shall understand a sequence of one or more actions, events and behaviours.

In Sect. 9 we shall formally summarise, cf. [12], that deduction. Since physical parts coexist — their translated behaviours operate concurrently. Since physical parts relate — these behaviours communicate. For that reason we shall express the part behaviours in terms of Hoare's CSP [17, 18, 22, 23]. Hence we shall express communication via channels.

9 Perdurants

To simplify matters we shall just deal with artefacts. These are described in terms of their sorts, whether atomic, composite or concrete (like 'sets of'), and unique identifiers, mereology and attributes. Transcendentally deduced artefact behaviours are described in terms of their signatures and definition bodies. We shall now show how to relate all of the endurant descriptions with their perdurant counterpart; that is, how the transcendental deduction works ! Each have a crucial rôle !

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9.1 Behaviour Signatures

A behaviour signature, for part *p*, is of the form:

value

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Name: ui:UI \rightarrow (st₁,...st_s):Statics \rightarrow me:Mereology \rightarrow [me = (ichs,iochs,ochs)] (ca₁,...,ca_c):Programmables \rightarrow in Monitorables, in_Mereology, in,out in_out_Mereology, out out_Mereology \rightarrow Unit

We explain this signature: Name is an analyser cum describer chosen name, usually a meaningful mnemonic; UI is the type of the unique identifier for the translated sort, i.e., of part p; Statics designates the zero (s=0), one or more static attributes of part p; Mereology designates the triplet mereology of the part, cf. last paragraph of Sect. 6.2; Programmables designates the zero (c=0), one or more programmable attributes of part p; Monitorable designates zero, one or more input channel references designating monitoriable attributes of part p; in_Mereology designates zero, one or more input channel references designating the parts from whom part p "receives" input; in_out_Mereology designates zero, one or more input down it "delivers" output; out_Mereology designates zero, one or more output channel references designating the parts to whom part p "delivers" output; and Unit designates that the behaviour goes on forever ! Technicalities are given in [12], Sects. 7.4.3–7.4.4.

9.2 Behaviour Definition Bodies: \mathscr{B}_P

In general the signature expresses that behaviour Name(uid) evolves around (i) constant values whose type is given in Statics; (ii) input from monitorable attributes (of values "residing" in part p, but not otherwise expressible) are expressed in the body of the behaviour definition by the CSP input expression attr_A? where A is a monitorable attribute of p; (iii) input from topologically related parts, q, are expressed by ch[ui_p,ui_q]?; and (iv) output of values v to topologically related parts, q, are expressed by ch[ui_p,ui_q]!v. (v) In other words, the channel designations of the signature are of the form: attr_A_i, ..., attr_A_j and ch[ui_p,ui_q]. Further technicalities are given in [12], Sect. 7.4.5.

9.3 From Part Descriptions to Behaviour Definitions

```
Composite parts: type Translate<sub>P</sub>: P \rightarrow RSL^+Text
```

```
value
    Translate<sub>P</sub>: P \rightarrow RSL^+Text
    Translate<sub>P</sub>(p) \equiv
         let ui = uid_P(p),
                                              me = mereo_P(p),
                                                                              Sects. 6.1,6.2
              sa = stat_attr_vals(p), ca = ctrl_attr_vals(p),
                                                                                  Sect 6.3.1
               MT = mereo_typs(p), ST = stat_attr_typs(p),
               CT = ctrl_attr_typs(p), IOR = calc_i_o_chn_refs(p),
               IOD = calc_all_ch_dcls(p) in
          value
                    \mathcal{M}_{P}: \mathsf{P}_{U} \mathsf{U} \to \mathsf{ST} \to \mathsf{MT} \to \mathsf{CT} \to \mathsf{IOR} Unit
                   \mathcal{M}_{P}(ui)(sa)(me)(ca) \equiv \mathcal{B}_{P}(ui)(sa)(me)(ca)
                     \Rightarrow Translate<sub>P1</sub> (obs_endurant_sorts_E<sub>1</sub>(p))
                    Translate<sub>P2</sub>(obs_endurant_sorts_E<sub>2</sub>(p))
                   ≪≫ ...
                    \Rightarrow Translate<sub>P<sub>n</sub></sub>(obs_endurant_sorts_E<sub>n</sub>(p))
          end
```

The above schema specifies the translation of composite parts into RSL^+ **Text**, where RSL is the RAISE Specification Language, [16]. The $\ll ... \gg$ designate the texts, ..., as written.

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Concrete parts: type Translate_P: $P \rightarrow RSL^+$ Text .

Atomic parts: type Translate_P: $P \rightarrow RSL^+$ Text

```
value

Translate<sub>P</sub>(p) =

let ui = uid_P(p), me = mereo_P(p),

sa = stat_attr_vals(p), ca = ctrl_attr_vals(p),

ST = stat_attr_typs(p), CT = ctrl_attr_typs(p),

IOR = calc_i_o_chn_refs(p), IOD = calc_all_chs(p) in

& channel IOD

value

\mathcal{M}_P: P_UI×MT×ST PT IOR Unit

\mathcal{M}_P(ui)(sa)(me)(ca) = \mathcal{B}_P(ui)(sa)(me)(ca) \Rightarrow

end
```

 $\mathscr{B}_P(ui)(sa)(me)(ca)$ designate the "body" of the definition of behaviour $\mathscr{B}_P(ui)$. For details we refer to the **Core Behaviour Schema** of [12, Sect. 7.5].

9.4 Channel Declarations

Here we shall just mention that the above **Translate** schemas refer to **channel**s. The channel declaration, in RSL, are of the form

• **channel** ch[{ui_p,ui_q}]: CH_MSG

where CH_MSG is a type expression for the values communicated over CSP channels. That is, the channel array indexes are two element sets of unique identifiers of relevant distinct parts as implied by their respective mereologies.

9.5 Concrete System

An instantiation of any given *universe of discourse, uod,* thus amounts to the parallel, \parallel , composition of behaviours, potentially one for each composite and each atomic part. [12, Sect. 7.6] illustrates an example.

10 Conclusion

In [9, Sect. 3.1.5] we elaborate extensively on the analysis & description process, while giving in [9, Sect. 5.3] an extensive review of related work. In [12, Sect. 9, *Closing*] we discuss, extensively, the wider

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ramifications of the domain science and engineering approach of the present paper.

10.1 What Have We Achieved?

We have summarised an essence of Kai Sørlander's Philosophy [31]: recounted how, from a basis of the inescapable meaning theory, the concepts of space, time and Newton's Laws can be transcendentally deduced, and from these the concepts of living species: plants and animals. And we have summarised the 161 essence of [12]: an ontology of endurants and perdurants, discrete and continuous (non-solid) endurants, physical parts, living species and structures, natural parts and artefacts; and their internal qualities: unique identifiers, mereology and attributes. Finally we have shown, by a transcendental deduction, how discrete 162 endurants can be "morphed" into perdurants, i.e., [in this paper] CSP behaviours whose signature can be derived from internal qualities of appropriate discrete endurants: unique identifiers, mereology and attributes. Throughout we have related the two areas: philosophy and computing. 163

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The Philosophy aspect of this paper is new. That is, it is, to our knowledge, the first time a serious attempt has been made to strongly relate an area of the science of computing to philosophy. The domain science & engineering of [12] is also new. For the first time we see a straight line from the domain of artefact problems to their solution by computing [1, 2, 5, 6, 7, 11]. We find that remarkable.

If you have a need for examples, please consult [12] and [13, twelve domain case studies].

10.2 **Open Problems**

We shall only focus on issues that relate to Sects. 4–9. Further studies seem necessary in order to secure the inevitability of the distinction between discreteness and continuity, justify the presence of structures, and the distinction between atomic and composite parts. The transcendental deduction of endurants into perdurants may not exactly satisfy Kai Sørlander's strict criteria for such deductions.

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Acknowledgment 10.3

I am grateful to Kai Sørlander for his patience and help in properly understanding his philosophy and for creating that philosophy [24, 25, 26, 27, 28, 29, 30, 31]: truly a remarkable feat — as also observed by Georg Henrik von Wright, Wittgenstein's successor at Cambridge, England, at age 32 [en.wikipedia.org/wiki/Georg_Henrik_von_Wright] [24].

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