# Towards a Formal Understanding of Urban Planning Some Initial Thoughts

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#### Abstract

<sup>1</sup> We examine concepts of urban planning. Emphasis, in this research note, is on the *information* ("data") and *functions* (*behaviours*) of urban planning. We abstract from the details of information (the "data") that urban planning is based on and results in. We distinguish between two kinds of urban planning behaviour: the *master*, 'ab initio', behaviour of determining "the general layout of the land (!)", and the *derived*, 'follow-up', behaviours focused on social and technological infrastructures. Master urban planning applies to descriptions of "the land": geographic, that is, geodetic, cadastral, geotechnical, meteorological, socio-economic and rules & regulations. Examples of derived urban plannings are such which are focused on humans and on social and technological artifacts: *industry zones, commercial (i.e., office and shopping) zones, residential zones, recreational areas, health care, schools, etc.* and *transport, electricity, water, waste, etc.* The overall aim of this paper is to suggest a formal foundation for urban planning. We must emphasize that all that is conceivable and describable in the domain can be described. We shall return to this remark, in this report, again-and-again.

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- Section 1.4 on Page 8 is new, Dec. 25, 2017.
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Wherever new section have been inserted subsequent section numbering has been adjusted.

## Contents

l Introduction			
	1.1	On Urban Planning	
		1.1.1 Infrastructures	
		1.1.2 Wikipedia: https://en.wikipedia.org/wiki/Urban_planning	
		1.1.3 Theories of Urban Planning	
		Technical aspects	
		Urban planners	
		1.1.4 <b>References</b>	
	1.2	A Triptych of Software Development	
	1.3	On Formality	
	1.4	On Describing Domains	
	1.5	Reiterating Domain Modeling	
	1.6	Partial, Precise, and Approximate Descriptions	
	1.7	On Formal Notations	
	1.8	On the Form of This Research Note	

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2	An I	Urban Planning System	10
3	Form	malisation of Urban Space and Planning Endurants	11
	3.1	Some Auxiliary Concepts	11
		3.1.1 Points and Areas	11
		3.1.2 Time and Time Intervals	12
	3.2	Urban Space Endurants	12
		3.2.1 Main Part and Attributes	13
		3.2.2 Urban Space Attributes – Narratives and Formalisation	13
		General Form of Attribute Models	13
		Geodetic Attribute[s]	13
			14
		Geotechnical Attribute[s]	14
		Meteorological Attribute[s]	15
		Socio-Economic Attribute[s]	15
		Law Attribute[s]: State, Province, Region, City and District Ordinances	15
		Industry and Business Economics	16
		Etcetera	16
		The Urban Snace Attributes	16
			16
	22	Urban Diamaing Auviliarias	16
	ງ.ງ ຊ_/		16
	Ј. <del>4</del> 2 г		17
	3.5	Orban Planning Endurants	17
		3.5.1 Urban Plans	17
	26	5.3.2 Urban Planning Anchiaries	17
	3.0	Assumptions About Orban Space and Planning Attributes	17
		3.0.1 Assumptions About Urban Space and Planning Attribute Values	17
		3.0.2 Assumptions About Urban Space and Planning Data	17
Δ	Two	o non-Urban Planning Behaviours	18
-	41	The Urban Space Behaviour	18
	4.2		10
	7.2		15
5	Reg	uirements, Goals and Indicators	20
	5.1	Example Graphics of Urban Plans	20
	5.2	Discussion of Forms & Contents of Urban Plans	24
	5.3	Requirements to Forms & Contents of Urban Plans	24
6	Mas	ster Urban Planning	24
	6.1	Urban Planning Information Categories	24
		6.1.1 "Input"	24
		6.1.2 <b>"Output"</b>	25
	6.2	The Iterative Nature of Urban Planning	25
	6.3	Initialisation	26
		6.3.1 Existing versus Evolving Plans	26
	6.4	A Simple Functional Form	27
	6.5	Oracles and Repositories	27
		6.5.1 The Master 'Input' Oracle	27
		652 The Master Resumption Repository	$\frac{-}{28}$
	6.6	A Simple Behavioural Form	$29^{-5}$
	0.0		-0
7	Deri	ived Urban Plannings	30
	7.1	Preliminaries	30
	-	7.1.1 Derived Urban Plan Indices	30
		7.1.2 A "Reservoir" of Derived Urban Planning Indices	31
		7.1.3 A Derived Urban Planning Index Selector	31
		714 The Derived Urban Plan Generator	31
		715 The Revised Master Urban Planning Behaviour	32
	70	The Derived Urban Planning Functions	32 29
	1.4 7 2	The Derived Urban Planning "Oracle" Rehaviour	-04 22
	7.J	The Derived Urban Planning Babaviour	24 24
	1.4 7 E	The Derived Orbeit Flamming Denaviour	04 94
	1.5		94

	7.6 7.7 7.8	7.5.1 7.5.2 7.5.3 7.5.4 7.5.5 <b>A Visu</b> <b>Revise</b> <b>The U</b>	The Consolidated Derived Resumption Map The Consolidated Derived Resumption Repository Channel The Consolidated Derived Resumption Repository Initial Consolidated Derived Urban Plannings Initialisation of The Derived "Quintuplet" Oracle al Rendition of Urban Planning Development d Selection of Derived Urban Plannings rban Planning System	34 35 35 35 35 37 37
8	Furt	her Wo	rk	37
	8.1	Reaso	ing About Deadlock, Starvation, Live-lock and Liveness	37
	8.2	Docun	nent Handling	37
		8.2.1	Information Categories	37
		0.2.2 8 2 3		38
	8.3	Valida	tion and Verification (V&V)	38
	8.4	Urban	Planning Project Management	38
		8.4.1	Urban Planning Projects	39
		8.4.2	Strategic, Tactical and Operational Management	39
			Project Resources	39
			Strategic Management	40
			Tactical Management	40
		012	Uperational Management	40
		0.4.5		40
9	Con	clusion		40
10	Bibl	iograhy		40
Α	A D	ocumer	t System	42
	A.1	Introd	uction	42
	A.2	A Doc	ument Systems Description	12
				42
	A.3	A Syst	em for Managing, Archiving and Handling Documents	42
	A.3 A.4	A Syst Princip	em for Managing, Archiving and Handling Documents	42 42 42
	A.3 A.4 A.5	A Syst Princip Unique	em for Managing, Archiving and Handling Documents	42 42 42 43 43
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum	em for Managing, Archiving and Handling Documents	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> </ul>
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2	em for Managing, Archiving and Handling Documents	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> <li>44</li> </ul>
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers Document Identifiers Document Descriptors Document Annotations	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> <li>44</li> <li>44</li> </ul>
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4	em for Managing, Archiving and Handling Documents	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> <li>44</li> <li>44</li> <li>44</li> </ul>
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> <li>44</li> <li>44</li> <li>44</li> <li>44</li> </ul>
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 A.6.6	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes	42 42 42 43 43 43 43 44 44 44 44 44
	A.3 A.4 A.5 A.6	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View	42 42 42 43 43 43 44 44 44 44 44 44 44 44
	A.3 A.4 A.5 A.6 A.7 A.8	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View	<ul> <li>42</li> <li>42</li> <li>42</li> <li>43</li> <li>43</li> <li>43</li> <li>44</li> <li>44</li> <li>44</li> <li>44</li> <li>46</li> <li>47</li> <li>48</li> </ul>
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A 10	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View Dormal Graphical System Rendition our Signatures	42 42 43 43 43 43 44 44 44 44 44 44 44 46 47 48 48
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A 11	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures	42 42 42 43 43 43 43 44 44 44 44 44 44 44 46 47 48 48 49
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions	42 42 42 43 43 43 43 43 44 44 44 44 44 44 44 44
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel	42 42 42 43 43 43 43 43 44 44 44 44 44 44 44 44
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behave Chann An Inf Behave Time A.11.1 A.11.2 A.11.3	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct	$\begin{array}{c} 42\\ 42\\ 42\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2 A.11.3 Behav	em for Managing, Archiving and Handling Documents al Endurants e Identifiers hents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States"	$\begin{array}{c} 42\\ 42\\ 42\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav A.11.1 A.11.2 A.11.3 Behav Inter-E	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers bents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States"	$\begin{array}{c} 42\\ 42\\ 42\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2 A.11.3 Behav S.11.3 Behav	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers nents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Annotations Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Sehaviour Messages with Respect to the Archive	$\begin{array}{c} 42\\ 42\\ 42\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2 A.11.3 Behav Inter-F A.13.1 A.13.2 A.13.2	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers nents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Contents: Text/Graphics Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Behaviour Messages with Respect to the Archive Management Messages with Respect to Handlers Document Assage Bishte	$\begin{array}{c} 42\\ 42\\ 42\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$
	A.3 A.4 A.5 A.6 A.7 A.8 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behave Chann An Inf Behave Time A.11.1 A.11.2 A.11.3 Behave Inter-E A.13.1 A.13.2 A.13.3 A.13.4	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers hents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Behaviour Messages Management Messages with Respect to the Archive Management Messages with Respect to Handlers Document Access Rights	$\begin{array}{c} 42\\ 42\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 46\\ 47\\ 8\\ 49\\ 49\\ 49\\ 50\\ 51\\ 51\\ 52\\ 52\end{array}$
	A.3 A.4 A.5 A.6 A.7 A.8 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2 A.11.3 Behav Inter-E A.13.1 A.13.2 A.13.3 A.13.4 A.13.5	em for Managing, Archiving and Handling Documents bal Endurants e Identifiers enents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Behaviour Messages Management Messages with Respect to the Archive Management Messages with Respect to Management Archive Messages with Respect to Management	$\begin{array}{c} 422\\ 422\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 46\\ 47\\ 48\\ 49\\ 49\\ 50\\ 51\\ 51\\ 52\\ 52\\ 52\\ 52\end{array}$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Chann A.11.1 A.11.2 A.11.3 Behav Inter-F A.13.1 A.13.2 A.13.3 A.13.4 A.13.5 A.13.6	em for Managing, Archiving and Handling Documents hal Endurants l Identifiers hents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Behaviour Messages Management Messages with Respect to the Archive Management Messages with Respect to Management Archive Messages with Respect to Documents Handler Messages with Respect to Documents Handler Messages with Respect to Documents Handler Messages with Respect to Documents	$\begin{array}{c} 422\\ 422\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 46\\ 47\\ 48\\ 49\\ 49\\ 49\\ 50\\ 51\\ 51\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52\\ 52$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique Docum A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Chann A.11.1 A.11.2 A.11.3 Behav S Inter-F A.13.1 A.13.2 A.13.3 A.13.4 A.13.5 A.13.6 A.13.7	em for Managing, Archiving and Handling Documents hal Endurants l Identifiers hents: A First View Document Identifiers Document Descriptors Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Management Messages with Respect to the Archive Management Messages with Respect to Management Archive Messages with Respect to Documents Handler Messages with Respect to Documents Handler Messages with Respect to Management An Infermal RSL Construct	$\begin{array}{c} 422\\ 422\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 46\\ 7\\ 88\\ 49\\ 49\\ 49\\ 50\\ 51\\ 51\\ 52\\ 52\\ 52\\ 53\\ \end{array}$
	A.3 A.4 A.5 A.6 A.7 A.8 A.9 A.10 A.11 A.12 A.13	A Syst Princip Unique A.6.1 A.6.2 A.6.3 A.6.4 A.6.5 A.6.6 Behav Chann An Inf Behav Time A.11.1 A.11.2 A.11.3 Behav Inter-F A.13.1 A.13.2 A.13.3 A.13.4 A.13.5 A.13.6 A.13.7 A.13.8	em for Managing, Archiving and Handling Documents hal Endurants ledentifiers hents: A First View Document Identifiers Document Descriptors Document Annotations Document Annotations Document Contents: Text/Graphics Document Histories A Summary of Document Attributes ours: An Informal, First View els, A First View ormal Graphical System Rendition our Signatures Time and Time Intervals: Types and Functions A Time Behaviour and a Time Channel An Informal RSL Construct our "States" Behaviour Messages Management Messages with Respect to the Archive Management Messages with Respect to Management Archive Messages with Respect to Documents Handler Messages with Respect to Documents A Summary of Behaviour Interactions	$\begin{array}{c} 422\\ 422\\ 43\\ 43\\ 43\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44\\ 44$

	$\Delta 15$ Cha	anels: A Final View	54
	A 16 Am		. 01 E4
	A.10 AI		. 04
	A.1	.I The Create Behaviour: Left Fig. 0 on Page 55	. 54
	A.1	.2 The Edit Behaviour: Right Fig. 6 on Page 55	. 55
	A.1	.3 The Read Behaviour: Left Fig. 7 on Page 56	. 55
	A.1	4 The Copy Behaviour: Right Fig. 7 on Page 56	. 55
	A 1	5 The Grant Behaviour: Left Fig. 8 on Page 57	56
	Δ 1	6 The Shred Behaviour: Right Fig. 8 on Page 57	. 57
	A.1/ Inc	Benaviour Actions	. 37
	A.1	.I Management Behaviour	. 57
		Management Create Behaviour: Left Fig. 6 on Page 55	. 58
		Management Copy Behaviour: Right Fig. 7 on Page 56	. 59
		Management Grant Behaviour: Left Fig. 8 on Page 57	. 60
		Management Shred Behaviour: Right Fig. 8 on Page 57	60
	Λ 1		. 00
	A.1		. 01
		The Archive Create Behaviour: Left Fig. 6 on Page 55	. 61
		The Archive Copy Behaviour: Right Fig. 7 on Page 56	. 62
		The Archive Shred Behaviour: Right Fig. 8 on Page 57	. 62
	A.1	.3 Handler Behaviours	. 63
		The Handler Create Behaviour: Left Fig. 6 on Page 55	63
		The Handler Edit Debuilder Dick Fig. 6 on Dage 55	. 00
		The Handler Eult Behaviour. Ngint Fig. 0 of Fage 55	. 05
		The Handler Read Behaviour: Left Fig. 7 on Page 56	. 64
		The Handler Copy Behaviour: Right Fig. 7 on Page 56	. 64
		The Handler Grant Behaviour: Left Fig. 8 on Page 57	. 65
	A.1	4 Document Behaviours	. 65
		The Document Edit Behaviour: Right Fig. 6 on Page 55	65
		The Document Read Behaviour: Left Fig. 7 on Page 56	. 66
		The Document Kear Dehaviour Birkt Fig. 9 on Days 57	. 00
	A 10 C		. 00
	A.18 Cor	ciusion	. 67
-			
~	DSI: Ih	RAINENDOCIICDOIODOIOOOOOOOOOO	
Б	NJL. III	MAISE Specification Language – A Frinter	68
D	B.1 Typ		. 68
Б	B.1 <b>Typ</b> B.1	Expressions	. 68 . 68
D	B.1 <b>Typ</b> B.1 B.1	Expressions	. 68 . 68 . 68 . 68
Б	B.1 <b>Typ</b> B.1 B.1 B.1	Expressions     Composite Types     Composite Types	. 68 . 68 . 68 . 68
Б	B.1 <b>Typ</b> B.1 B.1 B.1	Expressions     Atomic Types     Composite Types     Concrete Composite Types     Sorts and Observer Functions	08 . 68 . 68 . 68 . 68 . 68
D	B.1 Typ B.1 B.1 B.1	Expressions       Atomic Types         Composite Types       Concrete Composite Types         Sorts and Observer Functions       Definitions	68 68 68 68 68 68 68 68 69
В	B.1 Typ B.1 B.1 B.2 Typ	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions	68 68 68 68 68 68 68 68 69 70
В	B.1 Typ B.1 B.1 B.1 B.2 Typ B.2	Expressions       Atomic Types         2 Composite Types       Concrete Composite Types         2 Sorts and Observer Functions       Concrete Types         2 Concrete Types       Concrete Types	68 68 68 68 68 68 69 70 70
D	B.1 Typ B.1 B.1 B.1 B.2 B.2 B.2 B.2 B.2	Expressions       Atomic Types         Composite Types       Concrete Composite Types         Sorts and Observer Functions       Definitions         Concrete Types       Souther types         Subtypes       Subtypes	08           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         69           .         70           .         70
D	B.1 Typ B.1 B.1 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Definitions         Concrete Types         Subtypes         Sorts — Abstract Types	08           .         68           .         68           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70
D	B.1 Typ B.1 B.1 B.2 Typ B.2 Typ B.2 B.2 B.2 B.2 B.2	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus	08           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70           .         70           .         70
D	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Atomic Types       Atomic Types         Composite Types       Concrete Composite Types         Sorts and Observer Functions       Definitions         Concrete Types       Sorts — Abstract Types         Sorts — Abstract Types       RSL Predicate Calculus         Desitional Expressions       Sorts	08           .         68           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         71           .         71
B	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Atomic Types         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus         Dositional Expressions	08           .         68           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70           .         71           .         71
D	B.1 Typ B.1 B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Atomic Types         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus         positional Expressions         Simple Predicate Expressions	08           .         68           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         71           .         71           .         71
D	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4	Atomic Types         2 Composite Types         2 Composite Types         2 Concrete Composite Types         Sorts and Observer Functions         2 Definitions         2 Subtypes         3 Sorts — Abstract Types         Predicate Calculus         positional Expressions         2 Quantified Expressions	08           .         68           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         71           .         71           .         71
D	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor	Atomic Types         2 Composite Types         2 Composite Types         2 Concrete Composite Types         3 Sorts and Observer Functions         2 Definitions         2 Subtypes         3 Sorts — Abstract Types         RSL Predicate Calculus         positional Expressions         2 Quantified Expressions         2 Quantified Expressions         2 Concrete RSL Types: Values and Operations	08           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         71           .         71           .         71           .         71           .         71
D	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5	Atomic Types   2 Composite Types   2 Composite Types   2 Concrete Composite Types   3 Sorts and Observer Functions   2 Definitions   2 Subtypes   3 Sorts — Abstract Types   8 Sorts — Abstract Types   9 Sorts — Abstract Types   9 Sorts — Abstract Types   9 Simple Predicate Expressions   2 Quantified Expressions   2 Quantified Expressions   1 Arithmetic	08           .         68           .         68           .         68           .         69           .         70           .         70           .         70           .         70           .         70           .         70           .         70           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71
Б	B.1 Typ B.1 B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Atomic Types   2 Composite Types   2 Composite Types   2 Concrete Composite Types   3 Sorts and Observer Functions   2 Definitions   1 Concrete Types   2 Subtypes   3 Sorts — Abstract Types   8 Sorts — Abstract Types   9 Sortional Expressions   1 Simple Predicate Expressions   2 Quantified Expressions   2 Quantified Expressions   1 Arithmetic   2 Set Expressions	08           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         70           .         70           .         70           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.5 Cor B.5 B.5	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus         positional Expressions         Simple Predicate Expressions         Quantified Expressions         Arithmetic         Set Expressions         Set Enumerations	08           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         70           .         70           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         72           .         72
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.5 Cor B.5 B.5	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus         positional Expressions         Simple Predicate Expressions         Quantified Expressions         Arithmetic         Set Expressions         Set Enumerations         Set Enumerations	08           68           68           68           68           68           69           70           700           700           701           711           711           711           711           711           711           711           711           711           711           711           712           722           722
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Pefinitions         Concrete Types         Sorts - Abstract Types         Quantified Expressions         Quantified Expressions         Set Expressions         Set Enumerations         Set Comprehension         Correster Expressions         Set Comprehension	$\begin{array}{c} 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\ 08 \\$
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 Pro B.4 B.5 Cor B.5 B.5 B.5	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Definitions         Concrete Types         Sorts - Abstract Types         Sorts - Abstract Types         RSL Predicate Calculus         positional Expressions         Simple Predicate Expressions         Quantified Expressions         Crete RSL Types: Values and Operations         Arithmetic         Set Expressions         Set Comprehension         Cartesian Expressions	08           68           68           68           68           68           69           70           70           70           71           71           71           71           71           71           71           71           71           71           71           71           71           71           71           71           71           72           72           72           72           72
в	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	Expressions         Atomic Types         Composite Types         Concrete Composite Types         Sorts and Observer Functions         Definitions         Concrete Types         Subtypes         Sorts — Abstract Types         RSL Predicate Calculus         positional Expressions         Simple Predicate Expressions         Quantified Expressions         Arithmetic         Set Expressions         Set Expressions         Set Expressions         Set Expressions         Set Expressions         Set Enumerations         Set Comprehension         Cartesian Expressions         Cartesian Enumerations	08           68           68           68           68           68           700           700           700           700           711           711           711           711           711           711           711           711           711           712           722           722           722           722           722
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	e Expressions         1 Atomic Types         2 Composite Types         2 Composite Types         Sorts and Observer Functions         e Definitions         1 Concrete Types         2 Subtypes         3 Sorts — Abstract Types         RSL Predicate Calculus         sositional Expressions         2 Quantified Expressions         2 Set Expressions         3 Arithmetic         2 Set Expressions         3 Set Enumerations         3 Set Comprehension         3 Cartesian Expressions         3 Cartesian Enumerations         4 List Expressions	08           68           68           68           68           69           700           700           710           711           711           711           711           711           712           722           722           722           722           722           722           722           722           722
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5 B.5	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>positional Expressions</li> <li>Quantified Expressions</li> <li>Crete RSL Types: Values and Operations</li> <li>Arithmetic</li> <li>Set Expressions</li> <li>Set Enumerations</li> <li>Set Comprehension</li> <li>Cartesian Expressions</li> <li>List Expressions</li> </ul>	08           68           68           68           68           69           700           700           710           711           711           711           711           712           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           723           724           725
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5 B.5	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>positional Expressions</li> <li>Quantified Expressions</li> <li>Crete RSL Types: Values and Operations</li> <li>Arithmetic</li> <li>Set Expressions</li> <li>Set Expressions</li> <li>Set Comprehension</li> <li>Cartesian Enumerations</li> <li>List Expressions</li> <li>List Expressions</li> </ul>	08           68           68           68           68           69           700           700           710           711           711           711           711           712           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           722           723           724           725
Б	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5 B.5 B.5 B.5	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>positional Expressions</li> <li>Simple Predicate Expressions</li> <li>Quantified Expressions</li> <li>Arithmetic</li> <li>Set Expressions</li> <li>Set Enumerations</li> <li>Set Comprehension</li> <li>Cartesian Expressions</li> <li>List Expressions</li> <li>List Expressions</li> <li>Map Expressions</li> </ul>	08           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         68           .         70           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         71           .         72           .         72           .         72           .         72           .         72           .         72           .         72           .         72           .         72 <tr td="">         .</tr>
в	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5 B.5 B.5 B.5	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>constituent of the expressions</li> <li>Quantified Expressions</li> <li>Crete RSL Types: Values and Operations</li> <li>Arithmetic</li> <li>Set Expressions</li> <li>Set Enumerations</li> <li>Cartesian Enumerations</li> <li>List Expressions</li> <li>List Expressions</li> <li>Map Expressions</li> </ul>	08           68           68           68           68           69           700           700           701           711           711           711           711           712           722           722           722           722           722           722           722           722           723           73
в	B.1 Typ B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.3 The B.4 Pro B.4 B.4 B.5 Cor B.5 B.5 B.5 B.5 B.5 B.5 B.5	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>sositional Expressions</li> <li>Quantified Expressions</li> <li>Quantified Expressions</li> <li>Set Expressions</li> <li>Set Expressions</li> <li>Set Expressions</li> <li>Set Enumerations</li> <li>List Expressions</li> <li>List Enumerations</li> <li>Map Expressions</li> <li>Map Enumerations</li> </ul>	$\begin{array}{c} 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ $
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Б	B.1 Typ B.1 B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>RSL Predicate Calculus</li> <li>positional Expressions</li> <li>Quantified Expressions</li> <li>Quantified Expressions</li> <li>Set Expressions</li> <li>Set Enumerations</li> <li>Cartesian Expressions</li> <li>Cartesian Expressions</li> <li>List Enumerations</li> <li>List Comprehension</li> <li>Map Expressions</li> <li>Map Expressions</li> <li>Set Operations</li> <li>Set Operations</li> <li>Set Operators</li> <li>Set Operator Signatures</li> </ul>	$\begin{array}{c} 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ $
Б	B.1 Typ B.1 B.1 B.1 B.2 Typ B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2 B.2	<ul> <li>Expressions</li> <li>Atomic Types</li> <li>Composite Types</li> <li>Concrete Composite Types</li> <li>Sorts and Observer Functions</li> <li>Definitions</li> <li>Concrete Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>Subtypes</li> <li>Sorts — Abstract Types</li> <li>Quantified Expressions</li> <li>Quantified Expressions</li> <li>Quantified Expressions</li> <li>Set Expressions</li> <li>Set Expressions</li> <li>Cartesian Expressions</li> <li>List Enumerations</li> <li>List Enumerations</li> <li>List Enumerations</li> <li>Map Expressions</li> <li>Set Operator Signatures</li> <li>Set Expressions</li> </ul>	$\begin{array}{c} 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ 08\\ $

		Set Operator Definitions	74
	B.5.7	Cartesian Operations	75
	B.5.8	List Operations	75
		List Operator Signatures	75
		List Operation Examples	75
		Informal Explication	75
		List Operator Definitions	76
	B.5.9	Map Operations	77
		Map Operator Signatures and Map Operation Examples	77
		Map Operation Explication	77
		Map Operation Redefinitions	78
B.6	$\lambda$ -Calc	ulus + Functions	78
	B.6.1	The $\lambda$ -Calculus Syntax	78
	B.6.2	Free and Bound Variables	78
	B.6.3	Substitution	79
	B.6.4	$\alpha$ -Renaming and $\beta$ -Reduction	79
	B.6.5	Function Signatures	79
	B.6.6	Function Definitions	79
B.7	Other	Applicative Expressions	80
	B.7.1	Simple let Expressions	80
	B.7.2	Recursive let Expressions	80
	B.7.3	Predicative let Expressions	81
	B.7.4	Pattern and "Wild Card" let Expressions	81
	B.7.5	Conditionals	81
	B.7.6	Operator/Operand Expressions	82
B.8	Impera	ative Constructs	82
	B.8.1	Statements and State Changes	82
	B.8.2	Variables and Assignment	82
	B.8.3	Statement Sequences and skip	82
	B.8.4	Imperative Conditionals	83
	B.8.5	Iterative Conditionals	83
	B.8.6	Iterative Sequencing	83
B.9	Proces	ss Constructs	83
	B.9.1	Process Channels	83
	B.9.2	Process Composition	83
	B.9.3	Input/Output Events	83
	B.9.4	Process Definitions	84

## 1 Introduction

"Urban planning is a technical and political process concerned with the development and use of land, planning permission, protection and use of the environment, public welfare, and the design of the urban environment, including air, water, and the infrastructure passing into and out of urban areas, such as transportation, communications, and distribution networks."<sup>2</sup>

In this research note we shall try to understand two of the aspects of the domain underlying urban planning, (i) namely those of the "input" information to and "output" plans (etc.) from urban planning, and (ii) that of some possible urban planning (development) functions and processes. We are trying to understand and describe a domain, not requirements for IT for that domain and certainly not the IT (incl. its software). And: We are certainly not constructing any general or any specific urban plan!

The overall aim of this report is to suggest a formal foundation for urban planning. Another, secondary aim of this report is to suggest that a number of requirements must be satisfied before a fully professional urban development project can be commenced (cf. Sect. ??).

Version 2

<sup>&</sup>lt;sup>2</sup>https://en.wikipedia.org/wiki/Urban\_planning

#### 1.1 **On Urban Planning**

We search for answers to the question: "What is Urban Planning?". First we identify "planning areas". Then we sketch element of a first domain model for Urban Planning.

Urban planning seems to be also be about *infrastructure planning*. So we examine these terms. First the latter, then the former.

#### 1.1.1 Infrastructures

The term 'infrastructure' has gained currency in the last 80 years.<sup>3</sup>. It is more frequently used in socio-economic than in scientific, let alone computing science, contexts. According to the World Bank, 'infrastructure' is an umbrella term for many activities referred to as 'social overhead capital' by some development economists, and encompasses activities that share technical and economic features (such as economies of scale and spill-overs from users to non-users). We take a more technical view, and see infrastructures as concerned with supporting other systems or activities. Software for infrastructures is likely to be distributed and concerned in particular with supporting communication of data, people and/or materials. Hence issues of openness, timeliness, security, lack of corruption and resilience are often important.

Examples of infrastructures, or, more precisely, infrastructure components, are:

- transport systems (roads, railways, air traffic, canals/rivers/lake/ocean , etc.);
- water and sewage;
- telecommunications;
- postal service (physical letters, packages etc.);
- power: electricity, gas, oil, wind (generation, distribution); etc.
- the financial industry (banking, insurance, securities, clearing, etc.);

- documents (creation, editing, formatting, etc.);
- ministry of finance (taxation, budget, treasury, etc.);
- health care (private physicians, clinics, hospitals, pharmacies, etc.);
- education (kindergartens, pre-schools, primary schools, secondary schools, high schools, colleges, universities);
- manufacturing industry;
- etcetera.

#### 1.1.2 Wikipedia: https://en.wikipedia.org/wiki/Urban\_planning

"Urban planning is a technical and political process concerned with the **development and use of land** planning permission, protection and use of the environment, **public wellfare**, and the design of the urban environment, including **air**, **water**, **and the infrastructure** passing into and out of urban areas, such as **transportation**, **communications**, and **distribution networks** [2]."

"Urban planning is also referred to as urban and regional planning, regional planning, town planning, city planning, rural planning or some combination in various areas worldwide. It takes many forms and it can share perspectives and practices with urban design [1]."

"Urban planning guides orderly development in urban, suburban and rural areas. Although predominantly concerned with the planning of settlements and communities, urban planning is also responsible for the planning and development of water use and resources, rural and agricultural land, parks

<sup>&</sup>lt;sup>3</sup>Winston Churchill is quoted to have said, in the House of Commons, in 1936: ... the young Labourite speaker, that we just heard, obviously wishes to impress his constituency with the fact that he has attended Eton and Oxford when he uses such modern terms as 'infrastructure' ...

and conserving areas of natural environmental significance. Practitioners of urban planning are concerned with research and analysis, strategic thinking, architecture, urban design, public consultation, policy recommendations, implementation and management [3]."

"Urban planners work with the cognate fields of architecture, landscape architecture, civil engineering, and public administration to achieve strategic, policy and sustainability goals. Early urban planners were often members of these cognate fields. Today urban planning is a separate, independent professional discipline. The discipline is the broader category that includes different sub-fields such as land-use planning, zoning, economic development, environmental planning, and transportation planning [4]."

#### 1.1.3 Theories of Urban Planning

"Planning theory is the body of scientific concepts, definitions, behavioral relationships, and assumptions that define the body of knowledge of urban planning. There are eight procedural theories of planning that remain the principal theories of planning procedure today: the rational-comprehensive approach, the incremental approach, the transactive approach, the communicative approach, the advocacy approach, the equity approach, the radical approach, and the humanist or phenomenological approach [5]."

**Technical aspects** Technical aspects of urban planning involve applying scientific, technical processes, considerations and features that are involved in planning for land use, urban design, natural resources, transportation, and infrastructure. Urban planning includes techniques such as: predicting population growth, zoning, geographic mapping and analysis, analyzing park space, surveying the water supply, identifying transportation patterns, recognizing food supply demands, allocating healthcare and social services, and analyzing the impact of land use.

**Urban planners** An urban planner is a professional who works in the field of urban planning for the purpose of optimizing the effectiveness of a community's land use and infrastructure. They formulate plans for the development and management of urban and suburban areas, typically analyzing land use compatibility as well as economic, environmental and social trends. In developing the plan for a community (whether commercial, residential, agricultural, natural or recreational), urban planners must also consider a wide array of issues such as sustainability, air pollution, traffic congestion, crime, land values, legislation and zoning codes.

The importance of the urban planner is increasing throughout the 21st century, as modern society begins to face issues of increased population growth, climate change and unsustainable development. An urban planner could be considered a green collar professional.[clarification needed]

#### 1.1.4 References

1 "What is Urban Planning" (retrieved April 24, 2015) https://mcgill.ca/urbanplanning/planning

"Modern urban planning emerged as a profession in the early decades of the 20th century, largely as a response to the appalling sanitary, social, and economic conditions of rapidly-growing industrial cities. Initially the disciplines of architecture and civil engineering provided the nucleus of concerned professionals. They were joined by **public health** specialists, economists, sociologists, lawyers, and geographers, as the complexities of managing cities came to be more fully understood. Contemporary urban and regional planning techniques for survey, analysis, design, and implementation developed from an interdisciplinary synthesis of these fields. Today, urban planning can be described as a technical and political process concerned with the welfare of people, control of the use of land, design of the urban environment including transportation and communication networks, and protection and enhancement of the natural environment."

- 2 Van Assche, K., Beunen, R., Duineveld, M., & de Jong, H. (2013). Co-evolutions of planning and design: Risks and benefits of design perspectives in planning systems. Planning Theory, 12(2), 177-198.
- 3 Taylor, Nigel (2007). Urban Planning Theory since 1945, London, Sage.
- 4 https://www.planning.org/aboutplanning/whatisplanning.htm: "What Is Planning?". www.planning.org. Retrieved 2015-09-28.
- 5 https://www.planetizen.com/node/73570/how-planners-use-planning-theory: How Planners Use Planning Theory. Andrew Whittmore of the University of North Carolina Department of Urban and Regional Planning identifies planning theory in everyday practice.

## 1.2 A Triptych of Software Development

Before hardware and software systems can be designed and coded we must have a reasonable grasp of "its" requirements; before requirements can be prescribed we must have a reasonable grasp of "the underlying" domain. To us, therefore, software engineering contains the three sub-disciplines:

- domain engineering,
- requirements engineering and
- software design.

By a domain description we understand a collection of pairs of narrative and commensurate formal texts, where each pair describes either aspects of an endurant (i.e., a data) entity or aspects of a perdurant (i.e., an action, event or behaviour) entity.

## 1.3 **On Formality**

We consider software programs to be formal, i.e., mathematical, quantities — rather than of social/psychological interest. We wish to be able to reason about software, whether programs, or program specifications, or requirements prescriptions, or domain descriptions. Although we shall only try to understand some facets of the domain of urban planning we shall eventually let such an understanding, in the form of a precise, formal, mathematical, although non-deterministic, i.e., "multiple choice", description be the basis for subsequent requirements prescriptions for software support, and, again, eventually, "the real software itself", that is, tools, for urban planners. We do so, so that we can argue, eventually prove formally, that the software *is correct* with respect to the (i.e., its) formally prescribed requirements, and that the software *meets customer*, i.e., domain users' *expectations* – as expressed in the formal domain description.

## 1.4 On Describing Domains

If we can describe some domain phenomenon in logical statements and if these can be transcribed into some form of mathematical logic and set theory then we may have to describe it: narratively and formally. That is, even though it may be humanly or even technologically very cumbersome or even impossible to implement what is described we may find it necessary to describe it. As to when we have to describe something – that is another matter !<sup>4</sup> Let us give an example: The example is that of the domain of documents. Documents may be created, edited, read, copied, referred to, and shredded. We may talk, meaningfully, that is, rationally, logically, about the previous version of a document, and

 $<sup>^{4}</sup>$ We may find occasions in this document to discuss this "other matter" !

#### Towards a Formal Understanding of Urban Planning

hence we may be obliged to model document versions as from their first creation, who created, who edited, who read, who copied, and who shredded (sic!) a document, including, perhaps, the location and time of these operations, how they were edited, etc., etc. Let us take another example. As for the meteorological properties of any specific geographic area, these properties, like temperature, humidity, wind, etc., vary, in reality, continuously over time, from location to location, including altitude. In modeling meteorological properties we may be well-served when modeling exactly their continuous, however "sporadic" nature. To a first approximation we do not have to bother as to whether we can actually "implement" the recording of such continuous, "sporadic" "behaviours". In that sense the domain analyser cum describer is expected to be like the physicists,<sup>5</sup> certainly not like programmers. That is: the domain analyser cum describer are not necessarily describing computable domains.

## 1.5 Reiterating Domain Modeling

Any domain description is an approximation. One cannot ever hope to have described all facets of any domain. So, in setting out to analyse & describe a domain one is not trying to produce a definitive, final, model; one is merely studying and recording (some) results of that study. One is prepared to reiterate the study and produce alternative models. From such models one can develop requirements, [4], for software that in one way or another support activities of the domain. If you are to seriously develop software in this way, for example for the support of urban planners, then you must be prepared to "restart" the process, to develop, from scratch, a domain model. You have a basis from which to start, namely this report [9]. But do not try to simply modify it. Study [9] in depth, but rethink that basis. A description, any description, can be improved. Perhaps the emphasis should be refocused. For the example of software (incl. IT) support for the keeping, production, editing, etc., of the very many documents that are needed during urban planning, you may, in addition to refocusing the present report's focus on the documents of the very many document categories that are presumed, introduced and further elaborated upon in the present report, also study [5]. A principle guiding us in the reformulation of a domain model to be the basis for a specific software product is that we must strive to document all the assumptions about the context in which this software is to serve – otherwise we cannot hope to achieve a product that meets its customers expectations.

#### 1.6 Partial, Precise, and Approximate Descriptions

By a *partial description* we mean a description which covers only a fraction of the domain as a group of people working in that domain, that is, professionals, would otherwise talk about. Descriptions are here taken to describe *behaviours: first "do this*", then "do that"! By a *precise description* we mean a description which in whatever behaviour it describes, partially or fully, does so precisely, that is, it is precisely as described, no more, no less. By an *approximate description* we mean a description which in whatever behavior it describes, partially or fully, even when precisely so, allows for a set of interpretations. We shall then avail ourselves of two forms of 'approximation': *internal non-determinism* and *external non-determinism*. By *internal non-deterministic behaviour* we shall mean a behaviour whose "next step, next move" is "determined" by some "own flipping a coin". By *external non-deterministic behaviour* we shall mean a behaviour whose "next step, next move" is "determined" by some "outside demon"! In describing urban planning we shall allow for: partial descriptions: not all is described and what has been selected for description has been so, perhaps rather arbitrarily, by us, i.e., me, and both forms of 'approximation'. We shall endeavour to indicate where and why we present only partial descriptions, and deploy 'approximation'.

 $<sup>^{5}</sup>$ It is written above: that domain descriptions are based on mathematical logic and set theory. Yes, unfortunately! To properly describe domains involving continuity we need "mix" logic with classical calculus: differential equations, integrals, etc. And here we have nothing to say: the ability, in an informed ways, to blend mathematical logic and set theoretic descriptions with differential equations, integrals, etc., is almost non-existent as of 2017/2018!

## 1.7 On Formal Notations

To be able to prove formal correctness and meeting customer expectations we avail ourselves of some formal notation. In this research note we use the RAISE [12] Specification Language, RSL, [11]. Other formal notations, such as Alloy [14], Event B [1], VDM-SL [7, 8, 10] or Z [15] could be used. We choose RSL since it, to our taste, nicely embodies Hoare's concept of *Communicating Sequential Processes*, CSP [13].

## 1.8 On the Form of This Research Note

The present form of this research note, as of January 5, 2018: 09:42 am, is that of recording a development. The development is that of *trying to come to grips with what urban planning is*. We have made the decision, from an early start, that urban planning "as a whole" is a collection of one master and an evolving number of (initially zero) derived urban planning behaviours. Here we have made the choice to model the various behaviours of a complex of urban planning functions.

## 2 An Urban Planning System

We think of urban planning to be "dividable" into master urban planning, master\_up\_beh, and derived urban plannings, derived\_up\_beh<sub>i</sub>, where sub-index i indicate that there may be several, i.e.,  $i \in$  $\{d_1, d_2, ..., d_n\}$ , such derived urban plannings. We think of master urban planning to "convert" physical (geographic, that is, geodetic, cadestral, geo-technical, meteorological, etc.) information about the land area to be developed into a master plan, that is, cartographic, cadestral and other such information (zoning, etc.). And we think of derived urban planning to "convert" master plans into societal and/or technological plans. Societal and technological urban planning concerns are typical such as *industry* zones, commercial (i.e., office and shopping) zones, residential zones, recreational areas, health care, schools, etc. and transport, electricity, water, waste, etc. Each urban planning behaviour, whether 'master' or 'derived', is seen as a sequence of the application of "the same" urban planning function, i.e., an urban planning action – but possibly to different goals so that each application (of "the same" urban planning action) resolves a sub-goal. Each urban planning action takes a number of information arguments and yield information results. The master urban planning behaviour may start one or more derived urban planning behaviours,  $der_up\_beh_i$ , at the end of "completion" of a base urban planning action. Let  $\{d_1, d_2, ..., d_n\}$  index separate derived urban plannings, each concerned with a distinct, i.e., reasonably delineated technological and/or societal urban planning concern. During master urban planning actions may start any of these derived urban plannings once. Thus we think of urban planning as a system of a single master urban planning process (i.e., behaviour), master\_up\_beh, which "spawns" zero, one or more (but a definite number of) derived urban planning processes (i.e., behaviours), der\_up\_beh<sub>i</sub>. Derived urban planning processes, der\_up\_beh<sub>i</sub>, may themselves start other derived urban planning processes, der\_up\_beh<sub>i</sub>, der\_up\_beh<sub>k</sub>, ..., der\_up\_beh<sub>l</sub>. Figure 1 on the facing page is intended to illustrate the following: At time to a master urban planning is started. At time t1 the master urban planning initiates a number of derived urban development, D1, ..., Di. At time  $t_2$  the master urban planning initiates the  $D_j$  derived urban planning. At time  $t_3$  the derived urban planning Di initiates two derived urban plannings, Dk and  $D\ell$ . At time t4 the master urban planning ends. And at time  $t_5$  all urban plannings have ended. Urban planning actions are provided with "input" in the form of either geographic, geodetic, geo-technical, meteorological, etc., information, m\_geo:mTUS<sup>6</sup>, or auxiliary information, m\_aux:mAUX, or requirements information, m\_req:mREQ. The auxiliary ("management") information is such as time and date, name (etc.) of information provider,

 $<sup>^{6}</sup>$ The m\_ value prefixes and the m type prefixes shall designate master urban planning entities.

#### Towards a Formal Understanding of Urban Planning



Figure 1: An Urban Planning Development

"trustworthiness" of information, etc. The requirements information serves to direct, to inform, the urban planners towards what kind of urban plan is desired.

# **3** Formalisation of Urban Space and Planning Endurants

## 3.1 Some Auxiliary Concepts

## 3.1.1 **Points and Areas**

- 6 We shall assume a notion of *the urban space*, tus:TUS, from which we can observe the attribute: an infinite, compact Euclidean set of points.
- 7 By a *point* we shall understand a further undefined atomic notion.
- 8 By an *area* we shall understand a concept, related to the urban space, that allows us to speak of "*a point being in an area*" and "*an area being equal to or properly within another area*".
- 9 To an[y] *urban space* we can associate an area; we may think of an area being an *attribute* of the urban space.

type 6 TUS value 6 attr\_Pts: TUS  $\rightarrow$  Pt-infset type 7 Pt 8 Area value 9 attr\_Area: TUS  $\rightarrow$  Area 8 is\_Pt\_in\_Area: Pt  $\times$  (TUS|Area)  $\rightarrow$  Bool 8 is\_Area\_within\_Area: Area  $\times$  (TUS|Area)  $\rightarrow$  Bool

11

Version 2

#### 3.1.2 Time and Time Intervals

10 Time is modeled as a continuous entity.

- 11 One can subtract two times and obtain a time interval.
- 12 Time intervals are likewise modeled as continuous entities.
- 13 One can add or subtract a time interval to, resp. from a time and obtain a time.
- 14 One can compare two times, or two time intervals.
- 15 One can add and subtract time intervals.
- 16 One can multiply time intervals with real numbers.

type 10 T 11 TI value 11 sub:  $T \times T \rightarrow TI$ 13 add,sub:  $TI \times T \rightarrow T$ 13  $<, \leq, =, \geq, >: ((T \times T)|(TI \times TI)) \rightarrow Bool$ 15 add,sub:  $TI \times TI \rightarrow TI$ 16 mpy:  $TI \times Real \rightarrow TI$ 

## 3.2 Urban Space Endurants

By an *endurant* we shall understand *an entity that can be observed or conceived and described as a "complete thing" at no matter which given snapshot of time.* Were we to "freeze" time we would still be able to observe the entire endurant.

By the urban space endurants we shall here mean the facts by means of which we can characterize that which is subject to urban planning: the land, what is in and on it, its geodetics, its cadastre<sup>7</sup>, its meteorology, its socio-economics, its rule of law, etc. As such we shall consider 'the urban space' to be a part in the sense of [6]. And we shall consider the geodetic, cadastral, geotechnical, meteorological, "the law" (i.e., state, province, city and district ordinances) and socio-economic properties as attributes.



Left: geodetic map, right: cadastral map.

<sup>&</sup>lt;sup>7</sup>Cadastre: A Cadastre is normally a parcel based, and up-to-date land information system containing a record of interests in land (e.g. rights, restrictions and responsibilities). It usually includes a geometric description of land parcels linked to other records describing the nature of the interests, the ownership or control of those interests, and often the value of the parcel and its improvements. See http://www.fig.net/

#### 3.2.1 Main Part and Attributes

One way of observing *the urban space* is presented: to the left, in the framed box, we **narrate** the story; to the right, in the framed box, we **formalise** it.

17 The Urban Space (TUS) has the following	type		
a Geodetic attributes,	17 TUS, GeoD, Cada, GeoT, Met, Law, SocEco, value		
b Cadastre attributes,	17a attr_GeoD: TUS $ ightarrow$ GeoD		
c <b>Geot</b> echnical attributes,	17a attr_Cada: TUS $\rightarrow$ Cada 17c attr CenT: TUS $\rightarrow$ CenT		
d Meteorological attributes,	17d attr_Met: TUS $\rightarrow$ Met		
e Law attributes,	17e attr_Law: TUS $ ightarrow$ Law		
f ${\mbox{ Socio-Economic attributes, etcetera.}}$	17f attr_SocEco: TUS $\rightarrow$ SocEco		

The attr\_A:  $P \rightarrow A$  is the **signature** of a postulated *attribute (observer) function*. From parts of type P it **observes** attributes of type A. attr\_A are postulated functions. They express that we can always observe attributes of type A of parts of type P.

#### 3.2.2 Urban Space Attributes – Narratives and Formalisation

We describe attributes of the domain of urban spaces. As they are, in real life. Not as we may record them or represent them (on paper or within the computer). We can "freely" model that reality as we think it is. If we can talk about and describe it, then it is so! For meteorological attributes it means that we describe precipitation, evaporation, humidity and atmospheric pressure as these physical phenomena "really" are: continuous over time! Similar for all other attributes. Etcetera.

#### **General Form of Attribute Models**

- 18 We choose to model the *General Form of Attributes*, such as geodetical, cadastral, geotechnical, meteorological, socio-economic, legal, etcetera, as [continuous] functions from time to maps from points or areas to the specific properties of the attributes.
- 19 The points or areas of the properties maps must be in, respectively within, the area of the urban space whose attributes are being specified.

```
type
18 GFA = T \rightarrow ((Pt|Area) \rightarrow Properties)
value
     wf_GFA: GFA \times TUS \rightarrow Bool
19
19
      wf_GFA(gfa,tus) \equiv
19
          let area = attr_Area(tus) in
          \forall t: T \bullet t \in \mathcal{D} gfa \Rightarrow
19
19
               \forall pt:Pt • pt \in dom gfa(t) \Rightarrow is_Pt_in_Area(pt,area)
19
           \land \forall ar: Area \bullet ar \in \mathbf{dom} gfa(t) \Rightarrow is\_within\_Area(ar, area)
19
          end
```

 $\mathcal{D}$  is a hypothesized function which applies to continuous functions and yield their domain!

## Geodetic Attribute[s]

- 20 Geodetic attributes map points to
  - a land elevation and what kind of land it is; and (or) to

- b normal and current water depths and what kind of water it is.
- 21 Geodetic attributes also includes road nets and what kind of roads;

22 etcetera,

type

```
20 GeoD = T \rightarrow (Pt \overrightarrow{m} ((Land|Water) \times RoadNet \times ...))

20a Land = Elevation \times (Farmland|Urban|Forest|Wilderness|Meadow|Swamp|...)

20b Water = (NormDepth \times CurrDepth) \times (Spring|Creek|River|Lake|Dam|Sea|Ocean|...)

21 RoadNet = ...

22 ...
```

**Cadastral Attribute[s]** A cadastre is a public register showing details of ownership of the real property in a district, including boundaries and tax assessments.

23 Cadastral maps shows the boundaries and ownership of land parcels. Some cadastral maps show additional details, such as survey district names, unique identifying numbers for parcels, certificate of title numbers, positions of existing structures, section or lot numbers and their respective areas, adjoining and adjacent street names, selected boundary dimensions and references to prior maps.

 $24\,$  Etcetera.

```
type
23 Cada = T \rightarrow (Area \rightarrow m (Owner \times Value \times ...))
24 ...
```

## Geotechnical Attribute[s]

- 25 Geotechnical attributes map points to
  - a top and lower layer soil etc. composition, by depth levels,
  - b ground water occurrence, by depth levels,
  - c gas, oil occurrence, by depth levels,
  - d etcetera.

type

```
25 GeoT = (Pt  m Composition)
25a Composition = VerticalScaleUnit × Composite*
25b Composite = (Soil|GroundWater|Sand|Gravel|Rock|...|Oil|Gas|...)
25c Soil,Sand,Gravel,Rock,...,Oil,Gas,... = [chemical analysis]
25d ...
```

## Meteorological Attribute[s]

- 26 Meteorological information records, for points (of an area) precipitation, evaporation, humidity, etc.;
  - a precipitation: the amount of rain, snow, hail, etc.; that has fallen at a given place and at the time-stamped moment<sup>8</sup>, expressed, for example, in milimeters of water;
  - b evaporation: the amount of water evaporated (to the air);
  - c atmospheric pressure;
  - d air humidity;
  - e etcetera.

```
26 Met = T \rightarrow (Pt \overrightarrow{m} (Precip \times Evap \times AtmPress \times Humid \times ...))

26a Precip = MMs [milimeters]

26b Evap = MMs [milimeters]

26c AtmPress = MB [milibar]

26d Humid = Percent

26e ...
```

## Socio-Economic Attribute[s]

- 27 Socio-economic attributes include time-stamped area sub-attributes:
  - a income distribution;
  - b housing situation, by housing category: apt., etc.;
  - c migration (into, resp. out of the area);
  - d social welfare support, by citizen category;
  - e health status, by citizen category;

f etcetera.

#### type

```
27 SocEco = T \rightarrow (Area \overrightarrow{m} (Inc×Hou×Mig×SoWe×Heal×...))

27a Inc = ...

27b Hou = ...

27c Mig = {|"in","out"|} \overrightarrow{m} ({|"male","female"|} \overrightarrow{m} (Agegroup × Skills × HealthSumm × ...))

27d SoWe = ...

27e CommHeal = ...

27f ...
```

## Law Attribute[s]: State, Province, Region, City and District Ordinances

28 By the law we mean any state, province, region, city, district or other 'area' ordinance<sup>9</sup>.

 $29\ \dots$ 

 $<sup>^{8}-</sup>$  that is within a given time-unit

 $<sup>^{9}</sup>$ Ordinance: a law set forth by a governmental authority; specifically a municipal regulation: for ex.: A city ordinance forbids construction work to start before 8 a.m.

type 28 Law value 28 attr\_Law: TUS  $\rightarrow$  Law type 28 Law = Area  $\overrightarrow{m}$  Ordinances 29 ...

## **Industry and Business Economics**

TO BE WRITTEN

## **Etcetera**

#### TO BE WRITTEN

**The Urban Space Attributes** Summarising we can model the aggregate of urban space attributes, except for its point space, as follows.

- 30 Each of these attributes can be given a name.
- 31 And the aggregate can be modelled as a map (i.e., a function) from names to appropriately typed attribute values.

#### type

30 TUS\_Attr\_Nm = {|"ged","cad","get","law","eco",...|} 31 TUSm = TUS\_Attr\_Nm  $\xrightarrow{m}$  TUS\_Attr axiom 31  $\forall$  tusm:TUSm •  $\forall$  nm:TUS\_Attr\_Nm • nm  $\in$  dom tusm  $\Rightarrow$ 31 case (nm,mtusm(nm)) of 31 ("ged",v)  $\rightarrow$  is\_GeoD(v), ("cad",v)  $\rightarrow$  is\_CaDa(v), ("get",v)  $\rightarrow$  is\_GeoT(v), 31 ("law",v)  $\rightarrow$  is\_Law(v), ("eco",v)  $\rightarrow$  is\_Eco(v), ... 31 end

## 3.2.3 Discussion

TO BE WRITTEN

#### 3.3 Urban Planning Auxiliaries

By *urban planning auxiliaries* we mean such information that are *not* of geodetic, cadestral, geotechnical, meteorological, etc., nature, that is, are of the land, but are of urban planning project nature: project plan, time & resource schedules, project staffing, project budget, project financing, et cetera.

## 3.4 Urban Planning Requirements

By *urban planning requirements* we mean such information as expresses what the goal of the urban planning project is, i.e., deliverables, when and where; who provides what information; who consumes which information; and project deliverable acceptance criteria for validation and correctness.

## 3.5 Urban Planning Endurants

By an *urban planning endurant* we shall understand a tangible document that, as *urban plans*, can either be formally related to urban space endurants, that is, geodetic, cadestral, geotechnic and meteorological documents, or, as *urban planning ancillaries*, can be related to urban planning auxiliary documents.

#### 3.5.1 Urban Plans

By an *urban plan* we mean a document which describes

MORE TO COME

#### 3.5.2 Urban Planning Ancillaries

#### TO BE WRITTEN

#### **3.6** Assumptions About Urban Space and Planning Attributes

In this section we shall distinguish between assumptions about urban space and planning attributes as these assumptions are concerned with the domain of urban planning. that to the actual, "real world" phenomena of such things as geodesy, cadastre, geo-techniques, meteorology, etc.; and assumptions about urban space and planning attributes as these assumptions are concerned with requirements to the recording of the "real world" phenomena, that is to how the "values" of the phenomena are recorded. Please observe that this report is exclusively about the former. That is, it is not about requirements to the 'data' that may be input to, or output from actual urban planning projects, for example in the form of software data! We shall refer to the former as assumptions about urban space and planning attribute values, and to the latter as assumptions about urban space and planning data.

#### 3.6.1 Assumptions About Urban Space and Planning Attribute Values

The typical assumptions that we make about geodetical, geotechnical and meteorological phenomena are that their values are *continuous* over *time* and *space*, viewed separately and taken together. From this follows that *other* urban planning attributes derived from, or related to geodetical, geotechnical and meteorological phenomena, are themselves, in some sense (to be defined for each kind of *other* urban planning attribute) also *"continuous"*.

#### 3.6.2 Assumptions About Urban Space and Planning Data

Urban space and planning data are data that are strongly *related* to urban space and planning attribute values. But, being thought of a data, as values input to or resulting from urban planning, they are *discrete*, not continuous. That is, the urban space and planning data are approximate, finite *representations* of continuous phenomena. As such we must be able to formalise the *postulated relations* between the continuous urban space and planning attribute values and the discrete urban space and planning data and these relations must be such that we can likewise formalise a *quality factor:* "how good, or bad, is the data representation with respect to the 'real' domain phenomena"?

We leave our (hence short) discourse into the two concepts: assumptions about urban space and planning attribute values, and assumptions about urban space and planning data, bearing in mind that we assume "ideal" properties of the domain attribute values, while leaving assumptions about urban space and planning data to further, more final treatment only when dealing with requirements to software for urban planning.

...

Version 2



Figure 2: The Urban Space and Analysis Behaviours

## 4 Two non-Urban Planning Behaviours

In this section we shall "dispense" with two facets of urban planning. One is the modelling of the urban space, another is the modelling of the aggregate, i.e., the ensemble, of urban space analysis functions, in the form of analysis behaviours. Figure 2 hints at what is coming up. It is a "prefix" of Fig. 3 on Page 36.

## 4.1 The Urban Space Behaviour

In this section we shall refer to many other elements of our evolving specification. To grasp the seeming complexity of the urban space, its analyses and its urban planning functions, we refer to Fig. 3 on Page 36.

- 32 To every observable part, like tus: TUS, there corresponds a behaviour, in this case: the\_urb\_spa.
- 33 the\_urb\_spa behaviour has, for this report, just one static attribute, the point space, Pts.
- 34 the\_urb\_spa behaviour has the following biddable and programmable attributes, the Cadastral, the Law and the SocioEconomic attributes. The biddable and programmable attributes "translate" into behaviour parameters.
- 35 the\_urb\_spa behaviour has the following dynamic, non-biddable, non-programmable attributes, the GeoDetic, GeoTechnic and the Metorological attributes The non-biddable, non-programmable dynamic attributes "translate", in the conversion from parts to behaviours, to input channels etc.

the\_urb\_spa behaviour offers its attributes, upon demand,

- 36 to  $\omega$  urban space analysis behaviours, tus\_ana\_i via an array channel ana\_beh\_ch,
- 37 and one master urban planning behaviour, master\_up\_beh, via channel tus\_m\_ch.
- 38 the\_urb\_spa otherwise behaves as follows:
  - a it repeatedly "assembles" a tuple, tus, of all, except its point set, attributes;
  - b then it external non-deterministically either offers the tus tuple
  - c to either any of the urban space analysis behaviours,
  - d or to the master urban planning behaviour;
  - e in these cases it resumes being the\_urb\_spa behaviour;

#### Towards a Formal Understanding of Urban Planning

f or internal-nondeterministically chooses to

- g update the law, the cadastral, and the socio-economic attributes;
- h whereupon it resumes being the\_urb\_spa behaviour.

#### channel

```
35
     attr_GeoD_ch:GeoD, attr_GeoT_ch:GeoT, attr_Met_ch:Met
36
    tus_m_ch:TUSm
37
     {tus_ana_ch[i]|i \in {1..\omega}}:TUSm
value
32
    tus_beh:
33
         \mathsf{Pts} \rightarrow
34
              (Cada \times Law \times Soc_Eco \times ...) \rightarrow
35
                   in attr_GeoD_ch, attr_GeoT_ch, attr_Met_ch \rightarrow
                   out {ana_beh_ch[i]|i \in {|"m","d1","d2",...,"dn"}|} \rightarrow Unit
36
38
     tus\_beh(pts)(pro) \equiv
           let geo = ["ged" \mapsto attr_GeoD_ch?,"cad" \mapsto cada,"get" \mapsto attr_geoT_ch?,
38a
                        "met"\mapstoattr_Met_ch?,"law"\mapstolaw,"eco"\mapstoeco,...] in
38a
38c
           (([] {tus_ana_ch[i]!geo|i:Nat i \in {1...\omega}})
38b
             Π
38d
            tus_m_ch!geo);
38e
          tus_beh(pts)(pro)) end
38f
38g
           let pro':(Cada×Law×Soc_Eco×...)•fit_pro(pro,pro') in
38h
           tus_beh(pts)(pro') end
      fit_pro: (Cada×Law×Soc_Eco×...) × (Cada×Law×Soc_Eco×...) \rightarrow Bool
38g
```

We leave the *fitness predicate* fit\_pro further undefined. It is intended to ensure that the biddable and programmable attributes evolve in a commensurate manner.

#### 4.2 Urban Space Analysis

Analyses, or various kinds, of the urban spacem is an important prerequisite for urban planning. We therefore introduce a number,  $\omega$ , of urban space analysis behaviours,  $tus\_ana_i$  (for i in the set  $\{1, ..., \omega\}$ . The indexing designates that each  $tus\_ana_i$  caters for a distinct kind of urban space analysis, each analysis with respect to, i.e., across existing urban areas: (1) traffic statistics, (2) income distribution, (3) health statistics, (4) power consumption, ...,  $(\omega)$  ... . We shall model, by an indexed set of behaviours,  $tus\_ana_i$ , the urban [space] analyses that are an indispensable prerequisite for urban planning.

- 39 Urban [space] analyser, tus\_ana<sub>i</sub>, for  $i \in \{1..\omega\}$ , performs analysis of an urban space whose attributes, except for its point set, it obtains from that urban space via channel tus\_ana\_ch and
- 40 offers analysis results to the master\_up\_beh and the n derived\_up\_behaviours.
- 41 Urban analyser,  $tus\_ana_i$ , otherwise behaves as follows:
  - a The analyser obtains, from the urban space, its most recent set of attributes.
  - b The analyser then proceeds to perform the specific analysis as "determined" by its index i.
  - c The result,  $tus\_ana_i$ , is communicated whichever urban, the master or the derived, planning behaviour enquires.

d Whereupon the analyser resumes being the analyser, improving and/or extending its analysis.

```
type
41b TUS_Anal
channel
40 {ana_beh_ch[j]]:Nat•j \in {0...\omega}:TUS_Anal
value
39
     tus_ana<sub>i</sub>: Unit \rightarrow in tus_ana_ch[i]
40
                             out {ana_beh_ch[j]|j:Nat•j \in {0...\omega}} Unit
41 tus_ana<sub>i</sub>() \equiv
            let tusm = tus_ana_ch[i] ? in
41a
41b
            let tus_ana<sub>i</sub> = perform_analysis<sub>i</sub>(tusm) in
41c
            [] {ana_beh_ch[j] ! tus_ana<sub>i</sub> | j:Nat•j \in {0...\omega}};
41d
            tus_ana_i() end end
41b
       perform_analysis<sub>i</sub>: TUSm \rightarrow TUS_Anal
41b
       perform_analysis<sub>i</sub>(tus) \equiv ...
```

# 5 Requirements, Goals and Indicators

## 5.1 Example Graphics of Urban Plans

We show some uncommented graphics related to ["small"] urban plans. The choice of graphics shown reveals that the first author of this report is "a complete dilletante" when it comes to some aspects of urban planning. He therefore looks forward to his tow co-authors, **Prof. Herzog** and **Prof. Wu**, to, **pls., provide real, professional examples of urban plans.** 

## Towards a Formal Understanding of Urban Planning





Towards a Formal Understanding of Urban Planning



The examples shown so far are all very artisic. With pleasing images.



## 5.2 Discussion of Forms & Contents of Urban Plans

What can we conclude from just having seen some, perhaps not so, or not at all, professionally selected images of results of urban plans? As remarked, on Page 22, the "plans" are all very beautiful, creative, aesthetic, more than technical. And we are looking, primarily, for the technical and scientific proerties of urban plans. How can I, DB, summarise urban plans? They all related to an "underlying" urban space. That relationship must be a property of, and/or a relationship between PLAns on one hand and GeoDetic, Cadastral, GeoTechnical, METeorogical, LAW, Socio\_Economic, ..., information on the other hand.

MORE TO COME

It is suggested that this section be co-authored by **Prof. Otthein Herzog**<sup>1</sup> and **Prof. Siegfried ZhiQiang Wu**<sup>2</sup> <sup>1</sup> Jacobs University, Campus Ring 1, 28759 Bremen, Germany <sup>2</sup> CIUC – Tongji University, Siping Campus, Shanghai, China

## 5.3 Requirements to Forms & Contents of Urban Plans

We refer to Sect. 3.6 on Page 17. The term *requirements* in this sub-section's title refer the form and contents of plans: what should they contain, their possible mixture of graphics, formal texts (tables, formulas, ec.) and informal texts.

It is suggested that this section be co-authored by **Prof. Otthein Herzog**<sup>1</sup> and **Prof. Siegfried ZhiQiang Wu**<sup>2</sup> <sup>1</sup> Jacobs University, Campus Ring 1, 28759 Bremen, Germany <sup>2</sup> CIUC – Tongji University, Siping Campus, Shanghai, China

## 6 Master Urban Planning

We begin this section with abstractions of the, perhaps, two most important aspects of urban planning, such as it may be seen by its individual practitioners: the *information* (being handled: the "input", so-to-speak, to urban planning functions) and the urban planning *functions*. In two sections, in-between the *information* and the *function* sections (6.1 and 6.4), we very briefly discuss the *iterative nature* of urban planning, Sect. 6.2 on the next page, and *initial values*, Sect. 6.3, of the various information values.

## 6.1 Urban Planning Information Categories

## 6.1.1 "Input"

Among the arguments of urban planning, in addition to the urban space attributes, see Items 30 - 31 on Page 16, are

42 related, but not geographic, information, mAUX[iliary]<sup>10</sup>;

<sup>&</sup>lt;sup>10</sup>Auxiliary: giving help or support.

25

43 and some requirements, mREQ[uirements].

type 42 mAUX 43 mREQ

## 6.1.2 "Output"

Among results of urban planning are

44 "the plan" (or "plans"), mPLA[ns],

45 and possibly some other ancillary<sup>11</sup> documents, mANC[illerary].

type 44 mPLA 45 mANC

For this and the next sections we shall leave the mTUS, mAUX, and mREQ argument types and the mPLA, and mANC result types further undefined.

## 6.2 The Iterative Nature of Urban Planning

We take it that urban planning proceeds in "cycles":

46 In each cycle the master urban planning function, master\_up\_fct, is applied to an input argument triple, (m\_tus,m\_aux,m\_req):(mTUS×mAUX×mREQ):mTRI, of "fresh" geodetic/cadastral/-geotechnical/meteorological (etc.), auxiliary and requirements information.

type

46 mTRI = mTUS  $\times$  mAUX  $\times$  mREQ

47 Each cycle, that is, each application of master\_up\_fct, results in a "most recent", not necessarily "final", plan and ancillary information, (m\_pla,m\_anc):mPLA×mANC:mRES.

## **type** 47 mRES = mPLA $\times$ mANC

48 But, to "drive" the urban planning process, master\_up\_beh, towards a "final", that is, an adequately satisfactory plan etc., the urban planning function, master\_up\_fct, need also be provided with the previous iteration's result — which we take to be a ("quintuplet"<sup>12</sup>, i.e., a) pair of an (i.e., the "previous") "input" triple and the previous result pair.

#### type 48 mQUI = mTRI $\times$ mRES

<sup>&</sup>lt;sup>11</sup>Ancillary: providing necessary support to the main work

 $<sup>^{12}</sup>$ We put double quotes around the term *quintuplet* to indicate that we do not really mean it to be a quintuplet, but, as here, a pair of a triplet and a pair !

We shall refer to the input argument triple as 'the triplet', and to the "driver" quintuplet as a **resumption**. The above decisions on triplet arguments and quintuplet resumptions, including the latter's "feedback" to a next iteration function invocation is motivated as follows. We think of each invocation, i.e., step, of the urban planning function to "apply" itself to a small fragment of urban planning. Each such "small" step is to result in useful contributions to the evolving urban plan. The ancillary information emerging from each step informs about which aspects of urban planning was pursued in that step: where, in the plans, the outcome of those analysis and plan development can be seen. The reason for small step invocations are to allow ongoing reviews (not shown here), and to pass on intermediary results to other urban planning developments, etc. The decision to "feed" back "records" of the entire state of urban planning development is motivated by the need for these "small step" invocations to analyse the ongoing, full state.

## 6.3 Initialisation

Urban planning proceeds in iterating from initial

- 49 urban space, auxiliary and requirements information, as well as
- 50 (usually "empty") plans and ancillaries.

We extend the notion of initial values to

```
51 triplet arguments,
```

- 52 result pairs, and
- 53 "quintuplet" argument/result pairs.

towards such results (plans and ancillaries) that are deemed satisfactory.

## value

- 49 m\_tus\_init:mTUS,
- 49 m\_aux\_init:mAUX,
- 49 m\_req\_init:mREQ
- 50 m\_pla\_init: mPLA,
- 50 m\_anc\_init:mANC
- 51 m\_tri\_init: mTRI = (m\_tus\_init,m\_aux\_init,m\_req\_init)
- 51 assert: m\_tri\_fit(m\_tri\_init,m\_tri\_init)
- 52 m\_res\_init:  $mRES = (m_pla_init,m_anc_init)$
- 53 m\_qui\_init:  $mQUI = (m_{tri_init,m_res_init})$

We refer to Item 63 on Page 28 for an explanation of the m\_tri\_fit predicate.

## 6.3.1 Existing versus Evolving Plans

The quintuplet "feedback", which includes a 'plan' component, secures that possibly pre-existing plans are included, as initialised components of the plan results.<sup>13</sup> The iterative nature of urban planning thus allows for step-wise urban re-development, from existing "urban land-scapes" via mixed "previous" and "future" land-scapes to the final urban development plan.

 $<sup>^{13}\</sup>mathrm{We}$  refer to Item 31 on Page 16.

## 6.4 A Simple Functional Form

54 The master urban planning function, master\_up\_fct, thus applies to

- (i) a "most recent" triplet of urban space, auxiliary and requirements information, and to
- (ii) a "past quintuplet", a resumption<sup>14</sup>, that is, pair of urban space, auxiliary and requirements information as well as a pair of a plan and ancillary information

and yields such a resumption "quintuplet" pair of a triplet and a pair.

#### To repeat:

- 55 The application of master\_up\_fct to such arguments, i.e., master\_up\_fct(m\_tus,m\_aux,m\_req)(m\_qui) yields a "quintuplet" result, a resumption, m\_qui:((m\_tus',m\_aux',m\_req'),(m\_pla,m\_anc)).
- We "explain" the relations between "input" arguments and "output" (as) results:
  - 56 The "input" argument m\_tri is "carried forward", m\_tri' (=m\_tri), to be redeposited as part of the result.
  - 57 The main part of the result, (m\_pla,m\_anc), is related,  $\mathcal{P}_{master}$ , to the input argument including the previous "result", the resumption.
- 54 master\_up\_fct: mTRI  $\rightarrow$  mQUI  $\rightarrow$  mQUI
- 55 master\_up\_fct(m\_tri)(m\_qui) as (m\_tri',(m\_pla,m\_anc))
- 56  $m_tri = m_tri' \land$
- 57  $\mathcal{P}_{master}(m_{tri})(m_{qui})(m_{pla,m_{anc}})$

For the time being we shall leave the master urban planning function, master\_up\_fct, that is,  $\mathcal{P}_{master}$ , uninterpreted. Of course, "all the tricks of urban planning are 'hidden' in  $\mathcal{P}_{master}$ ".

#### 6.5 Oracles and Repositories

**Oracles** are simple behaviours that *offer* information to other behaviours. **Repositories** are simple behaviours that *store* information from behaviours and *offer* stored information to behaviours.

#### 6.5.1 The Master 'Input' Oracle

An urban planning oracle, when so requested, will select some information – usually in some nondeterministic fashion, and usually subject to some constraint – and present this information to the requestor, i.e., an urban planning behaviour. In this section, i.e. Sect. 6.5.1, we shall deal with one specific oracle, m\_tri\_beh: one that "assembles" triplets, m\_tri, of urban space, m\_tus:mTUS, auxiliary, m\_aux:mAUX, and requirements, m\_req:mREQ, information to requesting behaviours. We introduce a pair of specification components:

58 a *channel*, m\_tri\_ch, over which a master urban planning behaviour, master\_up\_beh, offers to receive triplets, m\_tri:mTRI, from an oracle, m\_tri\_beh,

59 and an *oracle*, m\_tri\_beh, which "remembers" its most recently communicated triplet<sup>15</sup>.

<sup>&</sup>lt;sup>14</sup>Resumption: like a repetition, a continuation

<sup>&</sup>lt;sup>15</sup>The oracle is initialised with b\_tri\_beh(m\_geo\_init,m\_aux\_init,m\_req\_init).

Towards a Formal Understanding of Urban Planning

channel 58 m\_tri\_ch:mTRI value 59 m\_tri\_beh: mTRI → out m\_tri\_ch Unit

- 60 The oracle assembles (m\_tri':mTRI), a master triplet which satisfies a predicate m\_tri\_fit(m\_tri,m\_tri') see Item 63.
- 61 That triplet is offered, m\_tri\_ch ! m\_tri', to the master urban behaviour -
- 62 whereupon the oracle resumes being the oracle, now, however, with the recently assembled master triplet as its resumption.

```
59 m_tri_beh(m_tri) \equiv
```

```
60 let m_tri':mTRI • m_tri_fit(m_tri,m_tri') in
```

```
61 m_tri_ch ! m_tri' ;
```

62 m\_tri\_beh(m\_tri')

```
59 end
```

- 64 pre: m\_tri\_fit(m\_tri,m\_tri)
  - 63 The fitness predicate, m\_tri\_fit(m\_tri,m\_tri'), checks whether a "newly" assembled master triplet, m\_tri', stands in some suitable<sup>16</sup> relation P(m\_tri,m\_tri') to a a similar (f.ex., "earlier") master triplet, m\_tri.
  - 64 The fitness predicate holds for m\_tri\_fit(m\_tri,m\_tri).
- $\textbf{63} \quad m\_tri\_fit: \ mTRI \times mTRI \rightarrow \mathbf{Bool}$
- 63 m\_tri\_fit(m\_tri,m\_tri')  $\equiv \mathcal{P}(m_tri,m_tri')$ 
  - 65 The oracle, m\_tri\_beh, is initialised with an initial triplet value m\_tri\_init, cf. formula Item 51 on Page 26.
- 63 m\_tri\_beh(m\_tri\_init): assert: m\_tri\_fit(m\_tri\_init,m\_tri\_init)

## 6.5.2 The Master Resumption Repository

The "quintuplet" pair of an "input" triple and a result pair,  $m_qui$ : ( $m_tri:mTRI$ , ( $m_pla:mPLA$ ,  $m_anc:mANC$ )) is thought of as residing in a *repository* behaviour,  $m_qui_beh$ , which ( $m_qui_ch$ ?) "receives" "quintuplets" from the urban planning behaviour, or "offers" ( $m_qui_ch ! m_qui$ ) such to the urban planning behaviour.

- 66 There is therefore a channel, m\_qui\_ch, between the urban planning behaviour and the "quintuplet" repository behaviour,
- 67 m\_qui\_beh.
- 68 It either

<sup>&</sup>lt;sup>16</sup>– to be defined for each specific urban planning project

```
69 accepts or
```

70 offers quintuplets.

```
channel

66 m_qui_ch:mQUI

value

67 m_qui_beh: mQUI \rightarrow in,out m_qui_ch Unit

67 m_qui_beh(m_qui) \equiv

69 m_qui_beh(m_qui_ch?)

68 []

70 m_qui_ch!(m_qui); m_qui_beh(m_qui)
```

## 6.6 A Simple Behavioural Form

Urban planning, however, is a time-consuming "affair". So we model it as a behaviour.

- 71 The master\_up\_beh\_0<sup>17</sup> behaviour takes no argument, hence the left signature element: Unit, avails itself of the input channel for obtaining proper input, m\_tri, and m\_qui, for the master urban function, master\_up\_fct, and output channel, for depositing a resumption, m\_qui', and (then) "goes on forever", as indicated by the right signature element: Unit.
  - 71 master\_up\_beh\_0: Unit  $\rightarrow$  in m\_tri\_ch in,out m\_qui\_ch Unit
- 72 The simple (version of the) master\_up\_beh\_0 behaviour
- 73 obtains the master triplet, m\_tri, and the master resumption, m\_qui, information,
- 74 performs the master\_up\_fct planning function and
- 75 provides its result, a resumption, m\_qui', to the master quintuplet repository,
- 76 whereupon it reverts to being master\_up\_beh\_0.

#### value

```
72 master_up_beh_0() \equiv
```

- 73  $let (m_tri,m_qui) = (m_tri_ch?,m_qui_ch?) in$
- 74 **let** m\_qui' = master\_up\_fct(m\_tri)(m\_qui) **in**
- 75 m\_qui\_ch ! m\_qui' end end ;
- 76 master\_up\_beh\_0()

The master\_up\_beh\_0 behaviour repeatedly "performs" urban planning, "from scratch", as if new urban space, auxiliary and requirements information was "new" in every re-planning — "ad infinitum"! We now revise master\_up\_beh\_0 into master\_up\_beh\_1 — a behaviour "almost" like master\_up\_beh\_0, but one which may terminate.

- 77 master\_up\_beh\_1
- 78 first behaves like master\_up\_beh\_0 (Items 73–75)

 $<sup>^{17}</sup>$ As there will be several versions, from simple towards more elaborate, of the master\_up\_beh behaviour, we index them.

- 79 then checks whether the obtained master resumption is satisfactory, that is, is OK as an end-result of master urban planning.
- 80 If so then master\_up\_beh\_1 terminates,
- 81 else it resumes being master\_up\_beh\_1.

## value

```
master_up_beh_1: Unit \rightarrow in m_tri_ch in,out m_qui_ch Unit
71
     master_up_beh_1() \equiv
77
73
       let (m_tri,m_qui) = (m_tri_ch?,m_qui_ch?) in
74
       let m_qui' = master_up_fct(m_tri)(m_qui) in
75
       m_qui_ch ! m_qui';
79
       if master_qui_satisfactory(m_qui')
80
           then skip
81
           else master_up_beh_1() end
77
       end end
```

```
79 master_qui_satisfactory: mQUI \rightarrow Bool
```

The  $m_qui_satisfactory$  predicate inquires the master quintuplet,  $m_qui$ , as for its suitability as a final candidate for an urban plan<sup>18</sup>.

# 7 Derived Urban Plannings

## 7.1 **Preliminaries**

It is a conjecture that urban planning can be "divided" into master urban planning and derived urban plannings.

## MORE TO COME

## 7.1.1 Derived Urban Plan Indices

We think of *master* urban planning function, modeled by **master\_up\_fct**, as being concerned with the overall "division" of the urban space (i.e., geographical area, land and water) into zones for building, recreation, and other (i.e., the *master plan*). Aggregations of these zones, one, more or all (usually several), can then be further "[derive] planned" into zones:

- $(d_1)$  light, medium and heavy industry,
- $(d_5)$  apartment bldg.,

•  $(d_2)$  public works,

• ..., etc.,

- $(d_3)$  office,
- $(d_4)$  mixed shopping and residential,
- (d<sub>m-1</sub>) villa, and
  (d<sub>m</sub>) recreational.

Additional forms of derived plannings are:

 $<sup>^{18}</sup>$  The m\_qui\_satisfactory argument, m\_qui, embodies not only that plan, but also the basis for its determination.

- $(d_{m+1})$  transport;
- $(d_{m+2})$  electricity supply;
- $(d_{m+3})$  water supply;
- $(d_{m+4})$  waste management;

We refer to the  $d_i$ 's as derived urban plan indices.

- 82 We think of this variety of "derived" plannings as indexed such as hinted at above,
- $83\,$  and  $\mathsf{dups}$  as the set of all indices.

type 82  $DP == \{|d_1, d_2, ..., d_n|\}$ value 83  $dups:DP-set = \{d_1, d_2, ..., d_n\}$ 

#### 7.1.2 A "Reservoir" of Derived Urban Planning Indices

84 To secure that at most one derived planning,  $d_i$ , is initiated we introduce a global variable, dps\_var, initialised to an empty set of derived planning tokens and updated with the addition of selected DP tokens.

#### variable

84 dps\_var:DP-set := {} comment dps\_var denotes a reference

#### 7.1.3 A Derived Urban Planning Index Selector

85 A function, sel\_dps, selects zero, one or more "fresh" DP indices, that is, DP tokens that have not been selected before.

value

```
85 sel_dps: Unit \rightarrow DP-set

85 sel_dps() \equiv

85 let dps:DP-set•dps\subseteqdups \ c dps_var in

85 dps_var := c dps_var \cup dps; dps end

comment

84 [ c denotes a contents-taking operator ]
```

We shall revise the above selector in Sect. 7.7 on Page 37.

#### 7.1.4 The Derived Urban Plan Generator

86 We therefore edit the master\_up\_beh\_1 behaviour slightly into the revised master\_up\_beh\_2. In master\_up\_beh\_2 we insert, "in parallel" (||) with the "resumption" of master\_up\_beh\_2 (cf. Item 81 on the facing page), an internal non-deterministic choice behaviour, der\_up(). It specifies the selection of zero, one of more DP tokens, and initiates corresponding derived planning behaviours, der\_up\_beh<sub>i</sub>(), as well as their corresponding "input" triplet oracles, d\_tri\_beh<sub>i</sub>(). But only at most once. These derived planning behaviours, der\_up\_beh<sub>i</sub>, and "input" triplet oracles, der\_tri\_beh<sub>i</sub>() are like master\_up\_beh\_1, respectively m\_tri\_beh, only now they are "tuned" to the specific derived planning issues (i.e., <sub>i</sub>).

- $(d_{m+5})$  health care;
- $(d_{m+6})$  fire brigades;
- ..., etc.,
- $(d_n)$  schools.

Version 2

When behaviour and function invocations where the names of these behaviors or functions names are prefixed with der\_, e.g., der\_name, and are indexed by some  $_i$ , i.e., der\_name $_i$ , then we mean the invocation of one specific i indexed behaviour or function from the indexed set of such, as defined by their behaviour and function definitions, see below.

## value

```
86 der_up: \mathbf{Unit} \rightarrow \mathbf{Unit}
```

der\_up()  $\equiv$  let dps = sel\_dps() in  $\|\{\det_up\_beh_i()\|d\_tri\_beh_i()|i:DP\bullet i \in dps\}$  end

We shall introduce the der\_up\_beh<sub>i</sub> and d\_tri\_beh<sub>i</sub> behaviours below.

## 7.1.5 The Revised Master Urban Planning Behaviour

We "take over", i.e., "copy", the basic structure and definition ("contents") of the urban planning function and behaviour from that of the *master* version. that is: master\_up\_beh\_2().

87 We think of zero, one or more derived plannings  $(der_up\_beh_1, der_up\_beh_2, ..., der_up\_beh_n)$  being initiated after some stage of *master* function, master\_up\\_fct, has concluded.

## value

- 77 master\_up\_beh\_2()  $\equiv$
- 73  $let (m_tri,m_qui) = (m_tri_ch?,m_qui_ch?) in$
- 74 let m\_qui' = master\_up\_fct(m\_tri)(m\_qui) in
- 75 m\_qui\_ch ! m\_qui';
- 79 if master\_satisfactory(m\_qui')
- 80 then skip
- 81' else der\_up() || master\_up\_beh\_2() end
- 77 end end

## 7.2 The Derived Urban Planning Functions

An important form of information for each derived urban planning function is the resumption, i.e., the "quintuplet" information from the master urban behaviour: mQui.

- 88 The new forms of information are: the derived urban planning auxiliary,  $dAUX_i$ , the derived urban planning requirements information,  $dREQ_i$ , as well as the derived urban planning plans,  $dPLA_i$ , and their ancillary information,  $dANC_i$ .
- 89 The primary arguments for the derived urban planning function, master\_up\_fct, is therefore a "quintuplet", d\_qui:dQUI, of a master triplet, m\_tri:mTRI, and the pair of the derived urban planning auxiliary information,  $d_{aux_i}:dAUX_i$ , and the derived urban planning requirements,  $d_{req_i}:dREQ_i$ .

The result of derived urban planning function,  $der_up_fct_i$ , as for the master urban planning function, master\_up\_fct,

- 90 is that of a "quintuplet", also referred to as a resumption,  $dQUI_i$ , of the primary arguments, b\_tri:bTRI, and
- 91 the result, a pair of a derived plan,  $d_pla_i$ , and derived ancillaries,  $d_anc_i$ .

- 92 As for the master urban planning function, master\_up\_fct, it has a secondary, derived "quintuplet" argument (which, as for master\_up\_fct, helps "kick-start" urban planning). This second argument is the result of a previous application of the der\_up\_fct<sub>i</sub>.
- 93 The derived urban planning function  $der_up_fct_i$  signature is therefore that of a function from a triplet of a most recent master "quintuplet", derived urban planning auxiliary and derived urban planning requirements information to functions from derived "quintuplet" arguments to derived "quintuplet" results.
- 94 The triplet argument,  $d_tri_i$ , and the first part of the result, also a triplet,  $d_tri_i$ , are the same.
- 95 The derived urban planning function  $\operatorname{der}_{\operatorname{up}}\operatorname{fct}_i$  is further characterised by a predicate,  $\mathcal{P}_{\operatorname{der}_i}$ , which we leave further undefined.

type

```
88 dAUX<sub>1</sub>, dAUX<sub>2</sub>, ..., dAUX<sub>n</sub>
88 dREQ<sub>1</sub>, dREQ<sub>2</sub>, ..., dREQ<sub>n</sub>
      dPLA_1, dPLA_2, ..., dPLA_n
88
     dANC_1, dANC_2, ..., dANC_n
88
      dTRI_i = mQUI \times dAUX_i \times dREQ_i
89
                                                           [i:DP•i∈dups]
      dRES_i = dPLA_i \times dANC_i
                                                           [i:DP•i∈dups
91
90 dQUI_i = dTRI_i \times dRES_i
                                                           [i:DP•i∈dups]
value
92
      der_up_fct<sub>i</sub>: dTRI<sub>i</sub> \rightarrow dQUI<sub>i</sub>m \rightarrow dQUI<sub>i</sub> i:DP
      der_up_fct_i(d_tri_i)(d_qui_i) as (d_tri_i', d_res_i)
93
           d_{tri_i} = d_{tri'_i} \wedge
94
           \mathcal{P}_{\mathsf{der}_i}(\mathsf{d\_tri}'_i,\mathsf{d\_res}_i)
95
```

95  $\mathcal{P}_{der_i}$ : dTRI<sub>i</sub> × dRES<sub>i</sub>  $\rightarrow$  Bool

## 7.3 The Derived Urban Planning "Oracle" Behaviour

- 96 We introduce the (indexed) type,  $dPAIR_i$ , of a *pair* of indexed derived auxiliaries and indexed derived requirements.
- 97 And we need an array channel that communicates the master quintuplet from the master quintuplet repository to an indexed derived triplet behaviour.

The  $d\_tri\_beh_i$  oracle evolves around:

- 98 the most recent dpair; it inputs master quintuplets over the master quintuplet repository to derived triplet oracle channel; and it outputs a triplet,  $dTRI_i$ , to the drived urban planning behaviour.
- 99 The d\_tri\_beh<sub>i</sub> behaviour "cycles" between forming (internal non-deterministically) a suitable, a fit, "next" dpair which it combines,
- 100 mq\_dt\_ch[i]? offers to the derived urban planning behaviour
- 101 whereupon it resumes being an oracle.
- 102 We leave the definition of *fit*ness of *dpairs* open.

```
type

96 dPAIR<sub>i</sub> = dAUX<sub>i</sub> × dREQ<sub>i</sub> [i:DP•i∈dups]

channel

97 {mq_dt_ch[i]|i:DP}:mQUI

value

98 d_tri_beh<sub>i</sub>: dPAIR<sub>i</sub> → in mq_dt_ch[i] out d_tri_ch[i] Unit

98 d_tri_beh<sub>i</sub>(d_pair<sub>i</sub>) =

99 let d_pair'<sub>i</sub>:dPAIR<sub>i</sub> • d_fit_pair(d_pair<sub>i</sub>,d_pair'<sub>i</sub>) in

100 d_tri_ch[i] ! (mq_dt_ch[i]?,d_pair'<sub>i</sub>) ;

101 d_tri_beh<sub>i</sub>(d_pair'<sub>i</sub>) end
```

```
102 d_fit_pair: dPAIR<sub>i</sub> × dPAIR<sub>i</sub> → Bool
```

## 7.4 The Derived Urban Planning Behaviour

103 We think of zero, one or more derived plannings  $(der\_up\_beh_{i_1}, der\_up\_beh_{i_2}, \ldots, der\_up\_beh_{i_k})$  being initiated after some stage of the  $der\_up\_fct_i$  function has concluded.

## value

```
77
     der_up_beh<sub>i</sub>() \equiv
73
          let (d_{tri_i}, d_{qui_i}) = (d_{tri_ch[i]}, d_{qui_ch[i]}) in
74
          let d_qui' = der_up_fct_i(d_tri_i)(d_qui_i) in
81
          d_qui_ch[i] ! d_qui'_i;
79
          if der_qui_satisfactory<sub>i</sub>(d_qui'<sub>i</sub>)
77
              then skip
78,103
               else der_up() \parallel der_up_beh<sub>i</sub>() end
77
          end end
```

```
79 der_qui_satisfactory: dQUI \rightarrow Bool
```

## 7.5 The Derived Resumption Repository

## 7.5.1 The Consolidated Derived Resumption Map

104 The derived urban planning functions (and thus behaviours) operate, not on simple resumptions, as do the master urban planning functions (and behaviours), but on the aggregation of all derived functions' (etc.) "quintuplets", that is, an indexed set of "quintuplets" – modeled as a derived resumptions map.

## type

104 dQUIm = DP  $\overrightarrow{m}$  dQUI<sub>i</sub>

## 7.5.2 The Consolidated Derived Resumption Repository Channel

105 Communications between the individual derived urban planning behaviours and the consolidated derived resumption repository are via an indexed set of channels communicating derived resumptions maps.

## channel

105 {d\_qui\_ch[i]:dQUIm|i:DP•  $i \in dups$ }

#### 7.5.3 The Consolidated Derived Resumption Repository

106 The consolidated derived resumption repository behaviour either ([]) updates its state map with received individual derived resumptions, or offers the entire such state maps to whichever derived urban planning behaviour so requests.

## value

#### 7.5.4 Initial Consolidated Derived Urban Plannings

value

init\_d\_qui\_1:dQUI\_1, ..., init\_d\_qui\_n:dQUI\_n init\_d\_qui\_m:dQUIm = [  $d_1 \mapsto init_d_qui_1, ..., d_n \mapsto init_d_qui_n$  ]

#### 7.5.5 Initialisation of The Derived "Quintuplet" Oracle

As for master oracle and repository behaviours we initialise the derived "quintuplet" oracle:

der\_qui\_beh(init\_d\_qui\_m)

## 7.6 A Visual Rendition of Urban Planning Development

The urban planning project domain, when operating at "full speed", consists of the master urban planning behaviour (i.e., project), zero, one or more derived urban planning behaviours, each of the latter initiated by either the master urban planning project or a derived urban planning project. See Fig. 3 on the next page. The planning behaviours, both the master and the deriveds, invoke respective urban planning functions, and these produce, such as we have modeled them, "quintuplets" of information, which are deposited with respective "quintuplet" repository behaviours: the master "quintuplet" repository behaviour, and the derived "quintuplet" repository behaviour — which maintains these "quintuplets" for all (invoked and thus ongoing) derived urban planning projects. We kindly ask you to review Fig. 3. All you have to grasp is the fact that there is one master urban planning project, with its repository of master urban planning "quintuplets", and between 0 and n derived urban planning projects, with their shared (consolidated<sup>19</sup>), derived urban planning "quintuplets", Then there are the channels: the query (input) channels providing auxiliary and requirements information to both the one master urban planning project and the n derived urban planning projects; and the query/repository channels providing "quintuplet" aggregated information to the master urban planning project, as well as "quintuplet" aggregated information to the derived urban planning projects. Finally there is the "global" value representing the index set of derived urban planning indices, and the variable which holds the index set of derived urban planning indices of ongoing derived urban planning projects.

<sup>&</sup>lt;sup>19</sup>– into a map



Figure 3: An Urban Planning:

The Urban Space, o Urban Space Analysis and n+1 Urban Planning behaviours, **2 Repository, 'qui'**, behaviours, n+1 Oracle, 'tri', behaviours,

1 Variable behaviour, a 1 Global value and  $5 \times n + 2$  Channels
### 7.7 Revised Selection of Derived Urban Plannings

TO BE WRITTEN

# 7.8 The Urban Planning System

107 Finally we can define an urban planning development as a system of concurrent behaviours:

- the master urban planning behaviour,
- the master "quintuplet" repository and
- the derived and consolidate "quintuplet" repository

### value

```
107 up_sys: Unit → Unit
107 up_sys() = master_up_beh() || m_qui_beh(m_qui_init) || d_qui_beh(init_d_qui_m)
```

Recall that the derived urban planning behaviours as well as the derived triplet behaviours are started by the master as well as the derived urban planning behaviours.

# 8 Further Work

### 8.1 Reasoning About Deadlock, Starvation, Live-lock and Liveness

The current author is quite unhappy about the way in which he has defined the urban planning, oracle and repository behaviours. Such issues as which invariants are maintained across behaviours are not addressed. In fact, it seems to be good practice, following Dijkstra, Lamport and others, to formulate appropriate such invariants and only then "derive" behaviour definitions accordingly. In a rewrite of this research note, if ever, into a proper paper, the current author hopes to follow proper practices. He hopes to find younger talent to co-author this effort.

### 8.2 **Document Handling**

I may appear odd to the reader that I now turn to document handling. One central aspect of urban planning, strange, perhaps, to the reader, is that of handling the "zillions upon zillions" of documents that enter into and accrue from urban planning. If handling of these documents is not done properly a true nightmare will occur. So we shall briefly examine the urban planning document situation! From that we conclude that we must first try understand:

### • What do we mean by a document?

#### 8.2.1 Information Categories

Urban planning consumes information, most likely in the form of documents and produces urban planning documents, i.e., plans — referred to in Sects. 6–7 as information ("contained" in triplets and in quintuplets). We remind the reader of the types of these documents.

type	е	46 $bTRI = bGEO \times bAUX \times bREQ$
31	bGEO	47 $bRES = bPLA \times bANC$
42	bAUX	48 $bQUI = bTRI \times bRES$
43	bREQ	88 dAUX <sub>1</sub> , dAUX <sub>2</sub> ,, dAUX <sub>n</sub>
44	bPLA	88 dREQ <sub>1</sub> , dREQ <sub>2</sub> ,, dREQ <sub>n</sub>
45	bANC	88 dPLA <sub>1</sub> , dPLA <sub>2</sub> ,, dPLA <sub>n</sub>

88	$dANC_1$ , $dANC_2$ ,, $dANC_n$	91 dRES	$S_i = dPLA_i  imes dANC_i$	[i:DP ● i∈dups]
89	$dTRI_i = bQUI \times dAUX_i \times dREQ_i [i:DP \bullet i \in dups]$	90 dQU	$I_i = dTRI_i \times dRES_i$	[i:DP • i∈dups]
		104 dQl	$JIm = DP \implies dQUI_i$	[i:DP • i∈dups]

### 8.2.2 Urban Planning Documents

The urban planning functions and the urban planning behaviours, including both the **base** and the n derived variants, rely on documents. These documents are **created**, **edited**, **read**, **copied**, and, eventually, **shredded** by urban-planners. Editing documents result in new versions of "the same" document. While a document is being **edited** or **read** we think of it as not being **accessible** to other urban-planners. If urban-planners need to read a latest version of a document while that version is subject to editing by another urban planner, copies must first be made, before editing, one for each "needy" reader. Once, editing has and readings have finished, the "reader" copies need, or can, be shredded.

### 8.2.3 A Document Handling System

In Appendix A, [5], we sketch a document handling system domain. That is, not a document handling software system, not even requirements for a document handling software system, but just a description which, in essence, models documents and urban planners' actions on documents. (The urban planners are referred to as document handlers.) The description further models two 'aggregate' notions: one of 'handler management', and one of 'document archive'. Both seem necessary in order to "sort out" the granting of document access rights (that is, permissions to perform operations on documents), and the creation and shredding of documents, and in order to avoid dead-locks in access to and handling of documents.

# 8.3 Validation and Verification (V&V)

By **validation** of a document we shall mean: the primarily informal and social process of checking that the document description meets customer expectations.

Validation serves to get the right product.

By **verification** of a document we shall mean: the primarily formal, i.e., mathematical process of checking, testing and formal prooof that the model, which the document description entails, satisfies a number of properties.

Verification serves to get the product right.

By validation of the urban planning model of this document we shall understand the social process of explaining the model to urban planning stakeholders, to obtain their reaction, and to possibly change the model according to stakeholder objections.

By **verification of the urban planning model** of this document we shall understand the formal process, based on formalisations (cf. Sect. ?? on Page ??) of the argument and result types of the description, of testing, model checking and formally proving properties of the model.

MORE TO COME

### 8.4 Urban Planning Project Management

In this research note we have focused on the urban planning project behaviours, their interactions, and their information "passing". Usually publications about urban planning: research papers, technical papers, survey papers, etcetera, focus on specific "functions". In this research note we do not. Such "functions" are, in this note, embodied in

- b\_tri\_fit (formula Item 63 on Page 28),
  base\_up\_fct (formula Item 74 on Page 29),
  der\_satisfactory<sub>i</sub> (formula Item 79 on Page 30)
  and
- base\_satisfactory (formula Item 79 on Page 30),
  der\_up\_fct<sub>i</sub> (formula Item 92 on Page 33).

We focus instead on what we can say about the domain of urban planning: the fact, or the possibility, that an initial, a core, here referred to as a base, urban planning effort (i.e., project, hence behaviour) can "spew off", generate, a number of (derived, i.e., in some sense subsidiary), more specialised, urban planning projects.

#### 8.4.1 Urban Planning Projects

We think of a comprehensive urban planning project as carried out by urban planners. As is evident from the model given in Sects. 6-7, the project consists of one base urban planning project and up to n derived urban planning projects. The urban planners involved in these projects are professionals in the areas of planning:

<ul> <li>base urban planning issues:</li> </ul>	$\circledast$ residential and shopping,	∞ water,
⊗ geodesy,	apartment buildings,	⊗ waste,
geotechniques,		
meteorology,	recreational,	• societal infrastructures:
• base urban plans:		∞ health care,
⊗ cartography,	<ul> <li>technological infrastructures:</li> </ul>	
cadestral matters,		∞ police,
⊗ zoning;	electricity,	
<ul> <li>derived urban planning issues:</li> </ul>	telecommunications,	
	⊗ gas,	• etcetera, etcetera, etcetera

To anyone with any experience in getting such diverse groups and individuals of highly skilled professionals to work together it is obvious that some form of management is required. The term 'comprehensive' was mentioned above. It is meant to express that the comprehensive urban planning project is the only one "dealing" with a given geographic area, and that no other urban planning projects "infringe" upon it, that is, "deal" with sub-areas of that given geographic area.

#### 8.4.2 Strategic, Tactical and Operational Management

We can distinguish between

- strategic,
- tactical and
- operational

management.

**Project Resources** But first we need take a look at the **resources** that management is charged with:

Version 2

- the urban planners, i.e., humans,
- time,

- office space,
- support technologies: computing etc.,

• finances,

• etcetera.

**Strategic Management** By **strategic management** we shall understand the analysis and decisions of, and concerning, scarce resources: people (skills), time, monies: their deployment and trade-offs.

**Tactical Management** By **tactical management** we shall understand the analysis and decisions with respect to budget and time plans, and the monitoring and control of serially reusable resources: office space, computing.

**Operational Management** By **operational management** we shall understand the monitoring and control of the enactment, progress and completion of individual deliverables, i.e., documents, the quality (adherence to "standards", fulfillment of expectations, etc.) of these documents, and the day-to-day human relations.

# 8.4.3 Urban Planning Management

The above (strategic, tactical & operational management) translates, in the context of urban planning, into:

TO BE WRITTEN

# 9 Conclusion

### TO BE WRITTEN

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# A A Document System

# A.1 Introduction

We analyse a notion of documents. Documents such as they occur in daily life. What can we say about documents – regardless of whether we can actually provide compelling evidence for what we say! That is: we model documents, not as electronic entities — which they are becoming, more-and-more, but as if they were manifest entities. When we, for example, say that "this document was recently edited by such-and-such and the changes of that editing with respect to the text before is such-and-such", then we can, of course, always claim so, even if it may be difficult or even impossible to verify the claim. It is a fact, although maybe not demonstrably so, that there was a version of any document before an edit of that document. It is a fact that some handler did the editing. It is a fact that the editing took place at (or in) exactly such-and-such a time (interval), etc. We model such facts.

### A.2 A Document Systems Description

This research note unravels its analysis  $\&^{20}$  description in stages.

# A.3 A System for Managing, Archiving and Handling Documents

The title of this section: A System for Managing, Archiving and Handling Documents immediately reveals the major concepts: That we are dealing with a system that manages, archives and handles documents. So what do we mean by managing, archiving and handling documents, and by documents? We give an ultra short survey. The survey relies on your prior knowledge of what you think documents are! Management decides<sup>21</sup> to direct handlers to work on documents. Management first directs the document archive to create documents. The document archive creates documents, as requested by management, and informs management of the unique document identifiers (by means of which handlers can handle these documents). Management then grants its designated handler(s) access rights to documents, these access rights enable handlers to edit, read and copy documents. The handlers' editing and reading of documents is accomplished by the handlers "working directly" with the documents (i.e., synchronising and communicating with document behaviours). The handlers' copying of documents is accomplished by the handlers requesting management, in collaboration with the archive behaviour, to do so.

### A.4 Principal Endurants

By an endurant we shall understand "an entity that can be observed or conceived and described as a "complete thing" at no matter which given snapshot of time." Were we to "freeze" time we would still be able to observe the entire endurant. This characterisation of what we mean by an 'endurant' is from [6, Manifest Domains: Analysis & Description]. We begin by identifying the principal endurants.

108 From document handling systems one can observe aggregates of handlers and documents.

We shall refer to 'aggregates of handlers' by M, for management, and to 'aggregates of documents' by A, for archive.

109 From aggregates of handlers (i.e., M) we can observe sets of handlers (i.e., H).

110 From aggregates of documents (i.e., A) we can observe sets of documents (i.e., D).

<sup>&</sup>lt;sup>20</sup>We use the logogram & between two terms, A & B, when we mean to express one meaning.

 $<sup>^{21}</sup>$ How these decisions come about is not shown in this research note – as it has nothing to do with the essence of document handling, but, perhaps, with 'management'.

type 108 S, M, A value 108 obs\_M:  $S \rightarrow M$ 108 obs\_A:  $S \rightarrow A$ type 109 H, Hs = H-set 110 D, Ds = D-set value 109 obs\_Hs:  $M \rightarrow Hs$ 110 obs\_Ds:  $A \rightarrow Ds$ 

# A.5 Unique Identifiers

The notion of unique identifiers is treated, at length, in [6, Manifest Domains: Analysis & Description].

111 We associate unique identifiers with aggregate, handler and document endurants.

112 These can be observed from respective parts<sup>22</sup>.

type 111 MI<sup>23</sup>, AI<sup>24</sup>, HI, DI value 112 uid\_MI<sup>25</sup>:  $M \rightarrow MI$ 112 uid\_AI<sup>26</sup>:  $A \rightarrow AI$ 112 uid\_HI:  $H \rightarrow HI$ 112 uid\_DI:  $D \rightarrow DI$ 

As reasoned in [6, Manifest Domains: Analysis & Description], the unique identifiers of endurant parts are indeed unique: No two parts, whether composite, as are the aggregates, or atomic, as are handlers and documents, can have the same unique identifiers.

### A.6 Documents: A First View

A document is a written, drawn, presented, or memorialized representation of thought. The word originates from the Latin *documentum*, which denotes a "teaching" or "lesson".<sup>27</sup> We shall, for this research note, take a document in its written and/or drawn form. In this section we shall survey the concept a documents.

### A.6.1 Document Identifiers

Documents have *unique identifiers*. If two or more documents have the same document identifier then they are the same, one (and not two or more) document(s).

 $<sup>^{22}</sup>$ [6, Manifest Domains: Analysis & Description] explains how 'parts' are the discrete endurants with which we associate the full complement of properties: unique identifiers, mereology and attributes.

 $<sup>^{23}</sup>$ We shall not, in this research note, make use of the (one and only) management identifier.

 $<sup>^{24}\</sup>mathrm{We}$  shall not, in this research note, make use of the (one and only) archive identifier.

 $<sup>^{25}\</sup>mathrm{Cf.}$  Footnote 23: hence we shall not be using the uid\_MI observer.

<sup>&</sup>lt;sup>26</sup>Cf. Footnote 24: hence we shall not be using the uid\_Al observer.

<sup>&</sup>lt;sup>27</sup>From: https://en.wikipedia.org/wiki/Document

#### A.6.2 Document Descriptors

With documents we associate *document descriptors*. We do not here stipulate what document descriptors are other than saying that when a document is **created** it is provided with a descriptor and this descriptor "remains" with the document and never changes value. In other words, it is a static attribute.<sup>28</sup> We do, however, include, in document descriptors, that the document they describe was initially based on a set of zero, one or more documents – identified by their unique identifiers.

#### A.6.3 Document Annotations

With documents we also associate document annotations. By a document annotation we mean a programmable attribute, that is, an attribute which can be 'augmented' by document handlers. We think of document annotations as "incremental", that is, as "adding" notes "on top of" previous notes. Thus we shall model document annotations as a repository: notes are added, i.e., annotations are augmented, previous notes are not edited, and no notes are deleted. We suggest that notes be time-stamped. The notes (of annotations) may be such which record handlers work on documents. Examples could be: "January 5, 2018: 09:42 am: This is version V.", "This document was released on January 5, 2018: 09:42 am.", "January 5, 2018: 09:42 am: Section X.Y.Z of version III was deleted.", "January 5, 2018: 09:42 am: References to documents doc<sub>i</sub> and doc<sub>j</sub> are inserted on Pages p and q, respectively." and "January 5, 2018: 09:42 am: Final release."

### A.6.4 Document Contents: Text/Graphics

The main idea of a document, to us, is the *written* (i.e., text) and/or *drawn* (i.e., graphics) contents. We do not characterise any format for this contents. We may wish to insert, in the contents, references to locations in the contents of other documents. But, for now, we shall not go into such details. The main operations on documents, to us, are concerned with: their **creation**, **editing**, **reading**, **copying** and **shredding**. The **editing** and **reading** operations are mainly concerned with document annotations and text/graphics.

### A.6.5 Document Histories

So documents are **create**d, **edit**ed, **read**, **copied** and **shred**ed. These operations are initiated by the management (**create**), by the archive (**create**), and by handlers (**edit**, **read**, **copy**), and at specific times.

### A.6.6 A Summary of Document Attributes

- 113 As separate attributes of documents we have document descriptors, document annotations, document contents and document histories.
- 114 Document annotations are lists of document notes.
- 115 Document histories are lists of time-stamped document operation designators.
- 116 A document operation designator is either a create, or an edit, or a read, or a copy, or a shred designator.
- 117 A create designator identifies

 $<sup>^{28}</sup>$ You may think of a document descriptor as giving the document a title; perhaps one or more authors; perhaps a physical address (of, for example, these authors); an initial date; as expressing whether the document is a research, or a technical report, or other; who is issuing the document (a public institution, a private firm, an individual citizen, or other); etc.

- a a handler and a time (at which the create request first arose), and presents
- b elements for constructing a document descriptor, one which
  - i besides some further undefined information
  - ii refers to a set of documents (i.e., embeds reference to their unique identifiers),
- c a (first) document note, and
- d an empty document contents.
- 118 An edit designator identifies a handler, a time, and specifies a pair of edit/undo functions.
- 119 A read designator identifies a handler.
- 120 A copy designator identifies a handler, a time, the document to be copied (by its unique identifier, and a document note to be inserted in both the master and the copy document.
- 121 A shred designator identifies a handler.
- 122 An edit function takes a triple of a document annotation, a document note and document contents and yields a pair of a document annotation and a document contents.
- 123 An undo function takes a pair of a document note and document contents and yields a triple of a document annotation, a document note and a document contents.
- 124 Proper pairs of (edit,undo) functions satisfy some inverse relation.

There is, of course, no need, in any document history, to identify the identifier of that document.

```
type
113
       DD, DA, DC, DH
value
113
      attr_DD: D \rightarrow DD
113
       attr_DA: D \rightarrow DA
       attr_DC: D \rightarrow DC
113
       attr_DH: D \rightarrow DH
113
type
      DA = DN^*
114
115
       DH = (TIME \times DO)^*
       DO == Crea | Edit | Read | Copy | Shre
116
117 Crea :: (HI × TIME) × (DI-set × Info) × DN × {|''empty_DC''|}
117(b)i Info = ...
value
         embed_DIs_in_DD: DI-set \times Info \rightarrow DD
117(b)ii
axiom
117d "empty_DC" \in DC
type
118 Edit :: (HI \times TIME) \times (EDIT \times UNDO)
119 Read :: (HI \times TIME) \times DI
120 Copy :: (HI \times TIME) \times DI \times DN
121
      Shre :: (HI \times TIME) \times DI
122 EDIT = (DA \times DN \times DC) \rightarrow (DA \times DC)
123 UNDO = (DA \times DC) \rightarrow (DA \times DN \times DC)
axiom
```

 $\begin{array}{rll} 124 & \forall \mbox{ mkEdit}(\_,(e,u)):Edit \bullet \\ 124 & \forall \mbox{ (da,dn,dc)}:(DA \times DN \times DC) \bullet \\ 124 & u(e(da,dn,dc))=(da,dn,dc) \end{array}$ 

# A.7 Behaviours: An Informal, First View

In [6, Manifest Domains: Analysis & Description] we show that we can associate behaviours with parts, where parts are such discrete endurants for which we choose to model all its observable properties: unique identifiers, mereology and attributes, and where behaviours are sequences of actions, events and behaviours.

- The overall document handler system behaviour can be expressed in terms of the parallel composition of the behaviours
  - 125 of the system core behaviour,
  - 126 of the handler aggregate (the management) behaviour
  - 127 and the document aggregate (the archive) behaviour,
  - with the (distributed) parallel composition of
  - 128 all the behaviours of handlers and,
  - the (distributed) parallel composition of
  - 129 at any one time, zero, one or more behaviours of documents.
- To express the latter
  - 130 we need introduce two "global" values: an indefinite set of handler identifiers and an indefinite set of document identifiers.

### value

```
130 his:HI-set, dis:DI-set
```

```
125 sys(...)
```

- 126 || mgtm(...)
- 127 || arch(...)
- 128  $|| || \{ hdlr_i(...) | i: Hl \bullet i \in his \}$
- 129  $|| || \{ docu_i(dd)(da, dc, dh) | i: DI \bullet i \in dis \}$

For now we leave undefined the arguments, (...) etc., of these behaviours. The arguments of the document behaviour, (dd)(da,dc,dh), are the static, respectively the three programmable (i.e., dynamic) attributes: document descriptor, document annotation, document contents and document history. The above expressions, Items 126–129, do not define anything, they can be said to be "snapshots" of a "behaviour state". Initially there are no document behaviours,  $docu_i(dd)(da,dc,dh)$ , Item 129. Document behaviours are "started" by the archive behaviour (on behalf of the management and the handler behaviours). Other than mentioning the system (core) behaviour we shall not model that behaviour further.

### A.8 Channels, A First View

Channels are means for behaviours to synchronise and communicate values (such as unique identifiers, mereologies and attributes).

- 131 The management behaviour, mgtm, need to (synchronise and) communicate with the archive behaviour, arch, in order, for the management behaviour, to request the archive behaviour
  - to **create** (ab initio or due to **copy**ing)
  - or **shred** document behaviours, docu<sub>j</sub>,

and for the archive behaviour

• to inform the management behaviour of the identity of the document( behaviour)s that it has created.

### channel

131 mgtm\_arch\_ch:MA

- 132 The management behaviour, mgtm, need to (synchronise and) communicate with all handler behaviours,  $hdlr_i$  and they, in turn, to (synchronised) communicate with the handler management behaviour, mgtm. The management behaviour need to do so in order
  - to inform a handler behaviour that it is granted access rights to a specific document, subsequently these access rights may be modified, including revoked.

#### channel

132 {mgtm\_hdlr\_ch[i]:MH|i:Hl•i  $\in$  his}

133 The document archive behaviour, arch, need (synchronise and) communicate with all document behaviours,  $docu_j$  and they, in turn, to (synchronise and) communicate with the archive behaviour, arch.

### channel

133 {arch\_docu\_ch[j]:AD|h:DI•j  $\in$  dis}

134 Handler behaviours,  $\mathsf{hdlr}_i$ , need (synchronise and) communicate with all the document behaviours,  $\mathsf{docu}_j$ , with which it has operational allowance to so do so<sup>29</sup>, and document behaviours,  $\mathsf{docu}_j$ , need (synchronise and) communicate with potentially all handler behaviours,  $\mathsf{hdlr}_i$ , namely those handler behaviours,  $\mathsf{hdlr}_i$  with which they have ("earlier" synchronised and) communicated.

### channel

134 {hdlr\_docu\_ch[i,j]:HD|i:HI,j:DI•i  $\in$  his $\land j \in$  dis}

135 At present we leave undefined the type of messages that are communicated.

type 135 MA, MH, AD, HD

 $<sup>^{29}\</sup>mathrm{The}$  notion of operational allowance will be explained below.



Figure 4: An Informal Snapshot of System Behaviours

#### A.9 An Informal Graphical System Rendition

Figure 4 is an informal rendition of the "state" of a number of behaviours: a single management behaviour, a single archive behaviour, a fixed number,  $n_h$ , of one or more handler behaviours, and a variable, initially zero number of document behaviours, with a maximum of these being  $n_d$ . The figure also indicates, again rather informally, the channels between these behaviours: one channel between the management and the archive behaviours;  $n_h$  channels ( $n_h$  is, again, informally indicated) between the management behaviour and the  $n_h$  handler behaviours;  $n_d$  channels ( $n_d$  is, again, informally indicated) between the archive behaviour and the  $n_d$  document behaviours; and  $n_h \times n_d$  channels ( $n_d \times n_d$  is, again, informally indicated) between the  $n_h$  handler behaviours and the  $n_d$  document behaviours

# A.10 Behaviour Signatures

- 136 The mgtm behaviour (synchronises and) communicates with the archive behaviour and with all of the handler behaviours,  $hdlr_i$ .
- 137 The archive behaviour (synchronises and) communicates with the mgtm behaviour and with all of the document behaviours,  $docu_j$ .
- 138 The signature of the generic handler behaviours,  $\mathsf{hdlr}_i$  expresses that they [occasionally] receive "orders" from management, and otherwise [regularly] interacts with document behaviours.
- 139 The signature of the generic document behaviours,  $docu_j$  expresses that they [occasionally] receive "orders" from the archive behaviour and that they [regularly] interacts with handler behaviours.

### value

136 mgtm: ...  $\rightarrow$  in,out mgtm\_arch\_ch, {mgtm\_hdlr\_ch[i]|i:Hl•i \in his} Unit

- 137 arch: ...  $\rightarrow$  in,out mgtm\_arch\_ch, {arch\_docu\_ch[j]|j:Dl•j \in dis} Unit
- 138  $hdlr_i: ... \rightarrow in mgtm_hdlr_ch[i], in,out {hdlr_docu_ch[i,j]|j:Dl•j\in dis} Unit$
- 139 docu<sub>j</sub>: ...  $\rightarrow$  in mgtm\_arch\_ch, in,out {hdlr\_docu\_ch[i,j]|i:Hl•i  $\in$  his} Unit

## A.11 Time

#### A.11.1 Time and Time Intervals: Types and Functions

- 140 We postulate a notion of time, one that covers both a calendar date (from before Christ up till now and beyond). But we do not specify any concrete type (i.e., format such as: YY:MM:DD, HH:MM:SS).
- 141 And we postulate a notion of (signed) time interval between two times (say: ±YY:MM:DD:HH:MM:SS).
- 142 Then we postulate some operations on time: Adding a time interval to a time obtaining a time; subtracting one time from another time obtaining a time interval, multiplying a time interval with a natural number; etc.
- 143 And we postulate some relations between times and between time intervals.

type 140 TIME 141 TIME\_INTERVAL value 142 add: TIME\_INTERVAL × TIME  $\rightarrow$  TIME 142 sub: TIME × TIME  $\rightarrow$  TIME\_INTERVAL 142 mpy: TIM\_INTERVALE × Nat  $\rightarrow$  TIME\_INTERVAL 143 <,<,=,=, $\neq$ ,>,>: ((TIME×TIME)|(TIME\_INTERVAL×TIME\_INTERVAL))  $\rightarrow$  Bool

# A.11.2 A Time Behaviour and a Time Channel

- 144 We postulate a[n "ongoing"] time behaviour: it either keeps being a time behaviour with unchanged time, t, or – internally non-deterministically – chooses being a time behaviour with a time interval incremented time, t+ti, or – internally non-deterministically – chooses to [first] offer its time on a [global] channel, time\_ch, then resumes being a time behaviour with unchanged time., t
- 145 The time interval increment, ti, is likewise internally non-deterministically chosen. We would assume that the increment is "infinitesimally small", but there is no need to specify so.
- 146 We also postulate a channel, time\_ch, on which the time behaviour offers time values to whoever so requests.

#### value

```
144 time: TIME \rightarrow time_ch TIME Unit

144 time(t) \equiv (time(t) || time(t+ti) || time_ch!t ; time(t))

145 ti:TIME_INTERVAL ...

channel

146 time_ch:TIME
```

# A.11.3 An Informal RSL Construct

The formal-looking specifications of this report appear in the style of the RAISE [12] Specification Language, RSL [11]. We shall be making use of an informal language construct:

• wait ti.

wait is a keyword; ti designates a time interval. A typical use of the wait construct is:

• ... *ptA* ; **wait** ti; *ptB* ; ...

If at specification text point ptA we may assert that time is t, then at specification text point ptB we can assert that time is t+ti.

# A.12 Behaviour "States"

We recall that the endurant parts, Management, Archive, Handlers, and Documents, have properties in the form of unique identifiers, mereologies and attributes. We shall not, in this research note, deal with possible mereologies of these endurants. In this section we shall discuss the endurant attributes of mgtm (management), arch (archive), hdlrs (handlers), and docus (documents). Together the values of these properties, notably the attributes, constitute states – and, since we associate behaviours with these endurants, we can refer to these states also a behaviour states. Some attributes are static, i.e., their value never changes. Other attributes are dynamic.<sup>30</sup> Document handling systems are rather conceptual, i.e., abstract in nature. The dynamic attributes, therefore, in this modeling "exercise", are constrained to just the programmable attributes. Programmable attributes are those whose value is set by "their" behaviour. For a behaviour  $\beta$  we shall show the static attributes as one set of parameters and the programmable attributes as another set of parameters.

value  $\beta$ : Static  $\rightarrow$  Program  $\rightarrow$  ... Unit

- 147 For the management endurant/behaviour we focus on one programmable attribute. The management behaviour needs keep track of all the handlers it is charged with, and for each of these which zero, one or more documents they have been granted access to (cf. Sect. A.13.3 on Page 52). Initially that management directory lists a number of handlers, by their identifiers, but with no granted documents.
- 148 For the archive behaviour we similarly focus on one programmable attribute. The archive behaviour needs keep track of all the documents it has used (i.e., created), those that are available (and not yet used), and of those it has shredded. Initially all these three archive directory sets are empty.
- 149 For the handler behaviour we similarly focus on one programmable attribute. The handler behaviour needs keep track of all the documents it has been charged with and its access rights to these.
- 150 Document attributes we mentioned above, cf. Items 113–116.

```
type
```

147 MDIR = HI  $\overrightarrow{m}$  (DI  $\overrightarrow{m}$  ANm-set) 148 ADIR = avail:DI-set × used:DI-set × gone:DI-set 149 HDIR = DI  $\overrightarrow{m}$  ANm-set 150 SDATR = DD, PDATR = DA × DC × DH axiom 148  $\forall$  (avail,used,gone):ADIR • avail  $\cap$  used = {}  $\land$  gone  $\subseteq$  used

We can now "complete" the behaviour signatures. We omit, for now, static attributes.

 $<sup>^{30}</sup>$ We refer to Sect. 3.4 of [6], and in particular its subsection 3.4.4.

value

136 mgtm: MDIR  $\rightarrow$  in,out mgtm\_arch\_ch, {mgtm\_hdlr\_ch[i]|i:Hl•i  $\in$  his} Unit 137 arch: ADIR  $\rightarrow$  in,out mgtm\_arch\_ch, {arch\_docu\_ch[j]|j:Dl•j  $\in$  dis} Unit 138 hdlr<sub>i</sub>: HDIR  $\rightarrow$  in mgtm\_hdlr\_ch[i], in,out {hdlr\_docu\_ch[i,j]|j:Dl•j $\in$ dis} Unit 139 docu<sub>i</sub>: SDATR  $\rightarrow$  PDATR  $\rightarrow$  in mgtm\_arch\_ch, in,out {hdlr\_docu\_ch[i,j]|i:Hl•i  $\in$  his} Unit

# A.13 Inter-Behaviour Messages

Documents are not "fixed, innate" entities. They embody a "history", they have a "past". Somehow or other they "carry a trace of all the "things" that have happened/occurred to them. And, to us, these things are the manipulations that management, via the archive and handlers perform on documents.

### A.13.1 Management Messages with Respect to the Archive

- 151 Management **create** documents. It does so by requesting the archive behaviour to allocate a document identifier and initialize the document "state" and start a document behaviour, with initial information, cf. Item 117 on Page 44:
  - a the identity of the initial handler of the document to be created,
  - b the time at wich the request is being made,
  - c a document descriptor which embodies a (finite) set of zero or more (used) document identifiers (dis),
  - d a document annotation note dn, and
  - e an initial, i.e., "empty" contents, "empty\_DC".

#### type

- 117. Crea :: (HI × TIME) × (DI-set × Info) × DN × {| "empty\_DC"} [cf. formula ltem 117, Page 45]
- 152 The management behaviour passes on to the archive behaviour, requests that it accepts from handlers behaviours, for the copying of document:

152 Copy ::  $DI \times HI \times TIME \times DN$  [cf. Item 162 on Page 53]

153 Management schreds documents by informing the archive behaviour to do so.

type 153 Shred :: TIME  $\times$  DI

# A.13.2 Management Messages with Respect to Handlers

154 Upon receiving, from the archive behaviour, the "feedback" the identifier of the created document (behaviour):

### type

Towards a Formal Understanding of Urban Planning

154. Create\_Reply :: NewDocID(di:DI)

Version 2

155 the management behaviour decides to **grant** access rights, **acrs**:ACRS<sup>31</sup>, to a document handler, hi:HI.

#### A.13.3 Document Access Rights

Implicit in the above is a notion of document access rights.

- 156 By document access rights we mean a set of action names.
- 157 By an action name we mean such tokens that indicate either of the document handler operations indicate above.

type

156 ACRS = ANm-set

157  $ANm = \{|''edit'', ''read'', ''copy''|\}$ 

#### A.13.4 Archive Messages with Respect to Management

To create a document management provides the archive with some initial information. The archive behaviour selects a document identifier that has not been used before.

158 The archive behaviour informs the management behaviour of the identifier of the created document.

type 158 NewDocID :: DI

# A.13.5 Archive Message with Respect to Documents

159 To shred a document the archive behaviour must access the designated document in order to **stop** it. No "message", other than a symbolic "**stop**", need be communicated to the document behaviour.

**type** 159 Shred :: {|"stop"|}

### A.13.6 Handler Messages with Respect to Documents

Handlers, generically referred to by  $\mathsf{hdlr}_i$ , may perform the following operations on documents: edit, read and copy. (Management, via the archive behaviour, creates and shreds documents.)

160 To perform an **edit** action handler  $hdlr_i$  must provide the following:

• the document identity – in the form of a (i:HI,j:DI) channel hdlr\_docu\_ch index value,

 $<sup>^{31}\</sup>mathrm{For}$  the concept of access rights see Sect. A.13.3.

- the handler identity, i,
- the time of the edit request,
- and a pair of functions: one which performs the editing and one which un-does it !

type

160 Edit ::  $DI \times HI \times TIME \times (EDIT \times UNDO)$ 

161 To perform a **read** action handler  $hdlr_i$  must provide the following information:

- the document identity in the form of a di:DI channel hdlr\_docu\_ch index value,
- the handler identity and
- the time of the read request.

```
type
```

```
161 Read :: DI \times HI \times TIME
```

#### A.13.7 Handler Messages with Respect to Management

- 162 To perform a **copy** action, a handler,  $hdlr_i$ , must provide the following information to the management behaviour, mgtm:
  - the document identity,
  - the handler identity in the form of an hi:HI channel mgtm\_hdlr\_ch index value,
  - the time of the copy request, and
  - a document note (to be affixed both the master and the copy documents).

162 Copy ::  $DI \times HI \times TIME \times DN$  [cf. Item 152 on Page 51]

How the handler, the management, the archive and the "named other" handlers then enact the copying, etc., will be outlined later.

### A.13.8 A Summary of Behaviour Interactions

Figure 5 on the following page summarises the sources, **out**, resp. !, and the targets, **in**, resp. ?, of the messages covered in the previous sections.

# A.14 A General Discussion of Handler and Document Interactions

We think of documents being manifest. Either a document is in paper form, or it is in electronic form. In paper form we think of a document as being in only one – and exactly one – physical location. In electronic form a document is also in only one – and exactly one – physical location. No two handlers can access the same document at the same time or in overlapping time intervals. If your conventional thinking makes you think that two or more handlers can, for example, read the same document "at the same time", then, in fact, they are reading either a master and a copy of that master, or they are reading two copies of a common master.



Figure 5: A Summary of Behaviour Interactions

# A.15 Channels: A Final View

We can now summarize the types of the various channel messages first referred to in Items 131, 132, 133 and 134.

### type

- 131 MA = Create (Item 151 on Page 51) | Shred (Item 151d on Page 51) | NewDoclD (Item 158 on Page 52)
- 132 MH = Grant (Item 151c on Page 51) | Copy (Item 162 on the previous page) |
- 133 AD = Shred (Item 159 on Page 52)
- 134 HD = Edit (Item 160 on Page 52) | Read (Item 161 on the preceding page) | Copy (Item 162 on the previous page)

### A.16 An Informal Summary of Behaviours

# A.16.1 The Create Behaviour: Left Fig. 6 on the facing page

- 163 [1] The management behaviour, at its own volition, initiates a create document behaviour. It does so by offering a create document message to the archive behaviour.
  - a [1.1] That message contains a meaningful document descriptor,
  - b [1.2] an initial document annotation,
  - c [1.3] an "empty" document contents and
  - d [1.4] a single element document history.

(We refer to Sect. A.13.1 on Page 51, Items 151–151e.)

- 164 [2] The archive behaviour offers to accept that management message. It then selects an available document identifier (here shown as k), henceforth marking k as used.
- 165 [3] The archive behaviour then "spawns off" document behaviour  $docu_k$  here shown by the "dash–dotted" rounded edge square.
- 166 [4] The archive behaviour then offers the document identifier k message to the management behaviour.

(We refer to Sect. A.13.4 on Page 52, Item 158.)

167 [5] The management behaviour then



Figure 6: Informal Snapshots of Create and Edit Document Behaviours

- a [5.1] selects a handler, here shown as i, i.e.,  $hdlr_i$ ,
- b [5.2] records that that handler is granted certain access rights to document k,
- c [5.3] and offers that granting to handler behaviour *i*.

(We refer to Sect. A.13.2 on Page 51, Item 155 on Page 52.)

168 [6] Handler behaviour i records that it now has certain access rights to doccument i.

# A.16.2 The Edit Behaviour: Right Fig. 6

- 1 Handler behaviour i, at its own volition, initiates an edit action on document j (where i has editing rights for document j). Handler i, optionally, provides document j with a(annotation) note. While editing document j handler i also "selects" an appropriate pair of edit/undo functions for document j.
- 2 Document behaviour j accepts the editing request, enacts the editing, optionally appends the (annotation) note, and, with handler i, completes the editing, after some time interval ti.
- 3 Handler behaviour i completes its edit action.

### A.16.3 The Read Behaviour: Left Fig. 7 on the following page

- 1 Handler behaviour i, at its own volition, initiates a read action on document j (where i has reading rights for document j). Handler i, optionally, provides document j with a(annotation) note.
- 2 Document behaviour j accepts the reading request, enacts the reading by providing the handler, i, with the document contents, and optionally appends the (annotation) note, and, with handler i, completes the reading, after some time interval ti.
- 3 Handler behaviour i completes its read action.

### A.16.4 The Copy Behaviour: Right Fig. 7 on the next page

1 Handler behaviour i, at its own volition, initiates a copy action on document j (where i has copying rights for document j). Handler i, optionally, provides master document j as well as the copied document (yet to be identified) with respective (annotation) notes.



Figure 7: Informal Snapshots of Read and Copy Document Behaviours

- 2 The management behaviour offers to accept the handler message. As for the create action, the management behaviour offers a combined *copy and create* document message to the archive behaviour.
- 3 The archive behaviour selects an available document identifier (here shown as k), henceforth marking k as used.
- 4 The archive behaviour then obtains, from the master document j its document descriptor,  $dd_j$ , its document annotations,  $da_j$ , its document contents,  $dc_j$ , and its document history,  $dh_j$ .
- 5 The archice behaviour informs the management behaviour of the identifier, k, of the (new) document copy,
- 6 while assembling the attributes for that (new) document copy: its document descriptor,  $dd_k$ , its document annotations,  $da_k$ , its document contents,  $dc_k$ , and its document history,  $dh_k$ , from these "similar" attributes of the master document j,
- 7 while then "spawning off" document behaviour  $\mathsf{docu}_k$  here shown by the "dash-dotted" rounded edge square.
- 8 The management behaviour accepts the identifier, k, of the (new) document copy, recording the identities of the handlers and their access rights to k,
- 9 while informing these handlers (informally indicated by a "dangling" dash-dotted line) of their grants,
- 10 while also informing the master copy of the copy identity (etcetera).
- 11 The handlers granted access to the copy record this fact.

## A.16.5 The Grant Behaviour: Left Fig. 8 on the facing page

This behaviour has its

- 1 Item [1] correspond, in essence, to Item [9] of the copy behaviour see just above and
- 2 Item [2] correspond, in essence, to Item [11] of the copy behaviour.



Figure 8: Informal Snapshots of Grant and Shred Document Behaviours

#### A.16.6 The Shred Behaviour: Right Fig. 8

- 1 The management, at its own volition, selects a document, j, to be shredded. It so informs the archive behaviour.
- 2 The archive behaviour records that document j is to be no longer in use, but shredded, and informs document j's behaviour.
- 3 The document j behaviour accepts the shred message and **stops** (indicated by the dotted rounded edge box).

# A.17 The Behaviour Actions

To properly structure the definitions of the four kinds of (management, archive, handler and document) behaviours we single each of these out "across" the six behaviour traces informally described in Sects. A.16.1–A.16.6. The idea is that if behaviour  $\beta$  is involved in  $\tau$  traces,  $\tau_1, \tau_2, ..., \tau_{\tau}$ , then behaviour  $\beta$  shall be defined in terms of  $\tau$  non-deterministic alternative behaviours named  $\beta_{\tau_1}, \beta_{\tau_2}, ..., \beta_{\tau_{\tau}}$ .

### A.17.1 Management Behaviour

169 The management behaviour is involved in the following action traces:

a	create	Fig. 6 on Page 55 Left
b	сору	Fig. 7 on the preceding page Right
с	grant	Fig. 8 Left
d	shred	Fig. 8 Right

value

# Management Create Behaviour: Left Fig. 6 on Page 55

- 170 The management create behaviour
- 171 initiates a create document behaviour (i.e., a request to the archive behaviour),
- 172 and then awaits its response.

### value

```
170 \quad \mathsf{mgtm\_create:} \ \mathsf{MDIR} \to \mathbf{in,out} \ \mathsf{mgtm\_arch\_ch}, \ \{\mathsf{mgtm\_hdlr\_ch[hi]}|\mathsf{hi:Hl}{\bullet}\mathsf{hi} \in \mathsf{his}\} \ \mathbf{Unit}
```

- 170 mgtm\_create(mdir)  $\equiv$
- 171 [1] let hi = mgtm\_create\_initiation(mdir); [Left Fig. 6 on Page 55]
- 172 [5] mgtm\_create\_awaits\_response(mdir)(hi) end [Left Fig. 6 on Page 55]

### The management create initiation behaviour

- 173 selects a handler on behalf of which it requests the document creation,
- 174 assembles the elements of the create message:
  - by embedding a set of zero or more document references, dis, with some information, info, into a document descriptor, adding
  - $\bullet\,$  a document note, dn, and
  - and initial, that is, empty document contents, "empty\_DC",

175 offers such a create document message to the archive behaviour, and

176 yields the identifier of the chosen handler.

#### value

```
171 \quad \texttt{mgtm\_create\_initiation: MDIR} \rightarrow \mathbf{in,out \ mgtm\_arch\_ch, \ } \{\texttt{mgtm\_hdlr\_ch[hi]|hi:Hl\bullethi \in his} \} \ \mathsf{HI}
```

- 171 mgtm\_create\_initiation(mdir)  $\equiv$
- 173 **let**  $hi:HI \cdot hi \in dom mdir,$
- 174 [1.2-.4] (dis,info):(DI-set×Info),dn:DN is\_meaningful(embed\_DIs\_in\_DD(dis,info))(mdir) in
- 175 [1.1] mgtm\_arch\_ch ! mkCreate(embed\_Dls\_in\_DD(ds,info),dn,"empty\_DC")
- 176 hi end
- 174 is\_meaningful:  $DD \rightarrow MDIR \rightarrow \mathbf{Bool}$  [left further undefined]

# The management create awaits response behaviour

- 177 starts by awaiting a reply from the archive behaviour with the identity, di, of the document (that that behaviour has created).
- 178 It then selects suitable access rights,
- 179 with which it updates its handler/document directory
- 180 and offers to the chosen handler
- 181 whereupon it resumes, with the updated management directory, being the management behaviour.

value

172 mgtm\_create\_awaits\_response: MDIR  $\rightarrow$  HI  $\rightarrow$  in,out mgtm\_arch\_ch, {mgtm\_hdlr\_ch[hi]|hi:HI•hi  $\in$  his} Unit

- 172 mgtm\_create\_awaits\_response(mdir)  $\equiv$
- 177 [5] let mkNewDoclD(di) = mgtm\_arch\_ch ? in
- 178 [5.1] let acrs:ANm-set in
- 179 [5.2] let  $mdir' = mdir \dagger [hi \mapsto [di \mapsto acrs]]$  in
- 180 [5.3] mgtm\_hdlr\_ch[hi] ! mkGrant(di,acrs)
- 181 mgtm(mdir') end end

### Management Copy Behaviour: Right Fig. 7 on Page 56

- 182 The management copy behaviour
- 183 accepts a copy document request from a handler behaviour (i.e., a request to the archive behaviour),
- 184 and then awaits a response from the archive behaviour;
- 185 after which it grants access rights to handlers to the document copy.

#### value

- 182 mgtm\_copy: MDIR  $\rightarrow$  in,out mgtm\_arch\_ch, {mgtm\_hdlr\_ch[hi]|hi:Hl•hi  $\in$  his} Unit
- 182 mgtm\_copy(mdir)  $\equiv$
- 183 [2] **let** hi = mgtm\_accept\_copy\_request(mdir) in
- 184 [8] let di = mgtm\_awaits\_copy\_response(mdir)(hi) in
- 185 [9] mgtm\_grant\_access\_rights(mdir)(di) end end
- 186 The **management accept copy** behaviour non-deterministically externally ([]) awaits a copy request from a[ny] handler (i) behaviour –
- 187 with the request identifying the master document, j, to be copied.
- 188 The management accept copy behaviour forwards (!) this request to the archive behaviour –
- 189 while yielding the identity of the requesting handler.
- 186. mgtm\_accept\_copy\_request: MDIR  $\rightarrow$  in,out mgtm\_arch\_ch, {mgtm\_hdlr\_ch[hi]|hi:Hl•hi  $\in$  his} HI
- 186. mgtm\_accept\_copy\_request(mdir)  $\equiv$
- 187. let mkCopy(di,hi,t,dn) =  $[] \{mgtm_hdlr_ch[i]?|i:Hl \cdot i \in his\}$  in
- 188. mgtm\_arch\_ch ! mkCopy(di,hi,t,dn) ;
- 188. hi end

#### The management awaits copy response behaviour

- 190 awaits a reply from the archive behaviour as to the identity of the newly created copy (di) of master document j.
- 191 The management awaits copy response behaviour then informs the 'copying-requesting' handler, hi, that the copying has been completed and the identity of the copy (di) –
- 192 while yielding the identity, di, of the newly created copy.

192. di end

# The management grants access rights behaviour

193 selects suitable access rights for a suitable number of selected handlers.

194 It then offers these to the selected handlers.

```
185. mgtm_grant_access_rights: MDIR \rightarrow DI \rightarrow in,out {mgtm_hdlr_ch[hi]|hi:HI•hi \in his} Unit
```

185. mgtm\_grant\_access\_rights(mdir)(di)  $\equiv$ 

```
193. let diarm = [hi \mapsto acrs|hi:HI, arcs:ANm-set \cdot hi \in dom mdir \land arcs \subseteq (diarm(hi))(di)] in
```

```
194. \| \{mgtm_hdlr_ch[hi]!mkGrant(hi,time_ch?,di,acrs) |
```

194.  $hi:HI,acrs:ANm-set \cdot hi \in dom diarm \land acrs \subseteq (diarm(hi))(di) \}$  end

# Management Grant Behaviour: Left Fig. 8 on Page 57 The management grant behaviour

195 is a variant of the mgtm\_grant\_access\_rights function, Items 193–194.

196 The management behaviour selects a suitable subset of known handler identifiers, and

197 for these a suitable subset of document identifiers from which

198 it then constructs a map from handler identifiers to subsets of access rights.

199 With this the management behaviour then issues appropriate grants to the chosen handlers.

# type

 $\mathsf{MDIR} = \mathsf{HI} \ \overrightarrow{m} \ (\mathsf{DI} \ \overrightarrow{m} \ \mathsf{ANm}\text{-}\mathbf{set})$ 

value

195 mgtm\_grant: MDIR  $\rightarrow$  in,out {mgtm\_hdlr\_ch[hi]|hi:Hl•hi  $\in$  his} Unit

- 195 mgtm\_grant(mdir)  $\equiv$
- 196 let his  $\subseteq$  dom dir in

```
197 let dis \subseteq \bigcup \{ \operatorname{dom} \mathsf{mdir}(\mathsf{hi}) | \mathsf{hi:HI} \cdot \mathsf{hi} \in \mathsf{his} \} in
```

```
198 let diarm = [hi \mapsto acrs|hi:HI,di:DI,arcs:ANm-set \cdot hi \in his \land di \in dis \land acrs \subseteq (diarm(hi))(di)] in
```

```
199 ||{mgtm_hdlr_ch[hi]!mkGrant(di,acrs) |
```

```
199 hi:HI,di:DI,acrs:ANm-set \cdot hi \in dom diarm \land di \in dis \land acrs \subseteq (diarm(hi))(di)}
```

```
195 end end end
```

# Management Shred Behaviour: Right Fig. 8 on Page 57 The management shred behaviour

200 initiates a request to the archive behaviour.

201 First the management shred behaviour selects a document identifier (from its directory).

 $202\,$  Then it communicates a shred document message to the archive behaviour;

203 then it notes the (to be shredded) document in its directory

204 whereupon the management shred behaviour resumes being the management behaviour.

### value

```
204 mgtm(mdir') end end
```

# A.17.2 Archive Behaviour

205 The archive behaviour is involved in the following action traces:

a create	Fig. 6 on Page 55 Left
b copy	Fig. 7 on Page 56 Right
c shred	Fig. 8 on Page 57 Right

type

```
148ADIR = avail:DI-set × used:DI-set × gone:DI-setaxiom148\forall (avail,used,gone):ADIR • avail \cap used = {} \land gone \subseteq used205arch: ADIR \rightarrow in,out mgmt_arch_ch, {arch_docu_ch[di]|di:DI•di \in dis} Unit205aarch(adir) \equiv205aarch_create(adir)205b|| arch_copy(adir)205c|| arch_shred(adir)
```

# The Archive Create Behaviour: Left Fig. 6 on Page 55 The archive create behaviour

206 accepts a request, from the management behaviour to create a document;

- 207 it then selects an available document identifier;
- 208 communicates this new document identifier to the management behaviour;
- 209 while initiating a new document behaviour,  $docu_{di}$ , with the document descriptor, dd, the initial document annotation being the singleton list of the note, an, and the initial document contents, dc all received from the management behaviour and an initial document history of just one entry: the date of creation, all
- 210 in parallel with resuming the archive behaviour with updated programmable attributes.
- 205a. arch\_create: AATTR  $\rightarrow$  in,out mgmt\_arch\_ch, {arch\_docu\_ch[di]|di:DI•di  $\in$  dis} Unit
- 205a. arch\_create(avail,used,gone)  $\equiv$
- 206. [2] let mkCreate((hi,t),dd,an,dc) = mgmt\_arch\_ch ? in
- 207. **let** di:DI•di  $\in$  avail in

Towards a Formal Understanding of Urban Planning

- 208. [4] mgmt\_arch\_ch ! mkNewDocID(di) ;
- 209. [3] docu<sub>di</sub>(dd)( $\langle an \rangle$ ,dc,<(date\_of\_creation)>)
- 210.  $|| \operatorname{arch}(\operatorname{avail}_{\operatorname{di}}, \operatorname{used}_{\operatorname{di}}, \operatorname{gone})$

```
205a. end end
```

```
Version 2
```

The Archive Copy Behaviour: Right Fig. 7 on Page 56 The archive copy behaviour

- 211 accepts a copy document request from the management behaviour with the identity, j, of the master document;
- 212 it communicates (the request to obtain all the attribute values of the master document, j) to that document behaviour;
- 213 whereupon it awaits their communication (i.e., (dd, da, dc, dh));
- 214 (meanwhile) it obtains an available document identifier,
- 215 which it communicates to the management behaviour,
- 216 while initiating a new document behaviour,  $docu_{di}$ , with the master document descriptor, dd, the master document annotation, and the master document contents, dc, and the master document history, dh (all received from the master document),
- 217 in parallel with resuming the archive behaviour with updated programmable attributes.
- 205b. arch\_copy: AATTR  $\rightarrow$  in,out mgmt\_arch\_ch, {arch\_docu\_ch[di]|di:DI•di  $\in$  dis} Unit
- 205b. arch\_copy(avail,used,gone)  $\equiv$
- 211. [3] let mkDoclD(j,hi) = mgtm\_arch\_ch ? in
- 212. arch\_docu\_ch[j] ! mkReqAttrs() ;
- 213. let  $mkAttrs(dd,da,dc,dh) = arch_docu_ch[j]$ ? in
- 214. **let** di:DI di  $\in$  avail **in**
- 215. mgtm\_arch\_ch ! mkCopyDocID(di) ;
- 216. [6,7] docu<sub>di</sub>(augment(dd,"copy",j,hi),augment(da,"copy",hi),dc,augment(dh,("copy",date\_and\_time,j,hi)))
- 217.  $|| \operatorname{arch}(\operatorname{avail}_{di}, \operatorname{used}_{di}, \operatorname{gone})$
- 205b. end end end

where we presently leave the [overloaded] augment functions undefined.

### The Archive Shred Behaviour: Right Fig. 8 on Page 57 The archive shred behaviour

- 218 accepts a shred request from the management behaviour.
- 219 It communicates this request to the identified document behaviour.
- 220 And then resumes being the archive behaviour, noting however, that the shredded document has been shredded.
- 205c. arch\_shred: AATTR  $\rightarrow$  in,out mgmt\_arch\_ch, {arch\_docu\_ch[di]|di:DI•di  $\in$  dis} Unit
- 205c. arch\_shred(avail,used,gone)  $\equiv$

```
218. [2] let mkShred(j) = mgmt_arch_ch ? in
```

- 219. arch\_docu\_ch[j] ! mkShred() ;
- 220.  $\operatorname{arch}(\operatorname{avail},\operatorname{used},\operatorname{gone}\cup\{j\})$
- 205c. end

#### A.17.3 Handler Behaviours

221 The handler behaviour is involved in the following action traces:

$\mathbf{a}$	create	Fig. 6 on Page 55 Left
b	edit	Fig. 6 on Page 55 Right
$\mathbf{c}$	read	Fig. 7 on Page 56 Left
d	сору	Fig. 7 on Page 56 Right
е	grant	Fig. 8 on Page 57 Left

#### value

221  $hdlr_{hi}: HATTRS \rightarrow in, out mgtm_hdlr_ch[hi], \{hdlr_docu_ch[hi,di]|di:Dl•di\in dis\} Unit$ 

- 221  $hdlr_{hi}(hattrs) \equiv$
- 221a  $hdlr\_create_{hi}(hattrs)$
- 221b  $\Box$  hdlr\_edit<sub>hi</sub>(hattrs)
- 221c  $\Box$  hdlr\_read<sub>hi</sub>(hattrs)
- 221d [] hdlr\_copy<sub>hi</sub>(hattrs)
- 221e  $\Box$  hdlr\_grant<sub>hi</sub>(hattrs)

### The Handler Create Behaviour: Left Fig. 6 on Page 55

- 222 The **handler create** behaviour offers to accept the granting of access rights, **acrs**, to document di.
- 223 It according updates its programmable hattrs attribute;
- 224 and resumes being a handler behaviour with that update.
- 221a hdlr\_create<sub>hi</sub>: HATTRS  $\times$  HHIST  $\rightarrow$  in,out mgtm\_hdlr\_ch[hi] Unit
- 221a hdlr\_create<sub>hi</sub>(hattrs, hhist)  $\equiv$
- 222 let mkGrant(di,acrs) = mgtm\_hdlr\_ch[hi] ? in
- 223 let hattrs' = hattrs  $\dagger$  [hi  $\mapsto$  acrs] in
- 224 hdlr\_create<sub>hi</sub>(hattrs', augment(hhist, mkGrant(di, acrs))) end end

#### The Handler Edit Behaviour: Right Fig. 6 on Page 55

- 225 The handler behaviour, on its own volition, decides to edit a document, di, for which it has editing rights.
- 226 The handler behaviour selects a suitable (...) pair of edit/undo functions and a suitable (annotation) note.
- 227 It then communicates the desire to edit document di with (e,u) (at time  $t=time_ch$ ?).
- 228 Editing take some time, ti.
- 229 We can therefore assert that the time at which editing has completed is t+ti.
- 230 The handler behaviour accepts the edit completion message from the document handler.
- 231 The handler behaviour can therefore resume with an updated document history.

221b  $hdlr_{di:DI} + HATTRS \times HHIST \rightarrow in, out {hdlr_docu_ch[hi,di]|di:DI + di \in dis} Unit$ 

- 221b hdlr\_edit<sub>hi</sub>(hattrs,hhist)  $\equiv$
- 225 [1] let di:DI di  $\in$  dom hattrs  $\wedge$  "edit"  $\in$  hattrs(di) in
- 226 [1] let (e,u):(EDIT×UNDO) ... , n:AN ... in
- 227 [1] hdlr\_docu\_ch[hi,di] ! mkEdit(hi,t=time\_ch?,e,u,n);
- 228 [2] let ti:TIME\_INTERVAL ... in
- 229 [2] wait ti ; assert: time\_ch? = t+ti
- 230 [3] let mkEditComplete(ti',...) = hdlr\_docu\_ch[hi,di] ? in assert ti'  $\cong$  ti
- 231 hdlr<sub>hi</sub>(hattrs,augment(hhist,(di,mkEdit(hi,t,ti,e,u))))
- 221b end end end

# The Handler Read Behaviour: Left Fig. 7 on Page 56

- 232 The handler behaviour, on its own volition, decides to read a document, di, for which it has reading rights.
- 233 It then communicates the desire to read document di with at time  $t=time\_ch?$  with an annotation note (n).
- 234 Reading take some time, ti.
- 235 We can therefore assert that the time at which reading has completed is t+ti.
- 236 The handler behaviour accepts the read completion message from the document handler.
- 237 The handler behaviour can therefore resume with an updated document history.
- 221c hdlr\_edit<sub>*hi*</sub>: HATTRS × HHIST  $\rightarrow$  in,out {hdlr\_docu\_ch[hi,di]|di:Dl•di $\in$ dis} Unit
- 221c hdlr\_edit<sub>hi</sub>(hattrs, hhist)  $\equiv$
- 232 [1] let di:DI di  $\in$  dom hattrs  $\land$  "read"  $\in$  hattrs(di), n:N ... in
- 233 [1] hdlr\_docu\_ch[hi,di] ! mkRead(hi,t=time\_ch?,n) ;
- 234 [2] let ti:TIME\_INTERVAL ... in
- 235 [2] wait ti ; assert: time\_ch? = t+ti
- 236 [3] let mkReadComplete(ti,...) = hdlr\_docu\_ch[hi,di] ? in
- hdlr<sub>hi</sub>(hattrs,augment(hhist,(di,mkRead(di,t,ti))))
- 221c end end end

# The Handler Copy Behaviour: Right Fig. 7 on Page 56

- 238 The **handler [copy] behaviour**, on its own volition, decides to copy a document, *di*, for which it has copying rights.
- 239 It communicates this copy request to the management behaviour.
- 240 After a while the handler [copy] behaviour receives acknowledgement of a completed copying from the management behaviour.
- 241 The handler [copy] behaviour records the request and acknowledgement in its, thus updated whereupon the handler [copy] behaviour resumes being the handler behaviour.

- 221d hdlr\_copy<sub>hi</sub>: HATTRS  $\times$  HHIST  $\rightarrow$  in,out mgtm\_hdlr\_ch[hi] Unit
- 221d hdlr\_copy<sub>hi</sub>(hattrs, hhist)  $\equiv$
- 238 [1] let di:Dl di  $\in$  dom hattrs  $\land$  "copy"  $\in$  hattrs(di) in
- 239 [1] mgtm\_hdlr\_ch[hi] ! mkCopy(di,hi,t=time\_ch?) ;
- 240 [10] let mkCopyComplete(di',di) = mgtm\_hdlr\_ch[hi] ? in
- 241 [10] hdlr<sub>hi</sub>(hattrs,augment(hhist,time\_ch?,(mkCopy(di,hi,,t),mkCopyComplete(di'))))
- 221d end end

### The Handler Grant Behaviour: Left Fig. 8 on Page 57

- 242 The **handler [grant] behaviour** offers to accept grant permissions from the management behaviour.
- 243 In response it updates its handler attribute while resuming being a handler behaviour.
- 221e hdlr\_grant<sub>hi</sub>: HATTRS × HHIST  $\rightarrow$  in,out mgtm\_hdlr\_ch[hi] Unit
- 221e hdlr\_grant<sub>hi</sub>(hattrs, hhist)  $\equiv$
- 242 [2] let mkGrant(di,acrs) = mgtm\_hdlr\_ch[hi] ? in
- 243 [2]  $hdlr_{hi}(hattrst[di \rightarrow acrs], augment(hhist, time_ch?, mkGrant(di, acrs)))$
- 221e end

### A.17.4 **Document Behaviours**

244 The document behaviour is involved in the following action traces:

a edit	Fig. 6 on Page 55 Right
b read	Fig. 7 on Page 56 Left
c shred	Fig. 8 on Page 57 Right

# value

244 docu<sub>di</sub>: DD × (DA × DC × DH)  $\rightarrow$  in,out arch\_docu\_ch[di], {hdlr\_docu\_ch[hi,di]|hi:Hl•hi∈his} Unit 244 docu<sub>di</sub>(dattrs) = 244a docu\_edit<sub>di</sub>(dd)(da,dc,dh) 244b [] docu\_read<sub>di</sub>(dd)(da,dc,dh)

244c [] docu\_shred\_{di}(dd)(da,dc,dh)

# The Document Edit Behaviour: Right Fig. 6 on Page 55

245 The **document [edit] behaviour** offers to accept edit requests from document handlers.

- a The document contents is edited, over a time interval of ti, with respect to the handlers edit function (e),
- b the document annotations are augmented with respect to the handlers note (n), and
- c the document history is augmented with the fact that an edit took place, at a certain time, with a pair of edit/undo functions.

246 The edit (etc.) function(s) take some time, ti, to do.

247 The handler behaviour is notified, mkEditComplete(...) of the completion of the edit, and

248 the document behaviour is then resumed with updated programmable attributes.

#### value

```
244a
        docu_edit<sub>di</sub>: DD × (DA × DC × DH) \rightarrow in,out {hdlr_docu_ch[hi,di]|hi:Hl•hi∈his} Unit
        docu_edit_{di}(dd)(da,dc,dh) \equiv
244a
        [2] let mkEdit(hi,t,e,u,n) = [] {hdlr_docu_ch[hi,di]?|hi:Hl•hi\inhis} in
245
        [2] let dc' = e(dc),
245a
                 da' = augment(da,((hi,t),("edit",e,u),n)),
245b
                 dh' = augment(dh,((hi,t),("edit",e,u))) in
245c
246
             let ti = time_ch? - t in
             hdlr_docu_ch[hi,di] ! mkEditComplete(ti,...);
247
             docu_{di}(dd)(da',dc',dh')
248
244a
             end end end
```

# The Document Read Behaviour: Left Fig. 7 on Page 56

249 The The document [read] behaviour offers to receive a read request from a handler behaviour.

- 250 The reading takes some time to do.
- 251 The handler behaviour is advised on completion.
- 252 And the document behaviour is resumed with appropriate programmable attributes being updated.

value

```
244b docu_read<sub>di</sub>: DD × (DA × DC × DH) \rightarrow in,out {hdlr_docu_ch[hi,di]|hi:Hl•hi∈his} Unit
```

```
244b docu_read<sub>di</sub>(dd)(da,dc,dh) \equiv
```

- 249 [2] let mkRead(hi,t,n) = {hdlr\_docu\_ch[hi,di]?|hi:Hl•hi $\in$ his} in
- 250 [2] let ti:TIME\_INTERVAL  $\bullet$  ... in
- 250 [2] wait ti ;
- 251 [2] hdlr\_docu\_ch[hi,di] ! mkReadComplete(ti,...);
- 252 [2] docu<sub>di</sub>(dd)(augment(da,n),dc,augment(dh,(hi,t,ti,"read")))
- 244b end end

### The Document Shred Behaviour: Right Fig. 8 on Page 57

- 253 The **document [shred] behaviour** offers to accept a document shred request from the archive behaviour –
- 254 whereupon it stops!

#### value

244c docu\_shred<sub>di</sub>: DD × (DA × DC × DH)  $\rightarrow$  in,out arch\_docu\_ch[di] Unit 244c docu\_shred<sub>di</sub>(dd)(da,dc,dh)  $\equiv$ 253 [3] let mkShred(...) = arch\_docu\_ch[di] ? in 254 stop 244c [3] end

## A.18 Conclusion

This completes a first draft version of this document. The date time is: January 5, 2018: 09:42 am. Many things need to be done. First a careful checking of all types and functions: that all used names have been defined. The internal non-deterministic choices in formula Items 169 on Page 57, 205 on Page 61, 221 on Page 63 and 244 on Page 65, need be checked. I suspect there should, instead, be som mix of both internal and external non-deterministic choices. Then a careful motivation for all the other non-deterministic choices.

# **B** RSL: The RAISE Specification Language – A Primer

# **B.1** Type Expressions

Type expressions are expressions whose value are types, that is, possibly infinite sets of values (of "that" type).

# B.1.1 Atomic Types

Atomic types have (atomic) values. That is, values which we consider to have no proper constituent (sub-)values, i.e., cannot, to us, be meaningfully "taken apart".

RSL has a number of *built-in* atomic types. There are the Booleans, integers, natural numbers, reals, characters, and texts.

type

- [1] Bool true, false
- [2] Int ..., -2, -2, 0, 1, 2, ...
- [3] Nat 0, 1, 2, ...
- [4] Real ..., -5.43, -1.0, 0.0,  $1.23 \cdots$ ,  $2,7182 \cdots$ ,  $3,1415 \cdots$ , 4.56, ...
- [5] **Char** "a", "b", ..., "0", ...
- [6] Text "abracadabra"

# B.1.2 Composite Types

Composite types have composite values. That is, values which we consider to have proper constituent (sub-)values, i.e., can be meaningfully "taken apart". There are two ways of expressing composite types: either explicitly, using concrete type expressions, or implicitly, using sorts (i.e., abstract types) and observer functions.

**Concrete Composite Types** From these one can form type expressions: finite sets, infinite sets, Cartesian products, lists, maps, etc.

Let A, B and C be any type names or type expressions, then the following are type expressions:

[7] A-set	[13] A  o B
[8] A-infset	$[14]$ A $\stackrel{\sim}{ ightarrow}$ B
$[9] A \times B \times \times C$	[15] (A)
[10] A*	[16] A   B     C
$[11] A^{\omega}$	[ 17 ] mk_id(sel_a:A,,sel_b:B)
$[12] A \xrightarrow{m} B$	[18] sel_a:A sel_b:B

The following the meaning of the atomic and the composite type expressions:

- 1 The Boolean type of truth values **false** and **true**.
- 2 The integer type on integers ..., –2, –1, 0, 1, 2, ... .
- 3 The natural number type of positive integer values 0, 1, 2,  $\ldots$
- 4 The real number type of real values, i.e., values whose numerals can be written as an integer, followed by a period ("."), followed by a natural number (the fraction).
- 5 The character type of character values "a", "bb", ...

- 6 The text type of character string values "aa", "aaa", ..., "abc", ...
- 7 The set type of finite cardinality set values.
- 8 The set type of infinite and finite cardinality set values.
- 9 The Cartesian type of Cartesian values.
- 10 The list type of finite length list values.
- 11 The list type of infinite and finite length list values.
- 12 The map type of finite definition set map values.
- 13 The function type of total function values.
- 14 The function type of partial function values.
- 15 In (A) A is constrained to be:
  - either a Cartesian  $B \times C \times ... \times D$ , in which case it is identical to type expression kind 9,
  - or not to be the name of a built-in type (cf., 1–6) or of a type, in which case the parentheses serve as simple delimiters, e.g., (A → B), or (A\*)-set, or (A-set)list, or (A|B) → (C|D|(E → F)), etc.
- 16 The postulated disjoint union of types A, B, ..., and C.
- 17 The record type of mk\_id-named record values mk\_id(av,...,bv), where av, ..., bv, are values of respective types. The distinct identifiers sel\_a, etc., designate selector functions.
- 18 The record type of unnamed record values (av,...,bv), where av, ..., bv, are values of respective types. The distinct identifiers sel\_a, etc., designate selector functions.

#### Sorts and Observer Functions

type A, B, C, ..., D value obs\_B: A  $\rightarrow$  B, obs\_C: A  $\rightarrow$  C, ..., obs\_D: A  $\rightarrow$  D

The above expresses that values of type A are composed from at least three values — and these are of type B, C,  $\ldots$ , and D. A concrete type definition corresponding to the above presupposing material of the next section

type B, C, ..., D  $A = B \times C \times ... \times D$ 

# **B.2** Type Definitions

# B.2.1 Concrete Types

Types can be concrete in which case the structure of the type is specified by type expressions:

type

 $A = Type\_expr$ 

Some schematic type definitions are:

where a form of [20]-[21] is provided by combining the types:

 $\begin{array}{l} Type\_name = A \mid B \mid ... \mid Z \\ A == mk\_id\_1(s\_a1:A\_1,...,s\_ai:A\_i) \\ B == mk\_id\_2(s\_b1:B\_1,...,s\_bj:B\_j) \\ ... \\ Z == mk\_id\_n(s\_z1:Z\_1,...,s\_zk:Z\_k) \end{array}$ 

Types A, B, ..., Z are disjoint, i.e., shares no values, provided all  $mk_id_k$  are distinct and due to the use of the disjoint record type constructor ==.

### axiom

```
∀ a1:A_1, a2:A_2, ..., ai:Ai •
    s_a1(mk_id_1(a1,a2,...,ai))=a1 ∧ s_a2(mk_id_1(a1,a2,...,ai))=a2 ∧
    ... ∧ s_ai(mk_id_1(a1,a2,...,ai))=ai ∧
    ∀ a:A • let mk_id_1(a1',a2',...,ai') = a in
    a1' = s_a1(a) ∧ a2' = s_a2(a) ∧ ... ∧ ai' = s_ai(a) end
```

# B.2.2 Subtypes

In RSL, each type represents a set of values. Such a set can be delimited by means of predicates. The set of values b which have type B and which satisfy the predicate  $\mathcal{P}$ , constitute the subtype A:

 $\begin{array}{l} \mathbf{type} \\ \mathsf{A} = \{ \mid \mathsf{b}: \mathsf{B} \bullet \mathcal{P}(\mathsf{b}) \mid \} \end{array}$ 

# B.2.3 Sorts — Abstract Types

Types can be (abstract) sorts in which case their structure is not specified:

type

A, B, ..., C

# B.3 The RSL Predicate Calculus

### **B.4** Propositional Expressions

Let identifiers (or propositional expressions) a, b, ..., c designate Boolean values (true or false [or chaos]). Then:

#### false, true

a, b, ..., c  $\sim$ a, a $\wedge$ b, a $\vee$ b, a $\Rightarrow$ b, a=b, a $\neq$ b

are propositional expressions having Boolean values.  $\sim, \wedge, \vee, \Rightarrow$ , = and  $\neq$  are Boolean connectives (i.e., operators). They can be read as: not, and, or, if then (or implies), equal and not equal.

#### B.4.1 Simple Predicate Expressions

Let identifiers (or propositional expressions) a, b, ..., c designate Boolean values, let x, y, ..., z (or term expressions) designate non-Boolean values and let i, j, ..., k designate number values, then:

```
false, true
a, b, ..., c
\sima, a\wedgeb, a\veeb, a\Rightarrowb, a=b, a\neqb
x=y, x\neqy,
i<j, i\leqj, i\geqj, i\neqj, i\geqj, i>j
```

are simple predicate expressions.

#### **B.4.2 Quantified Expressions**

Let X, Y, ..., C be type names or type expressions, and let  $\mathcal{P}(x)$ ,  $\mathcal{Q}(y)$  and  $\mathcal{R}(z)$  designate predicate expressions in which x, y and z are free. Then:

 $\forall \mathbf{x}: \mathbf{X} \bullet \mathcal{P}(x) \\ \exists \mathbf{y}: \mathbf{Y} \bullet \mathcal{Q}(y) \\ \exists \mathbf{!} \mathbf{z}: \mathbf{Z} \bullet \mathcal{R}(z)$ 

are quantified expressions — also being predicate expressions.

They are "read" as: For all x (values in type X) the predicate  $\mathcal{P}(x)$  holds; there exists (at least) one y (value in type Y) such that the predicate  $\mathcal{Q}(y)$  holds; and there exists a unique z (value in type Z) such that the predicate  $\mathcal{R}(z)$  holds.

### B.5 Concrete RSL Types: Values and Operations

### B.5.1 Arithmetic

type Nat, Int, Real value  $+,-,*: Nat \times Nat \rightarrow Nat | Int \times Int \rightarrow Int | Real \times Real \rightarrow Real$   $/: Nat \times Nat \xrightarrow{\sim} Nat | Int \times Int \xrightarrow{\sim} Int | Real \times Real \xrightarrow{\sim} Real$  $<,\leq,=,\neq,\geq,> (Nat | Int | Real) \rightarrow (Nat | Int | Real)$ 

Version 2

### B.5.2 Set Expressions

**Set Enumerations** Let the below a's denote values of type A, then the below designate simple set enumerations:

 $\{\{\}, \{a\}, \{e_1, e_2, \dots, e_n\}, \dots\} \in A\text{-set} \\ \{\{\}, \{a\}, \{e_1, e_2, \dots, e_n\}, \dots, \{e_1, e_2, \dots\}\} \in A\text{-infset}$ 

**Set Comprehension** The expression, last line below, to the right of the  $\equiv$ , expresses set comprehension. The expression "builds" the set of values satisfying the given predicate. It is abstract in the sense that it does not do so by following a concrete algorithm.

type

A, B  $P = A \rightarrow Bool$  $Q = A \xrightarrow{\sim} B$ 

value

 $\begin{array}{l} \mbox{comprehend: } A\mbox{-infset} \times P \times Q \rightarrow B\mbox{-infset} \\ \mbox{comprehend}(s,P,Q) \equiv \{ \ Q(a) \mid a : A \bullet a \in s \land P(a) \} \end{array}$ 

## **B.5.3** Cartesian Expressions

**Cartesian Enumerations** Let e range over values of Cartesian types involving  $A, B, \ldots, C$ , then the below expressions are simple Cartesian enumerations:

type A, B, ..., C  $A \times B \times ... \times C$ value (e1,e2,...,en)

#### B.5.4 List Expressions

**List Enumerations** Let a range over values of type A, then the below expressions are simple list enumerations:

 $\{ \langle \rangle, \langle e \rangle, ..., \langle e1, e2, ..., en \rangle, ... \} \in \mathsf{A}^* \\ \{ \langle \rangle, \langle e \rangle, ..., \langle e1, e2, ..., en \rangle, ..., \langle e1, e2, ..., en, ... \rangle, ... \} \in \mathsf{A}^{\omega} \\ \langle \mathsf{a}_i ... \mathsf{a}_j \rangle$ 

The last line above assumes  $a_i$  and  $a_j$  to be integer-valued expressions. It then expresses the set of integers from the value of  $e_i$  to and including the value of  $e_j$ . If the latter is smaller than the former, then the list is empty.

List Comprehension The last line below expresses list comprehension.

type A, B, P = A  $\rightarrow$  Bool, Q = A  $\stackrel{\sim}{\rightarrow}$  B value comprehend: A<sup>\u03c6</sup> × P × Q  $\stackrel{\sim}{\rightarrow}$  B<sup>\u03c6</sup> comprehend(I,P,Q)  $\equiv \langle Q(I(i)) | i in \langle 1..len | \rangle \bullet P(I(i)) \rangle$
#### B.5.5 Map Expressions

**Map Enumerations** Let (possibly indexed) u and v range over values of type T1 and T2, respectively, then the below expressions are simple map enumerations:

 $\begin{array}{l} \mathbf{type} \\ & \mathsf{T1, T2} \\ \mathsf{M} = \mathsf{T1} \xrightarrow{} \mathsf{m} \mathsf{T2} \\ \mathbf{value} \\ & \mathsf{u,u1,u2,...,un:T1, v,v1,v2,...,vn:T2} \\ & [], \ [\mathsf{u} {\mapsto} \mathsf{v}], \ ..., \ [\mathsf{u1} {\mapsto} \mathsf{v1,u2} {\mapsto} \mathsf{v2,...,un} {\mapsto} \mathsf{vn}] \mathsf{all} \in \mathsf{M} \end{array}$ 

Map Comprehension The last line below expresses map comprehension:

#### type

U, V, X, Y  $M = U \xrightarrow{m} V$   $F = U \xrightarrow{\sim} X$   $G = V \xrightarrow{\sim} Y$   $P = U \rightarrow \textbf{Bool}$ value comprehend:  $M \times F \times G \times P \rightarrow (X \xrightarrow{m} Y)$ comprehend(m,F,G,P)  $\equiv [F(u) \mapsto G(m(u)) \mid u: U \bullet u \in \textbf{dom } m \land P(u)]$ 

## B.5.6 Set Operations Set Operator Signatures

#### value

30 card: A-infset  $\xrightarrow{\sim}$  Nat

# Set Examples

### examples

 $\begin{array}{l} a \in \{a,b,c\} \\ a \not\in \{\}, \ a \not\in \{b,c\} \\ \{a,b,c\} \cup \{a,b,d,e\} = \{a,b,c,d,e\} \\ \cup \{\{a\},\{a,bb\},\{a,d\}\} = \{a,b,d\} \\ \{a,b,c\} \cap \{c,d,e\} = \{c\} \end{array}$ 

Towards a Formal Understanding of Urban Planning

 $\bigcap \{ \{a\}, \{a, bb\}, \{a, d\} \} = \{a\} \\ \{a, b, c\} \setminus \{c, d\} = \{a, bb\} \\ \{a, b, c\} \subseteq \{a, b, c\} \\ \{a, b, c\} \subseteq \{a, b, c\} \\ \{a, b, c\} = \{a, b, c\} \\ \{a, b, c\} \neq \{a, bb\} \\ card \{\} = 0, card \{a, b, c\} = 3$ 

## **Informal Explication**

- 19  $\in$ : The membership operator expresses that an element is a member of a set.
- 20  $\notin$ : The nonmembership operator expresses that an element is not a member of a set.
- 21  $\cup$ : The infix union operator. When applied to two sets, the operator gives the set whose members are in either or both of the two operand sets.
- 22  $\cup$ : The distributed prefix union operator. When applied to a set of sets, the operator gives the set whose members are in some of the operand sets.
- 23  $\cap$ : The infix intersection operator. When applied to two sets, the operator gives the set whose members are in both of the two operand sets.
- 24  $\cap$ : The prefix distributed intersection operator. When applied to a set of sets, the operator gives the set whose members are in some of the operand sets.
- 25 \: The set complement (or set subtraction) operator. When applied to two sets, the operator gives the set whose members are those of the left operand set which are not in the right operand set.
- 26  $\subseteq$ : The proper subset operator expresses that all members of the left operand set are also in the right operand set.
- 27  $\subset$ : The proper subset operator expresses that all members of the left operand set are also in the right operand set, and that the two sets are not identical.
- 28 =: The equal operator expresses that the two operand sets are identical.
- 29  $\neq$ : The nonequal operator expresses that the two operand sets are *not* identical.
- 30 card: The cardinality operator gives the number of elements in a finite set.

**Set Operator Definitions** The operations can be defined as follows ( $\equiv$  is the definition symbol):

#### value

 $\begin{array}{l} s' \cup s'' \equiv \left\{ \begin{array}{l} a \mid a:A \bullet a \in s' \lor a \in s'' \end{array} \right\} \\ s' \cap s'' \equiv \left\{ \begin{array}{l} a \mid a:A \bullet a \in s' \land a \in s'' \end{array} \right\} \\ s' \setminus s'' \equiv \left\{ \begin{array}{l} a \mid a:A \bullet a \in s' \land a \notin s'' \end{array} \right\} \\ s' \subseteq s'' \equiv \forall a:A \bullet a \in s' \Rightarrow a \in s'' \\ s' \subseteq s'' \equiv s' \subseteq s'' \land \exists a:A \bullet a \in s'' \land a \notin s' \\ s' = s'' \equiv \forall a:A \bullet a \in s' \equiv a \in s'' \equiv s \subseteq s' \land s' \subseteq s \\ s' \neq s'' \equiv s' \cap s'' \neq \left\{ \right\} \\ card s \equiv \end{array}$ 

 $\label{eq:stars} \begin{array}{l} \mbox{if $s=\{$} \mbox{ then 0 else} \\ \mbox{let $a:A$ $\bullet$ $a $\in $s$ in $1+$ $card $($s $\setminus $a$) end end} \\ \mbox{pre $s$ $/*$ is $a$ finite set $*/$ \\ \mbox{card $s $\equiv$ $chaos $/*$ tests for infinity of $s$ $*/$ } \end{array}$ 

## B.5.7 Cartesian Operations

#### type

A, B, C g0: G0 = A  $\times$  B  $\times$  C g1: G1 = ( A  $\times$  B  $\times$  C ) g2: G2 = ( A  $\times$  B )  $\times$  C g3: G3 = A  $\times$  ( B  $\times$  C )

value

va:A, vb:B, vc:C, vd:D (va,vb,vc):G0,

B.5.8 List Operations List Operator Signatures

value

hd:  $A^{\omega} \xrightarrow{\sim} A$ tl:  $A^{\omega} \xrightarrow{\sim} A^{\omega}$ len:  $A^{\omega} \xrightarrow{\sim} Nat$ inds:  $A^{\omega} \rightarrow Nat$ -infset elems:  $A^{\omega} \rightarrow A$ -infset .(.):  $A^{\omega} \times Nat \xrightarrow{\sim} A$  $\widehat{}: A^{*} \xrightarrow{*} A^{\omega} A^{\omega} A^{\omega} BoBbol$ 

#### List Operation Examples

## examples

```
 \begin{array}{l} \mathbf{hd}\langle a1,a2,...,am\rangle = a1 \\ \mathbf{tl}\langle a1,a2,...,am\rangle = \langle a2,...,am\rangle \\ \mathbf{len}\langle a1,a2,...,am\rangle = m \\ \mathbf{inds}\langle a1,a2,...,am\rangle = \{1,2,...,m\} \\ \mathbf{elems}\langle a1,a2,...,am\rangle = \{a1,a2,...,am\} \\ \langle a1,a2,...,am\rangle(\mathbf{i}) = a\mathbf{i} \\ \langle a,b,c\rangle^{\frown}\langle a,b,d\rangle = \langle a,b,c,a,b,d\rangle \\ \langle a,b,c\rangle = \langle a,b,c\rangle \\ \langle a,b,c\rangle \neq \langle a,b,d\rangle \\ \end{array}
```

## **Informal Explication**

Towards a Formal Understanding of Urban Planning

- hd: Head gives the first element in a nonempty list.
- tl: Tail gives the remaining list of a nonempty list when Head is removed.

75

(va,vb,vc):G1 ((va,vb),vc):G2 (va3,(vb3,vc3)):G3

decomposition expressions

 $\begin{array}{l} {\rm let} \ (a1,b1,c1) = g0, \\ (a1',b1',c1') = g1 \ {\rm in} \ .. \ end \\ {\rm let} \ ((a2,b2),c2) = g2 \ {\rm in} \ .. \ end \\ {\rm let} \ (a3,(b3,c3)) = g3 \ {\rm in} \ .. \ end \end{array}$ 

- len: Length gives the number of elements in a finite list.
- inds: Indices give the set of indices from 1 to the length of a nonempty list. For empty lists, this set is the empty set as well.
- elems: Elements gives the possibly infinite set of all distinct elements in a list.
- $\ell(i)$ : Indexing with a natural number, *i* larger than 0, into a list  $\ell$  having a number of elements larger than or equal to *i*, gives the *i*th element of the list.
- ^: Concatenates two operand lists into one. The elements of the left operand list are followed by the elements of the right. The order with respect to each list is maintained.
- =: The equal operator expresses that the two operand lists are identical.
- $\neq$ : The nonequal operator expresses that the two operand lists are *not* identical.

The operations can also be defined as follows:

## **List Operator Definitions**

# value is\_finite\_list: $A^{\omega} \rightarrow \mathbf{Bool}$ len q $\equiv$ case is\_finite\_list(q) of true $\rightarrow$ if q = $\langle \rangle$ then 0 else 1 + len tl q end, $false \rightarrow chaos \ end$ inds $q \equiv$ case is\_finite\_list(q) of true $\rightarrow$ { i | i:Nat • 1 $\leq$ i $\leq$ len q }, false $\rightarrow$ { i | i:Nat • i \neq 0 } end elems $q \equiv \{ q(i) \mid i: Nat \cdot i \in inds q \}$ $q(i) \equiv$ if i=1then if $q \neq \langle \rangle$ then let $a:A,q':Q \cdot q = \langle a \rangle^{\hat{q}'}$ in a end else chaos end else q(i-1) end $fq \cap iq \equiv$ $\langle if 1 \leq i \leq len fq then fq(i) else iq(i - len fq) end$ $|i:Nat \cdot if len iq \neq chaos then i \leq len fq + len end \rangle$ pre is\_finite\_list(fq) $ig' = ig'' \equiv$ inds $iq' = inds iq'' \land \forall i:Nat \bullet i \in inds iq' \Rightarrow iq'(i) = iq''(i)$ $ig' \neq ig'' \equiv \sim (ig' = ig'')$

# B.5.9 Map Operations

Map Operator Signatures and Map Operation Examples

## value

m(a): M  $\rightarrow$  A  $\stackrel{\sim}{\rightarrow}$  B, m(a) = b

- dom:  $M \rightarrow A$ -infset [domain of map] dom [a1 $\mapsto$ b1,a2 $\mapsto$ b2,...,an $\mapsto$ bn] = {a1,a2,...,an}
- **rng**:  $M \rightarrow B$ -**infset** [range of map] **rng** [a1 $\mapsto$ b1,a2 $\mapsto$ b2,...,an $\mapsto$ bn] = {b1,b2,...,bn}
- $\label{eq:matrix} \begin{array}{l} \dagger: \ M \times M \to M \ [ \text{override extension} ] \\ [ a \mapsto b, a' \mapsto bb', a'' \mapsto bb'' ] \ \dagger \ [ a' \mapsto bb'', a'' \mapsto bb'' ] = [ a \mapsto b, a' \mapsto bb'', a'' \mapsto bb'' ] \end{array}$
- $\begin{array}{l} \cup: \ \mathsf{M} \times \mathsf{M} \to \mathsf{M} \ [\,\mathsf{merge} \cup ] \\ [\,\mathsf{a} \mapsto \mathsf{b}, \mathsf{a}' \mapsto \mathsf{b} \mathsf{b}', \mathsf{a}'' \mapsto \mathsf{b} \mathsf{b}''] \cup [\,\mathsf{a}''' \mapsto \mathsf{b} \mathsf{b}'''] = [\,\mathsf{a} \mapsto \mathsf{b}, \mathsf{a}' \mapsto \mathsf{b} \mathsf{b}', \mathsf{a}'' \mapsto \mathsf{b} \mathsf{b}'', \mathsf{a}''' \mapsto \mathsf{b} \mathsf{b}'''] \end{array}$
- $\label{eq:alpha} \begin{array}{l} & \cdot : \ M \times A\text{-}\mathbf{infset} \to M \ [restriction \ by] \\ & [a \mapsto b, a' \mapsto bb', a'' \mapsto bb''] \backslash \{a\} = [a' \mapsto bb', a'' \mapsto bb''] \end{array}$
- $\begin{array}{l} /: \ \mathsf{M} \times A\text{-infset} \to \mathsf{M} \ [restriction \ to] \\ [a \mapsto b, a' \mapsto bb', a'' \mapsto bb''] / \{a', a''\} = [a' \mapsto bb', a'' \mapsto bb''] \end{array}$
- $=, \neq: M \times M \rightarrow \mathbf{Bool}$
- $\stackrel{\circ:}{(A \atop \overrightarrow{m} B) \times (B \atop \overrightarrow{m} C) \to (A \atop \overrightarrow{m} C) [composition] \\ [a \mapsto b, a' \mapsto bb'] \stackrel{\circ}{(bb \mapsto c, bb' \mapsto c', bb'' \mapsto c''] = [a \mapsto c, a' \mapsto c']$

#### Map Operation Explication

- m(a): Application gives the element that a maps to in the map m.
- dom: Domain/Definition Set gives the set of values which *maps to* in a map.
- rng: Range/Image Set gives the set of values which are mapped to in a map.
- †: Override/Extend. When applied to two operand maps, it gives the map which is like an override of the left operand map by all or some "pairings" of the right operand map.
- $\cup$ : Merge. When applied to two operand maps, it gives a merge of these maps.
- \: Restriction. When applied to two operand maps, it gives the map which is a restriction of the left operand map to the elements that are not in the right operand set.
- /: Restriction. When applied to two operand maps, it gives the map which is a restriction of the left operand map to the elements of the right operand set.
- =: The equal operator expresses that the two operand maps are identical.
- $\neq$ : The nonequal operator expresses that the two operand maps are *not* identical.

• °: Composition. When applied to two operand maps, it gives the map from definition set elements of the left operand map,  $m_1$ , to the range elements of the right operand map,  $m_2$ , such that if a is in the definition set of  $m_1$  and maps into b, and if b is in the definition set of  $m_2$  and maps into c, then a, in the composition, maps into c.

Map Operation Redefinitions The map operations can also be defined as follows:

```
value

rng m = { m(a) | a:A • a ∈ dom m }

m1 † m2 =

[ a\mapstob | a:A,b:B •

a ∈ dom m1 \ dom m2 \land bb=m1(a) \lor a ∈ dom m2 \land bb=m2(a) ]

m1 \cup m2 = [ a\mapstob | a:A,b:B •

a ∈ dom m1 \land bb=m1(a) \lor a ∈ dom m2 \land bb=m2(a) ]

m \ s = [ a\mapstom(a) | a:A • a ∈ dom m \ s ]

m \ s = [ a\mapstom(a) | a:A • a ∈ dom m \ s ]

m1 = m2 =

dom m1 = dom m2 \land \forall a:A • a ∈ dom m1 \Rightarrow m1(a) = m2(a)

m1 \neq m2 = \sim(m1 = m2)

m°n =

[ a\mapstoc | a:A,c:C • a ∈ dom m \land c = n(m(a)) ]
```

## **B.6** $\lambda$ -Calculus + Functions

pre rng m  $\subseteq$  dom n

## **B.6.1** The $\lambda$ -Calculus Syntax

 $\begin{array}{l} \textbf{type } /* \text{ A BNF Syntax: } */ \\ \langle L \rangle ::= \langle V \rangle \mid \langle F \rangle \mid \langle A \rangle \mid (\langle A \rangle ) \\ \langle V \rangle ::= /* \text{ variables, i.e. identifiers } */ \\ \langle F \rangle ::= \lambda \langle V \rangle \bullet \langle L \rangle \\ \langle A \rangle ::= (\langle L \rangle \langle L \rangle ) \\ \textbf{value } /* \text{ Examples } */ \\ \langle L \rangle : \text{ e, f, a, ...} \\ \langle V \rangle : \text{ x, ...} \\ \langle F \rangle : \lambda \times \bullet \text{ e, ...} \\ \langle A \rangle :: \text{ f a, (f a), f(a), (f)(a), ...} \end{array}$ 

#### B.6.2 Free and Bound Variables

Let x, y be variable names and e, f be  $\lambda$ -expressions.

- $\langle \mathbf{V} \rangle$ : Variable x is free in x.
- $\langle F \rangle$ : x is free in  $\lambda y \cdot e$  if  $x \neq y$  and x is free in e.
- $\langle A \rangle$ : x is free in f(e) if it is free in either f or e (i.e., also in both).

### B.6.3 Substitution

In RSL, the following rules for substitution apply:

- subst $([N/x]x) \equiv N;$
- $subst([N/x]a) \equiv a$ ,

for all variables  $a \neq x$ ;

- $subst([N/x](P \ Q)) \equiv (subst([N/x]P) \ subst([N/x]Q));$
- subst( $[N/x](\lambda x \cdot P)$ )  $\equiv \lambda y \cdot P$ ;
- subst([N/x]( $\lambda$  y•P))  $\equiv \lambda y$  subst([N/x]P),

if  $x \neq y$  and y is not free in N or x is not free in P;

• subst([N/x]( $\lambda y \cdot P$ ))  $\equiv \lambda z \cdot subst([N/z]subst([z/y]P)),$ 

if  $y \neq x$  and y is free in N and x is free in P (where z is not free in (N P)).

#### **B.6.4** $\alpha$ -Renaming and $\beta$ -Reduction

•  $\alpha$ -renaming:  $\lambda x \cdot M$ 

If x, y are distinct variables then replacing x by y in  $\lambda x \cdot M$  results in  $\lambda y \cdot subst([y/x]M)$ . We can rename the formal parameter of a  $\lambda$ -function expression provided that no free variables of its body M thereby become bound.

•  $\beta$ -reduction:  $(\lambda x \cdot M)(N)$ 

All free occurrences of x in M are replaced by the expression N provided that no free variables of N thereby become bound in the result.  $(\lambda x \cdot M)(N) \equiv subst([N/x]M)$ 

#### B.6.5 Function Signatures

For sorts we may want to postulate some functions:

```
type

A, B, C

value

obs_B: A \rightarrow B,

obs_C: A \rightarrow C,

gen_A: BB \times C \rightarrow A
```

## B.6.6 Function Definitions

Functions can be defined explicitly:

value f: Arguments  $\rightarrow$  Result f(args)  $\equiv$  DValueExpr g: Arguments  $\xrightarrow{\sim}$  Result g(args)  $\equiv$  ValueAndStateChangeClause

 $\mathbf{pre} \ \mathsf{P}(\mathsf{args})$ 

Or functions can be defined implicitly:

value

f: Arguments  $\rightarrow$  Result f(args) as result post P1(args,result)

g: Arguments  $\xrightarrow{\sim}$  Result g(args) as result pre P2(args) post P3(args,result)

The symbol  $\xrightarrow{\sim}$  indicates that the function is partial and thus not defined for all arguments. Partial functions should be assisted by preconditions stating the criteria for arguments to be meaningful to the function.

# **B.7** Other Applicative Expressions

### **B.7.1** Simple let Expressions

Simple (i.e., nonrecursive) **let** expressions:

let  $a = \mathcal{E}_d$  in  $\mathcal{E}_b(a)$  end

is an "expanded" form of:

 $(\lambda a. \mathcal{E}_b(a))(\mathcal{E}_d)$ 

## **B.7.2** Recursive let Expressions

Recursive **let** expressions are written as:

let  $f = \lambda a: A \cdot E(f)$  in B(f,a) end

is "the same" as:

let f = YF in B(f,a) end

where:

 $F \equiv \lambda g \cdot \lambda a \cdot (E(g))$  and YF = F(YF)

#### **B.7.3 Predicative** let **Expressions**

Predicative **let** expressions:

let a:A •  $\mathcal{P}(a)$  in  $\mathcal{B}(a)$  end

express the selection of a value a of type A which satisfies a predicate  $\mathcal{P}(a)$  for evaluation in the body  $\mathcal{B}(a)$ .

## B.7.4 Pattern and "Wild Card" let Expressions

Patterns and wild cards can be used:

let  $\{a\} \cup s = set in \dots end$ let  $\{a,\_\} \cup s = set in \dots end$ let  $\{a,\_\} \cup s = set in \dots end$ let  $(a,b,\dots,c) = cart in \dots end$ let  $(a,\_,\dots,c) = cart in \dots end$ let  $\langle a \rangle^{\widehat{\ell}} = list in \dots end$ let  $\langle a,\_,bb \rangle^{\widehat{\ell}} = list in \dots end$ let  $[a \mapsto bb] \cup m = map in \dots end$ let  $[a \mapsto bb_{\_}] \cup m = map in \dots end$ 

# B.7.5 Conditionals

Various kinds of conditional expressions are offered by RSL:

```
if b_expr then c_expr else a_expr
end
```

```
if b_expr then c_expr end \equiv /* same as: */
if b_expr then c_expr else skip end
```

```
if b_expr_1 then c_expr_1
elsif b_expr_2 then c_expr_2
elsif b_expr_3 then c_expr_3
...
elsif b_expr_n then c_expr_n end
case expr of
choice_pattern_1 \rightarrow expr_1,
choice_pattern_2 \rightarrow expr_2,
...
choice_pattern_n_or_wild_card \rightarrow expr_n
end
```

## **B.7.6 Operator/Operand Expressions**

```
\begin{array}{l} \langle \mathsf{Expr} \rangle :::= & \langle \mathsf{Prefix\_Op} \rangle \langle \mathsf{Expr} \rangle \\ & | \langle \mathsf{Expr} \rangle \langle \mathsf{Infix\_Op} \rangle \langle \mathsf{Expr} \rangle \\ & | \langle \mathsf{Expr} \rangle \langle \mathsf{Suffix\_Op} \rangle \\ & | \dots \\ \langle \mathsf{Prefix\_Op} \rangle :::= & \\ & - | \sim | \cup | \cap | \operatorname{\mathbf{card}} | \operatorname{\mathbf{len}} | \operatorname{\mathbf{inds}} | \operatorname{\mathbf{elems}} | \operatorname{\mathbf{hd}} | \operatorname{\mathbf{tl}} | \operatorname{\mathbf{dom}} | \operatorname{\mathbf{rng}} \\ \langle \mathsf{Infix\_Op} \rangle :::= & \\ & = | \neq | \equiv | + | - | * | \uparrow | / | < | \leq | \geq | > | \land | \lor | \Rightarrow \\ & | \in | \notin | \cup | \cap | \setminus | \subset | \subseteq | \supseteq | \supset | \cap | \uparrow | ^{\circ} \\ \langle \mathsf{Suffix\_Op} \rangle :::= ! \end{array}
```

# B.8 Imperative Constructs

## **B.8.1** Statements and State Changes

Often, following the RAISE method, software development starts with highly abstract-applicative constructs which, through stages of refinements, are turned into concrete and imperative constructs. Imperative constructs are thus inevitable in RSL.

```
\begin{array}{c} {\bf Unit} \\ {\bf value} \\ {\tt stmt:} \ {\bf Unit} \rightarrow {\bf Unit} \\ {\tt stmt()} \end{array}
```

- Statements accept no arguments.
- Statement execution changes the state (of declared variables).
- Unit  $\rightarrow$  Unit designates a function from states to states.
- Statements, stmt, denote state-to-state changing functions.
- Writing () as "only" arguments to a function "means" that () is an argument of type Unit.

## **B.8.2** Variables and Assignment

- 0. **variable** v:Type := expression
- $1. \ v := expr$

## B.8.3 Statement Sequences and skip

Sequencing is expressed using the ';' operator. **skip** is the empty statement having no value or side-effect.

- 2. skip
- 3. stm\_1;stm\_2;...;stm\_n

#### **B.8.4** Imperative Conditionals

- 4. if expr then stm\_c else stm\_a end
- 5. case e of:  $p_1 \rightarrow S_1(p_1), \dots, p_n \rightarrow S_n(p_n)$  end

## B.8.5 Iterative Conditionals

- 6. while expr do stm end
- 7. do stmt until expr end

#### B.8.6 Iterative Sequencing

8. for e in list\_expr  $\cdot$  P(b) do S(b) end

## **B.9 Process Constructs**

## **B.9.1 Process Channels**

Let A and B stand for two types of (channel) messages and i:Kldx for channel array indexes, then:

channel c:A
channel { k[i]:B • i:Kldx }

declare a channel, c, and a set (an array) of channels, k[i], capable of communicating values of the designated types (A and B).

## B.9.2 Process Composition

Let P and Q stand for names of process functions, i.e., of functions which express willingness to engage in input and/or output events, thereby communicating over declared channels. Let P() and Q stand for process expressions, then:

- $P \parallel Q$  Parallel composition
- P [] Q Nondeterministic external choice (either/or)
- P [] Q Nondeterministic internal choice (either/or)
- $P \parallel Q$  Interlock parallel composition

express the parallel ( $\parallel$ ) of two processes, or the nondeterministic choice between two processes: either external ( $\parallel$ ) or internal ( $\parallel$ ). The interlock ( $\parallel$ ) composition expresses that the two processes are forced to communicate only with one another, until one of them terminates.

## B.9.3 Input/Output Events

Let c, k[i] and e designate channels of type A and B, then:

c ?, k[i] ? Input c ! e, k[i] ! e Output

expresses the willingness of a process to engage in an event that "reads" an input, respectively "writes" an output.

## **B.9.4 Process Definitions**

The below signatures are just examples. They emphasise that process functions must somehow express, in their signature, via which channels they wish to engage in input and output events.

value P: Unit  $\rightarrow$  in c out k[i] Unit Q: i:Kldx  $\rightarrow$  out c in k[i] Unit

 $\begin{array}{l} \mathsf{P}() \equiv ... \; c \; ? \; ... \; k[i] \; ! \; e \; ... \\ \mathsf{Q}(i) \equiv ... \; k[i] \; ? \; ... \; c \; ! \; e \; ... \end{array}$ 

The process function definitions (i.e., their bodies) express possible events.

# **B.10** Simple RSL Specifications

Often, we do not want to encapsulate small specifications in schemes, classes, and objects, as is often done in RSL. An RSL specification is simply a sequence of one or more types, values (including functions), variables, channels and axioms:

type ... variable ... channel ... value ... axiom ...

In practice a full specification repeats the above listings many times, once for each "module" (i.e., aspect, facet, view) of specification. Each of these modules may be "wrapped" into scheme, class or object definitions.<sup>32</sup>

hd tl inds elems fq iq bn rng

 $<sup>^{32}</sup>$ For schemes, classes and objects we refer to [2, Chap. 10]