## Mandatory Exercise: Suffix Trees

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**1** String Dictionaries with ? Let  $S = s_1 s_2 \cdots s_n$  be a string of length *n* over an alphabet  $\Sigma$ . We are interested in a data structure for *S* that supports the following query.

• search?( $P_1, P_2$ ): return the starting position of all occurrences of  $P_1$ ? $P_2$  in *S*. Here  $P_1$ ? $P_2$  denotes the string  $P_1$  followed by any character (denoted by the ?) followed in turn by the string  $P_2$ .

Give a data structure that supports search?( $P_1$ ,  $P_2$ ) queries efficiently. Your space should be  $O(n \log n)$ . Your query time should be output sensitive, i.e., achieve a bound of the form  $m + f(n) + \operatorname{occ}$ , where  $m = |P_1| + 1 + |P_2|$ , occ is the length of the returned sequence and f(n) is a small function of n.